

$$K_1 + K_2 + 2K_3 = b_1$$

$$K_1 + K_3 = b_2$$

$$2K_1 + K_2 + 3K_3 = b_3$$

$$A = \begin{bmatrix} 1 & 1 & 2 \\ 1 & 0 & 1 \\ 2 & 1 & 3 \end{bmatrix}$$

$$|A| = 1(0-1) - 1(3-2) + 2(1-0)$$

$$|A| = -1 - 1 + 2$$

$$|A| = 0$$

$$\det(A) = 0$$

So, v_1, v_2, v_3 do not span.

$$\textcircled{2} \quad v_1 = (2, 2, 2), v_2 = (0, 0, 3), v_3 = (0, 1, 1)$$

Solution

$$b = K_1 v_1 + K_2 v_2 + K_3 v_3$$

$$(b_1, b_2, b_3) = K_1(2, 2, 2) + K_2(0, 0, 3) + K_3(0, 1, 1)$$

$$2K_1 = b_1$$

$$2K_1 + K_3 = b_2$$

$$2K_1 + 3K_2 + K_3 = b_3$$

$$A = \begin{bmatrix} 2 & 0 & 0 \\ 2 & 0 & 1 \\ 2 & 3 & 1 \end{bmatrix}$$