=) 
$$V(t,t_0) = V(t,0) = (\cos\theta / 1 + i \sin\theta \frac{S_z}{2})$$
  
 $\theta = \frac{rBt}{2}$ 

$$\hat{S}_z(t) = V(0,t) \hat{S}_z V(t,00)$$

$$=$$
  $S_{Z}$ 

$$\hat{S}_{x}(t) = V^{\dagger}(t,0) \hat{S}_{x}V(t,0)$$

= 
$$(\cos\theta 1 - i\sin\theta \frac{S_z}{h/2})$$
  $S_{\infty}$   $(\cos\theta 1 + i\sin\theta \frac{S_z}{h/2})$ 

= 
$$\cos^2\theta S_x + \sin^2\theta (-S_x)$$

now 
$$[\hat{S}_z, \hat{S}_{\infty}] = i\hbar \hat{S}_y$$

$$\Rightarrow \hat{S}_x(t) = \cos 2\theta \hat{S}_x + i\sin 2\theta \hat{S}_y$$

$$\Rightarrow \hat{S}_x(t) = \cos (\beta t) \hat{S}_x + i\sin (\gamma b t) \hat{S}_y$$

$$\hat{S}_y(t) = \left(\cos \theta 1 - i\sin \theta \frac{S_z}{\hbar h}\right) \hat{S}_y \left(\cos \theta 1 + i\sin \theta \frac{S_z}{\hbar h}\right)$$

$$= \cos^2 \theta \hat{S}_y - \sin^2 \theta \hat{S}_y + i\sin 2\theta [\hat{S}_y, \hat{S}_z]$$

$$= \cos^2 \theta \hat{S}_y - \sin^2 \theta \hat{S}_y$$

$$\Rightarrow \hat{S}_y(t) = \cos^2 \theta \hat{S}_y - \sin^2 \theta \hat{S}_y$$

$$\Rightarrow \hat{S}_y(t) = \cos^2 \theta \hat{S}_y - \sin^2 \theta \hat{S}_y$$