

## High Performance Computing for Science and Engineering I

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## Set 5 - MPI Part II

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**Grading:** To get full credits solve **all** of the questions.

## Question 1: Diffusion (100 points)

The diffusion of a substance can be described by the equation

$$\frac{\partial c(x,y,t)}{\partial t} = D\left(\frac{\partial^2 c(x,y,t)}{\partial x^2} + \frac{\partial^2 c(x,y,t)}{\partial y^2}\right),\,$$

where c is the concentration of the substance at position (x, y) and at time t, and D is the diffusion constant. The diffusion process happens in the domain |x| < L/2 and |y| < L/2. The concentration is zero on the boundaries of the domain. The initial concentration is

$$c(x, y, 0) = \begin{cases} 1, & \text{if } |x| < L/4 \text{ and } |y| < L/4, \\ 0, & \text{otherwise.} \end{cases}$$

- a) The skeleton code solves the equation on a uniform grid using a central finite difference scheme in space and forward Euler time integration. Parallellize the code by filling parts marked by TODO in the functions advance and main. Use a tiling decomposition scheme (i.e., distribute the rows evenly to the MPI processes). How to run the code:
  - make to compile the code
  - make run to run single core (please not in the login node on euler!). If not locally on the laptop, use sbatch launch\_single.sh to submit a job via slurm.
  - to run multicore use: mpirun -n x ./diffusion D L N. You can also use sbatch launch\_single.sh to submit a job via slurm.
- b) For a given time compute the integral of c(x,y,t) over the domain (total ammount of the substance). Fill the missing MPI parts in compute\_diagnostics, and plot the result as a function of time using  $D=1,\ L=2$  and N=100. When run correctly, the code will output file called diagnostics.dat. To plot this data use python plot\_diagnostics.py (module load python).
- c) For a given time compute the histogram of c(x,y,t) in the function compute\_histogram by implementing the missing MPI parts marked by TODO, and plot or print the resulting histogram for t=0.5 using D=1, L=2 and N=100.

- d) Suggest other ways to divide the real-space domain between processes with the aim of minimizing communication overhead. Prove your argument by computing the message communication size for the tiling domain decomposition and for your suggestion.
- e) Make a strong and weak scaling plot up to 48 cores. Justify what is happening in your plots. Make at least five different numbers of cores runs (e.g. [1, 12, 24, 36, 48] or [1, 2, 4, 8, 16]). For the strong scaling plot use:  $N = \{1024, 2048, 4096, 8192\}$ , in other words, plot at least four lines (if too slow use smaller N's). For the weak scaling plot, use N = 1024 and N = 2048 (if those are taking too long use smaller N's). Use D = 1, L = 2 and modify the number of timesteps step = 100. Do not forget to state which CPU you ran the tests on! You can use the run.sh script to run for different number of cores. On euler use run.sh via sbatch launch.sh. Draw the plots either directly on the paper (which is the way you will do it on the exam). Or use any desired ploting scripts.