

$$u + (-u) = \begin{bmatrix} a_1 & -a_1 & 0 \\ 0 & 0 & b_1 - b_1 \end{bmatrix}$$

$$u + (-u) = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$$

Hence, for every $u \in V$ there is an inverse element $-u \in V$.

Axioms 06

$$ku \in V$$

Let k is any scalar in R then ku is also be in R .

$$ku = k \begin{bmatrix} a_1 & 0 \\ 0 & b_1 \end{bmatrix} = \begin{bmatrix} ka_1 & 0 \\ 0 & kb_1 \end{bmatrix}$$

Hence, Axiom 6 satisfied in V , because $u \in V$ and k is any scalar then $ku \in V$.

Axioms 07

Let k is scalar, show that $k(u+v) = ku + kv$

$$k(u+v) = k \left(\begin{bmatrix} a_1 & 0 \\ 0 & b_1 \end{bmatrix} + \begin{bmatrix} a_2 & 0 \\ 0 & b_2 \end{bmatrix} \right)$$