

The component of u orthogonal to w is

$$\begin{aligned}\text{Proj}_w^\perp u &= u - \text{Proj}_w u \\ &= (1, 1, 1) - \left(\frac{4}{25}, 1, -\frac{3}{25}\right)\end{aligned}$$

$$\boxed{\text{Proj}_w^\perp u = \left(\frac{21}{25}, 0, \frac{28}{25}\right)}$$

GRAM-Schmidt Process:-

To convert a basis vectors u_1, u_2, \dots, u_n in an orthogonal (perpendicular) vectors perform the following computations.

Step 01

$$v_1 = u_1$$

Step 02

$$v_2 = u_2 - \text{Proj}_{v_1} u_2$$

$$v_2 = u_2 - \frac{\langle u_2, v_1 \rangle}{\|v_1\|^2} v_1$$