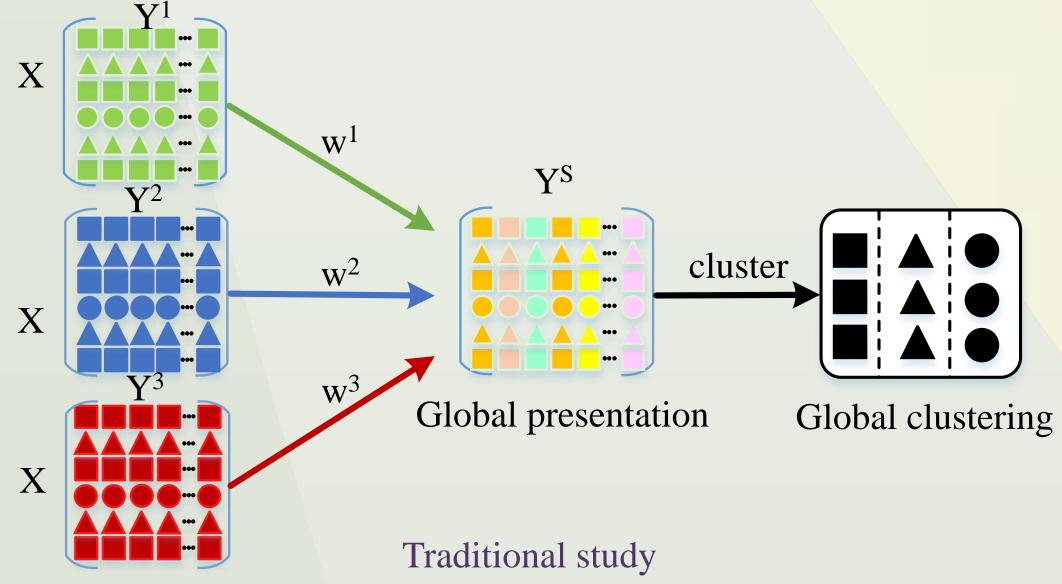
# A Parameter-free Multi-view Information Bottleneck Clustering Method by Cross-view Weighting

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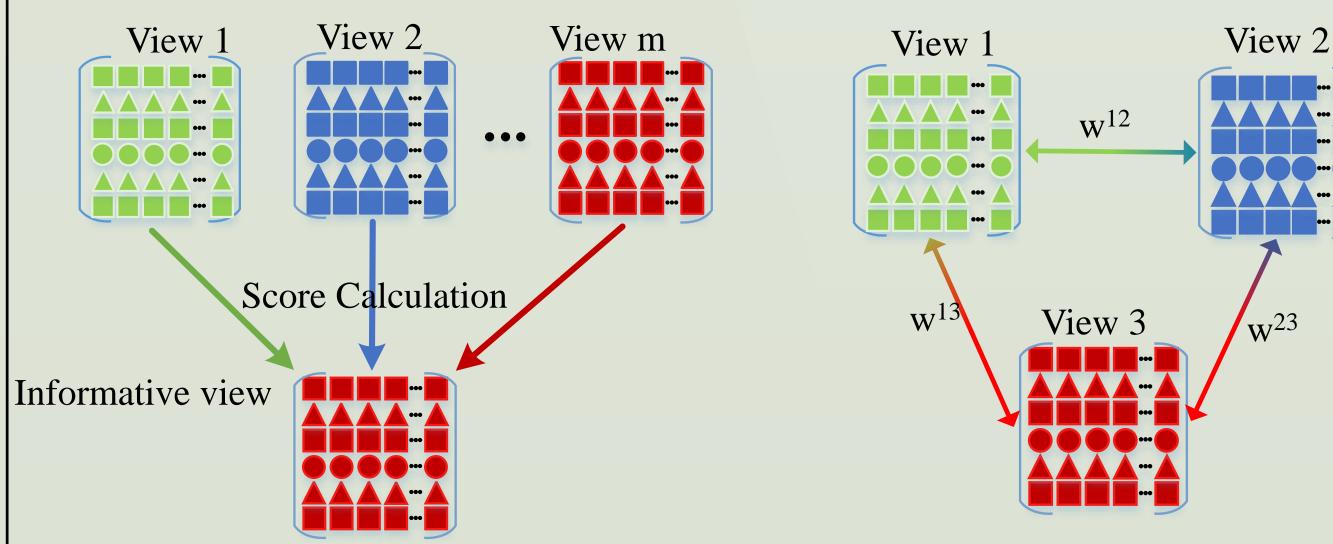
#### **ABSTRACT**

With the fast-growing multi-modal/media data in the Big Data era, multi-view clustering (MVC) has attracted lots of attentions lately. Most MVCs focus on integrating and utilizing the complementary information among views by linear sum of the learned view weights and have shown great success in some fields. However, they fail to quantify how complementary the information across views actually utilized for benefiting final clustering. Additionally, most of them contain at least one parameter for regularization without prior knowledge, which puts pressure on the parameter tuning and thus makes them impractical. In this paper, we propose a novel parameter-free multi-view information bottleneck (PMIB) clustering method to automatically identify and exploit useful complementary information among views, thus reducing the negative impact from the harmful views. Specifically, we first discover the informative view by measuring the relevant information preserved by the original data and the compact clusters with mutual information. Then, a new cross-view weight learning scheme is designed to learn how complementary between the informative view and remaining views. Finally, the quantitative correlations among views are fully exploited to improve the clustering performance without needing any additional parameters or prior knowledge. Experimental results on different kinds of multi-view datasets show the effectiveness of the proposed method.



# **METHODS**

Informative View Discovery. We discover the informative view by measuring the relevant information preserved by the original data and the compact clusters with the concept of MI. On one hand, for the *i*-th view, we calculate and measure the relevant information between the data variable X and its feature variables  $Y^i$  via MI. The higher the MI value obtains, the more informative or relevant the *i*-view is. On the other hand, we perform the IB method on each view to obtain the data assignments, by which we compute the MI between it and the feature variable  $Y^i$ . The higher the MI value obtains, the bigger contribution the current view makes, which thus makes it more informative. Based on the above, we obtain the following score calculation for informative view discovery:



Informative View Discovery

Score= 
$$\frac{I(X;Y^{i}) + I(T^{i};Y^{i})}{\sum_{i=1}^{m} I(X;Y^{i}) + I(T^{i};Y^{i})}$$

Cross-view Weights Learning. Most

existing MVCs utilize the view-weighted

scheme to learn a weight for every view by

measuring the importance of views in order

to employ the complementary information.

view and then combine views together by

is actually utilized for benefiting the data

clustering. Unlike existing view weighted

schemes only considering the importance of

individual view, cross-view weight takes into

account the importance of pairwise views by

quantifying how complementary across

However, they only focus on each individual

linear weighted sum, failing to quantify how

complementary the information across views

**Algorithm 1 The Proposed PMIB method** 

Input:*m* joint distributions  $\{p(X,Y^i)\}_i^{m=1}$ , cluster number *c*. Output: Final data assignments p(t | x).

Cross-View Weighting

 $\lambda^{ij} = \frac{I(V_{row}^{ij}; V_{column}^{ij}) + I(V_{row}^{ji}; V_{column}^{ji})}{I(X; Y^{i}) + I(X; Y^{j})}, w^{ij} = w^{ji} = \frac{\lambda^{ij}}{\sum_{i} \lambda^{ij}}$ 

Initialization:  $T \leftarrow$ Random partition of X into c clusters; Discover the informative view among m views via informative view strategy

Compute the cross-view weights between the informative view and remaining views via cross-view weighting scheme. repeat

for all  $x \in X$  do

Draw: Draw x from the original cluster  $t_{old}$ ;

Merger: Assign x into the clusters of m view, and choose a new cluster  $t_{new}$  with the minimal merger cost by optimization operation. Then, x is merged into the new chosen cluster; end for

until Data samples of clusters in views remain unchanged.

**Objective function:**  $F_{\text{max}}[p(t \mid x)] = S^a \cdot I(T; Y^a) + \sum_{i=1}^{m} w^{ai} \cdot I(T; Y^i)$ 

The advantages of PMIB:

- Usage of quantitative complementary information
- Cross-view weighting
- No parameters are involved

#### **EXPERIMENTS**

$\beta$ : {1,1.5,2,4,6,8} $\lambda$ :[0.01,0.05] (step=0.01)
$\lambda$ :[0.01,0.05] (step=0.01)
$\gamma$ :[0.1,2] (step=0.2)
$\{\lambda_i\}_{i=1}^{m}=1:[0.1,0.9] \text{ (step=0.1)}$
λ:{0.005,0.01,0.05,0.1,0.5}
$\gamma$ :[1,10] (step=1)
$\lambda$ :[1,30] (step= $\lambda$ /2 or $\lambda$ * 2)
$\lambda \ge 1$ : (step= $\lambda/2$ or $\lambda * 2$ )
$\alpha:[2^0, 2^3, \ldots, 2^{15}]$
$anchors = \{c, 2c, 3c\}$
Parameter-free

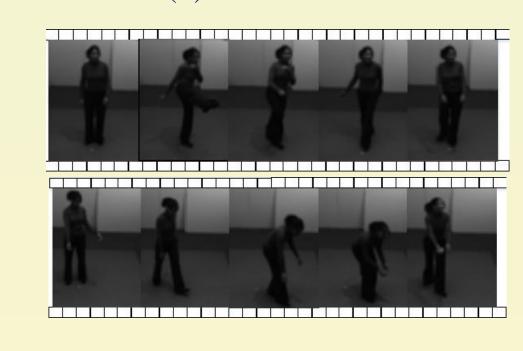
Parameter settings of the compared multi-view clustering methods and ours

Dataset	Type	View	Samples	Clusters	Dimensionality
20NGs	Text	3	500	5	2000
COIL20	Image	3	1440	20	1000
COIL100	Image	2	7200	100	800
IXMAS	Video	4	330	11	1000
arge Dataset	Туре	View	Samples	Clusters	Dimensionality
GHIM	Image	2	10000	20	500
ALOI	Image	3	11025	100	(77, 64, 64)
CIFAR	Image	2	15000	10	1000

Details of the involved multi-view datasets



(a) COIL100



(b) IXMAS

Some datasets examples

	Method	20NGs		COIL20		COIL100		IXMAS	
	Wethod	Acc	NMI	Acc	NMI	Acc	NMI	Acc	NMI
	KM	23.68±0.39	6.41±0.64	52.05±2.25	64.59±1.22	30.17±1.94	62.31±1.91	14.33±2.40	11.56±3.59
	IB	$85.48 \pm 10.57$	$76.07 \pm 7.68$	68.43±3.89	$78.44 \pm 2.61$	$40.76 \pm 1.43$	$68.36 \pm 0.78$	43.63±4.54	41.41±3.70
	AVKM	21.12±0.53	1.49±0.45	44.56±6.84	59.30±7.40	30.53±3.16	51.10±2.93	12.03±2.15	4.80±3.28
	AVIB	91.80±9.88	92.72±6.71	77.52±5.99	91.42±2.55	37.45±2.29	$67.68 \pm 2.45$	26.82±8.98	48.06±8.24
	MVIB (DASFAA'07)	94.22±1.37	83.21±3.18	62.19±10.50	73.54±6.81	46.35±1.68	70.21±0.67	59.03±3.92	57.23±3.06
	Co(reg) (NeurIPS'11)	$20.35 \pm 0.83$	$3.87 \pm 0.73$	$64.75 \pm 1.28$	$84.13 \pm 0.37$	$48.68 \pm 0.47$	$71.19 \pm 0.14$	$17.26 \pm 1.20$	$31.06 \pm 1.14$
	RMKMC (IJCAI'13)	$48.20 \pm 3.43$	$36.86 \pm 4.12$	$53.06 \pm 3.82$	$72.02 \pm 2.99$	45.01±1.61	$68.79 \pm 0.68$	$34.27 \pm 4.34$	$36.20 \pm 3.49$
	MfIB (IJCAI'13)	$93.76 \pm 2.89$	85.11±4.54	$78.99 \pm 3.88$	$88.54 \pm 1.27$	$56.52 \pm 0.08$	$80.81 \pm 0.46$	$64.85 \pm 6.42$	$67.48 \pm 3.21$
	RMSC (AAAI'14)	$37.26 \pm 0.91$	$15.70 \pm 0.84$	$65.45 \pm 4.26$	79.13±1.89	$46.32 \pm 0.28$	$69.33 \pm 0.45$	$52.61 \pm 2.76$	68.79±1.61
	DEKM (CVPR'16)	$31.60 \pm 0.00$	$13.48 \pm 0.00$	$40.69 \pm 0.00$	$59.52 \pm 0.00$	$42.76 \pm 0.00$	$69.57 \pm 0.00$	$17.27 \pm 0.00$	$9.75 \pm 0.00$
	MLAN (TIP'18)	$96.40 \pm 0.11$	89.18±0.17	$86.91 \pm 0.40$	$94.49 \pm 0.00$	$45.05 \pm 0.41$	$59.55 \pm 0.53$	$68.15 \pm 2.57$	$72.23 \pm 1.71$
	GMC (TKDE'20)	$98.20 \pm 0.00$	$93.92 \pm 0.00$	$73.33 \pm 0.00$	$92.11 \pm 0.00$	$38.86 \pm 0.00$	$67.55 \pm 0.00$	$67.58 \pm 0.00$	$78.51 \pm 0.00$
	ONMSC (AAAI'20)	$97.20 \pm 0.00$	$91.48 \pm 0.00$	$13.06 \pm 0.00$	$11.88 \pm 0.00$	$6.47 \pm 0.00$	$18.47 \pm 0.00$	$65.76 \pm 0.00$	$77.67 \pm 0.00$
	SMVSC (ACM MM'21)	$63.70 \pm 5.53$	$50.69 \pm 5.18$	66.15±3.93	82.42±1.16	42.13±0.91	$67.42 \pm 0.73$	$36.06 \pm 2.15$	46.61±0.00
	PMIB (Parameter-free)	99.18±0.24	97.28±0.66	85.83±3.98	93.60±1.72	62.01±1.87	84.59±0.88	73.67±9.51	76.85±6.15

Clustering Results (+/-Standard Deviation) on the Four Multi-view Datasets

## **CONCLUSION**

In this paper, a novel parameter-free multi-view information bottleneck (PMIB) method is proposed to improve the multi-view clustering performance. Unlike existing MVCs utilizing complementary information by linear sum of view weights, PMIB can fully exploit the quantitative complementary information by cross-view weights. Instead of learning view-based weights, a novel cross-view weight learning scheme is designed to accurately quantify the complementary information between views. Additionally, our PMIB is totally parameter-free without involving any parameters or prior knowledge, thus being more practical. Experimental results on different kinds of multi-view datasets show the effectiveness of the proposed method. In the future, we plan to extend our method to address more complicated incomplete multi-view clustering for broad applications.

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