

Question The set of all pairs of Real number
 (x, y) with the operations.
 $(x, y) + (x', y') = (x+x', y+y')$
 $K(x, y) = (x, Ky)$

Solution :-

→ Axioms 07

$$K(u+v) = Ku + Kv$$

$$u = (x, y), \quad v = (x', y')$$

$$\begin{aligned} K(u+v) &= K((x, y) \oplus (x', y')) \\ &= K((x+x'), (y+y')) \\ &= ((x+x'), K(y+y')) \\ &= ((x, Ky) + (x', Ky')) \end{aligned}$$

$$Ku + Kv = K(x, y) \oplus K(x', y')$$

(Not Hold)

→ Axioms 08

$$(K+C)u = Ku + Cu$$

$$\begin{aligned} (K+C)u &= (K+C) \cdot (x, y) \\ &= (x, (K+C)y) \\ &= (x, Ky + Cy) \end{aligned}$$

$$\begin{aligned} Ku + Cu &= K(x, y) + C(x, y) \\ &= (x, Ky) + (x, Cy) \\ &= (2x, Ky + Cy) \end{aligned}$$

L.H.S \neq R.H.S

(Not Hold)