## **Assignment 1**

**AI1110**: Probability and Random Variables Indian Institute of Technology Hyderabad

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**12.13.6.3: Question**. Suppose that 5% of men and 0.25% of women have grey hair. A grey haired person is selected at random. What is the probability of this person being male? Assume that there are equal number of males and females.

Answer:  $\frac{20}{21}$ .

**Solution**: Let us conside a random variable X which depicts whether a person is a male of female.

X = 0, a person being a male X = 1, a person being a female

As given the question that there are equal number of males and females,

$$Pr(X = 0) = \frac{1}{2}$$
  
 $Pr(X = 1) = \frac{1}{2}$ 

And let E be the event where a person has grey hair. Given,

$$Pr(E|X = 0) = \frac{5}{100}$$

$$Pr(E|X = 1) = \frac{0.25}{100}$$

Now ,the probability that the selected person is male given that he's grey haired is Pr(X = 0|E) which is equal to

$$\Pr(X = 0|E) = \frac{\Pr(E + X = 0)}{\Pr(E)}$$

$$\Rightarrow \frac{\Pr(E|X = 0)\Pr(X = 0)}{\Pr(E)}$$

$$\Rightarrow \frac{\Pr(E|X = 0)\Pr(X = 0)}{\Pr(E|X = 0)\Pr(X = 0)}$$

Substitutuing all the values,

$$\Pr(X = 0|E) = \frac{\frac{5}{100} \frac{1}{2}}{\frac{5}{100} \frac{1}{2} + \frac{0.25}{100} * \frac{1}{2}}$$
$$= \frac{5}{5.25}$$
$$= \frac{20}{21}$$

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Therefore, the required probability is  $\frac{20}{21}$ .