

Matrix of  $T$  corresponding to  $B$  is

$$[T: B] = [T]_B = \begin{bmatrix} 0 & 2 & 1 \\ 1 & -4 & 0 \\ 3 & 0 & 0 \end{bmatrix}$$

Solution

$$T(a, b, c) = (2b + c, a - 4b, 3a)$$

$$T(1, 1, 1) = (3, -3, 3)$$

$$T(1, 1, 0) = (2, -3, 3)$$

$$T(1, 0, 0) = (0, 1, 3)$$

Let,

$$(a, b, c) = x(1, 1, 1) + y(1, 1, 0) + z(1, 0, 0)$$
$$(a, b, c) = (x + y + z, x + y, x)$$

$$a = x + y + z$$

$$b = x + y$$

$$c = x$$

$$\boxed{x = c}$$