

# Linear Algebra

## GENERAL VECTOR SPACES

CHAPTER 05

Vector Space Axioms :-

$V$  - a set whose elements are called vectors.

$F$  - a set of numbers called scalars.

Two Operations defined on  $V$ .

1. Vector Addition.

2. Scalar Multiplication.

$u, v$  and  $w$  are vectors in  $V$ .

$k$  and  $c$  are Real numbers.

Axioms :- Vector Addition Axioms

1.  $u + v \in V$  Closure Under Addition.

2.  $u + v = v + u$  Commutative.

3.  $u + (v + w) = (u + v) + w$  Associative.

4.  $V$  has an additive identity  $0$

Such that for every  $v$  in  $V$

$$v + 0 = v \quad (\text{additive identity})$$

5. For every  $v$  in  $V$  there is an additive inverse  $-v$  such that

$$v + (-v) = 0$$