

Unit - 1Basic Definitions →

- 1) Circuit : An Electric Circuit is a closed path Component of active and Elements to which Current can flow.
- 2) Electric Network → A Combination of various Electric Elements Connected in any manner whatever is called Electric network.
- 3) Excitation → The input to a network is referred to as Excitation that is the Excitation represents Energy Supply to the network from an External Source.
- 4) Response → The Output of the network is called Response that is Response represents the Utilization of Energy Supply by the Excitation.
- 5) Active Element → Any Energy Source that is a Voltage or a Current Source is said to be an Active Element. which are Energy producing Element
Eg. Current & Voltage Source.
- 6) Passive Element : An Element which is not an Energy Source is a Passive Element. A Passive Element transform or a Stored Energy either in the form of magnetic field or electric field Eg. Capacitor and Inductor

7) Bilateral and Unilateral Elements \Rightarrow

Bilateral Elements are those which transmit equally in either direction. Eg Transmission line.

On the other hand, Unilateral Element conduct only in one direction Eg Diode

8) Linear and Non Linear Elements \Rightarrow

These are Elements in whose Case response is directly proportional to the Excitation that is they follow OHM's Law. These Element are called as linear Elements While non-linear Elements are those Elements where the output is independent of the input & they also do not follow Ohm's law.

Eg. of Linear Elements : Resistance

Eg. of Non-Linear Elements : Vacuum tubes.

9) Lumped and distributed Parameter \Rightarrow Physically, Separate Elements such as resistor, inductor and capacitor are known as Lumped Elements

While the distributed elements are those elements which are not separated for Analytics purpose

An Example of a Circuit with distributed Elements is a transmission line.

Where the Elements in which R, L, G, C are distributed throughout the whole length of the line.

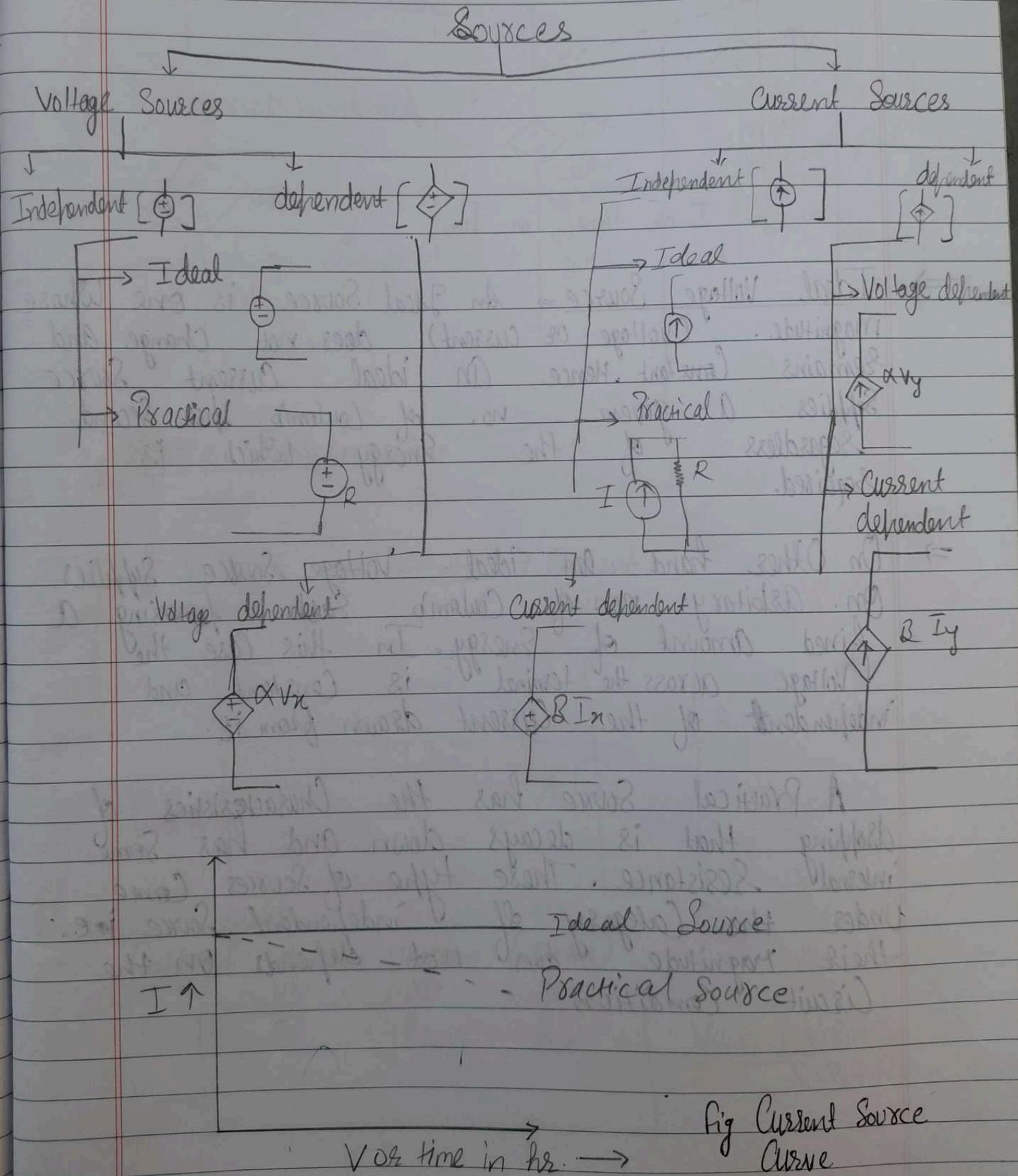
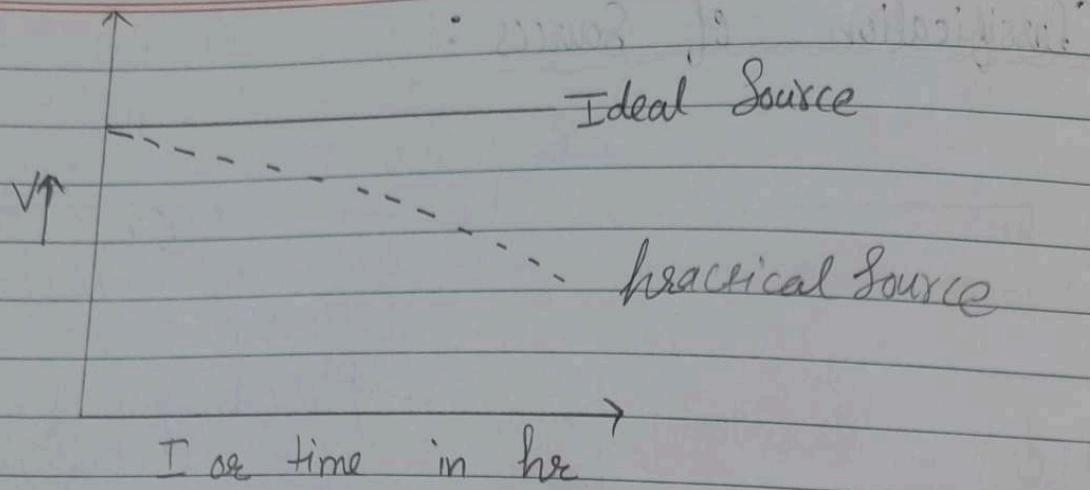
Classification of Sources :

Fig Current Source Curve

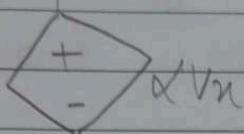


\Rightarrow Ideal Voltage Source \Rightarrow An Ideal Source is one whose magnitude. (Voltage or Current) does not change and remains constant. Hence An ideal Current Source supplies a given no. of Coulomb per second regardless of the Energy which is required.

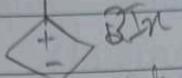
\Rightarrow On Other hand an ideal Voltage Source supplies an arbitrary no. of Coulomb Each passing a fixed amount of Energy. In this Case the Voltage across the terminal is Constant and independent of the Current drawn from it.

A Practical Source has the Characteristics of dropping that is decays down and has some internal resistance. These type of sources come under the Category of independent Source i.e. their magnitude does not depends on the Circuit Condition.

Dependent Sources \Rightarrow



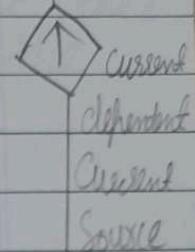
Voltage dependent
Voltage Source



Current
dependent
voltage
source



Voltage
dependent
current
source

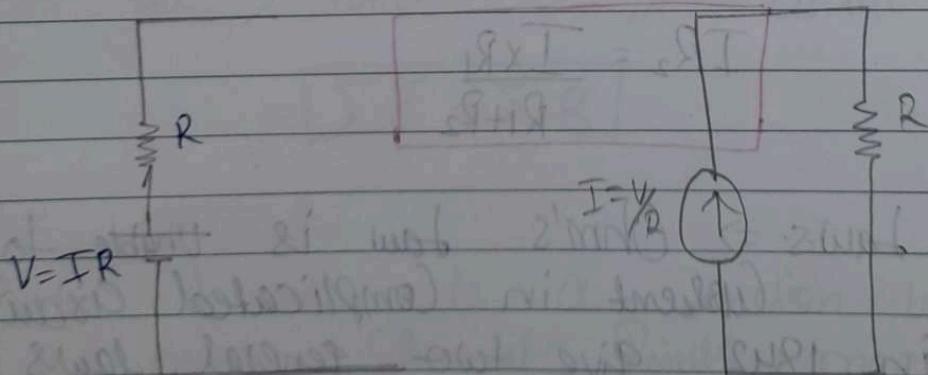


Current
dependent
current
source

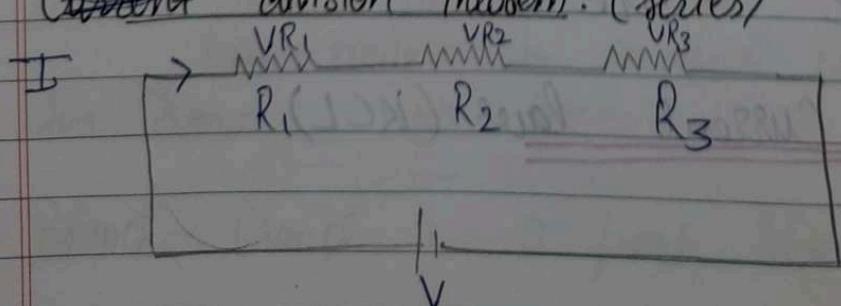
Source Transformation

Voltage
Source

Current
Source



Current division theorem: (series)

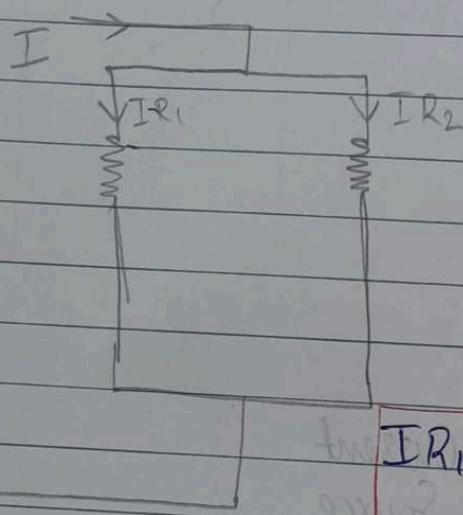


$$VR_1 = \frac{V \times R_1}{R_1 + R_2 + R_3}$$

$$VR_2 = \frac{V \times R_2}{R_1 + R_2 + R_3}$$

$$VR_3 = \frac{V \times R_3}{R_1 + R_2 + R_3}$$

Current division Theorem
(Parallel)



$$IR_1 = \frac{I \times R_2}{R_1 + R_2}$$

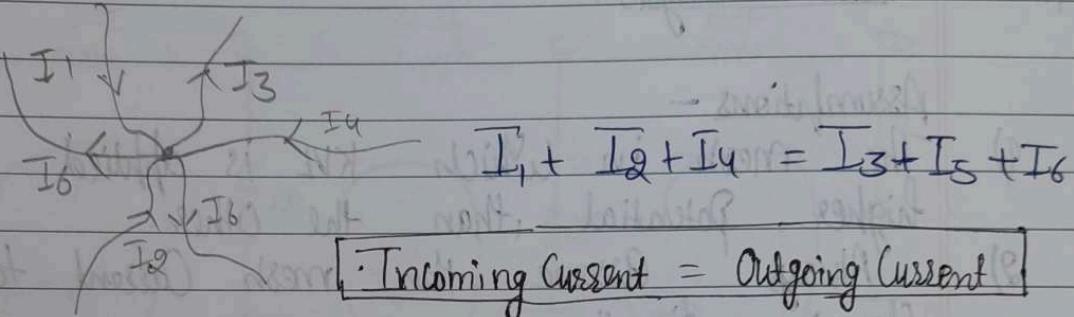
$$IR_2 = \frac{I \times R_1}{R_1 + R_2}$$

Kirchhoff's Laws \Rightarrow Ohm's law is unable to give current in complicated circuit.
Kirchhoff in 1842 give two general laws which are extremely useful in Electric Electrical Circuits. These are

(1) Kirchhoff Current Law (KCL)

\Rightarrow The algebraic sum of the current at any junction in a circuit is zero
 $\sum i = 0$

The current which flows towards a point are taken as +ve while those flowing away from the point are taken as -ve (negative)



Kirchhoff Voltage Law \Rightarrow If any closed circuit the algebraic sum of the products of the current and resistance in any closed circuit of each part of the circuit is the total EMF in circuit

$$\boxed{\sum E \Rightarrow \sum IR}$$

Node : A node is a junction where two or more elemental points meet.

Path : Path is the route through elements from one node to another without going through the same node twice.

Branch : Branch is a part between two adjoining nodes

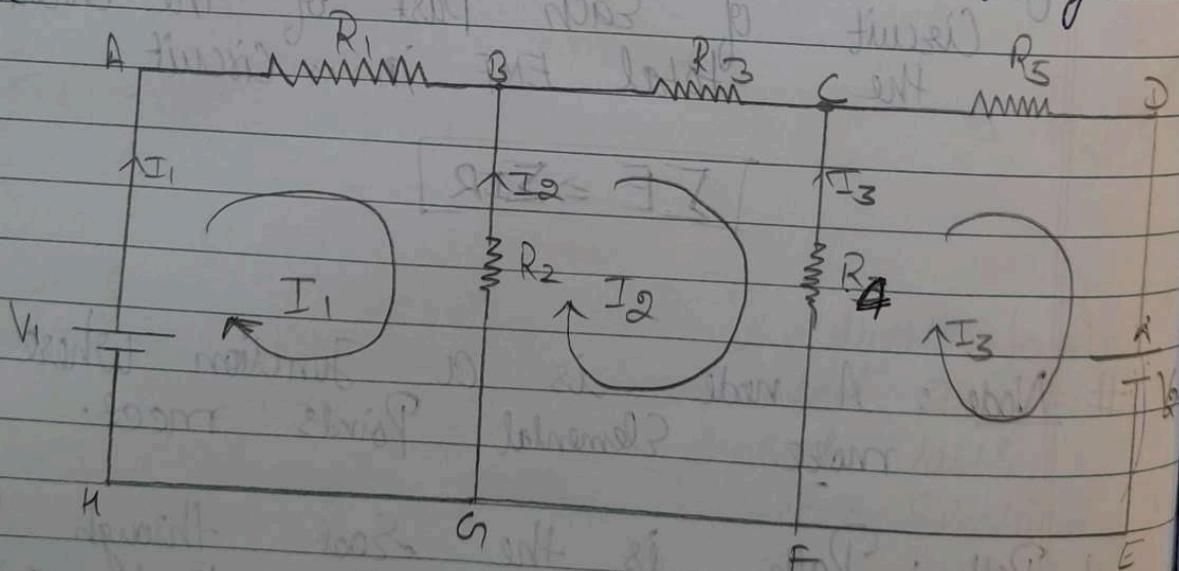
Loop : Loop is a closed path where the loop ends upon the starting node.

Mesh : Mesh is a loop that does not contain any other loop in it.

Mesh Analysis :

Assumptions -

- (1) The mesh in which KVL is applied is at a higher potential than the other.
- (2) Always assume the mesh current to be in clockwise direction.
- (3) All the sources must be voltage source. If my practical current source is there it means to convert into its equivalent voltage source.



In ABCDA.

$$V_1 = I_1 R_1 + R_2 (I_1 - I_2) - \textcircled{1}$$

In loop BCFCGB

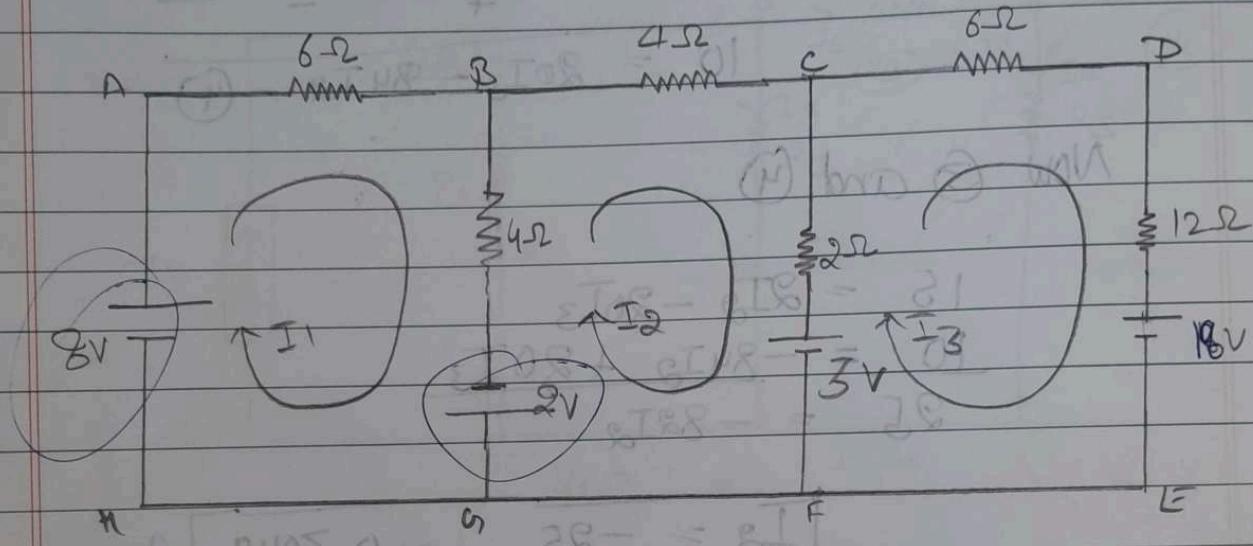
$$0 = R_3 I_3 + R_1 (I_2 - I_3) + R_2 (I_2 - I_1) - \textcircled{2}$$

In loop CDEFH

$$-V_b = R_5 I_3 + R_4 (I_3 - I_2) - \textcircled{3}$$

$$I_1, I_2, I_3 = ?$$

Eq



Solve In loop ABCGHA

$$8+2 = 6I_1 + 4(I_1 - I_2)$$

$$10 = 6I_1 + 4I_1 - 4I_2$$

$$10 = 10I_1 - 4I_2 \quad \textcircled{1}$$

In loop BCFCGB

$$-2-3 = 4(I_2 - I_1) + 4I_2 + 2(I_2 - I_3)$$

$$-5 = 10I_2 - 4I_1 - 2I_3 \quad \textcircled{2}$$

$$-5 = 4I_1 - 10I_2 + 2I_3$$

In loop CDEFH =

$$3-18 = 6I_3 + 12I_3 + 2(I_3 - I_2)$$

$$-15 = 20I_3 - 2I_2$$

$$15 = 2I_2 - 20I_3 \quad \textcircled{3}$$

By Solving eqn ① - ④

$$4(10 = 10I_1 - 4I_2)$$

$$10(5 = 4I_1 - 110I_2 + 2I_3)$$

$$40 = 40I_1 - 16I_2$$

$$\underline{50} = \underline{-10I_1 - 100I_2 + 20I_3}$$

$$10 = 20I_3 - 84I_2 \quad \text{--- (4)}$$

Now ③ and ④

$$15 = 2I_2 - 20I_3$$

$$10 = -84I_2 + 20I_3$$

$$25 = -82I_2$$

$$I_2 = \frac{-25}{82} = -0.3049 \quad \boxed{\text{Ans.}}$$

From eqn ③

$$\boxed{\begin{aligned} I_1 &= 0.878 \\ I_3 &= -0.7805 \end{aligned}} \quad \boxed{\text{Ans.}}$$

Nodal Analysis \Rightarrow A node is a terminal or collection of more than two elements. In Nodal Analysis, KCL is applicable.

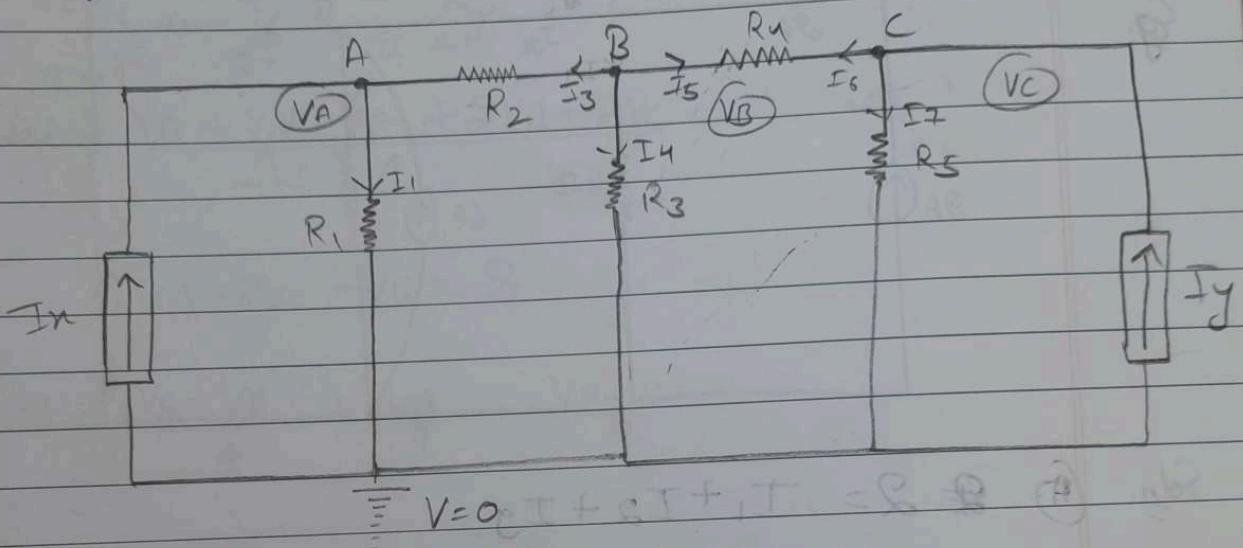
Assumption:

1) All the Sources must be Current Sources

If any practical Voltage Source is there it has to be controlled into its Equivalent

Current Sources.

- 2) Always assume that unknown current through the element to be flowing away from the node. This means that, the node at which KCL is applied is at upper potential or higher potential than the other.



$$\text{At } B: I_B = I_1 + I_2 \quad (1)$$

$$\text{At } B: 0 = I_3 + I_4 + I_5 \quad (2)$$

$$\text{At } C: I_y = I_6 + I_7 \quad (3)$$

$$I_1 = \frac{V_A - 0}{R_1} \quad I_2 = \frac{V_A - V_B}{R_2}, \quad I_3 = \frac{V_B - V_A}{R_2}, \quad I_4 = \frac{V_B - 0}{R_3}$$

$$I_5 = \frac{V_B - V_C}{R_4}, \quad I_6 = \frac{V_C - V_B}{R_4}, \quad I_7 = \frac{V_C - 0}{R_5}$$

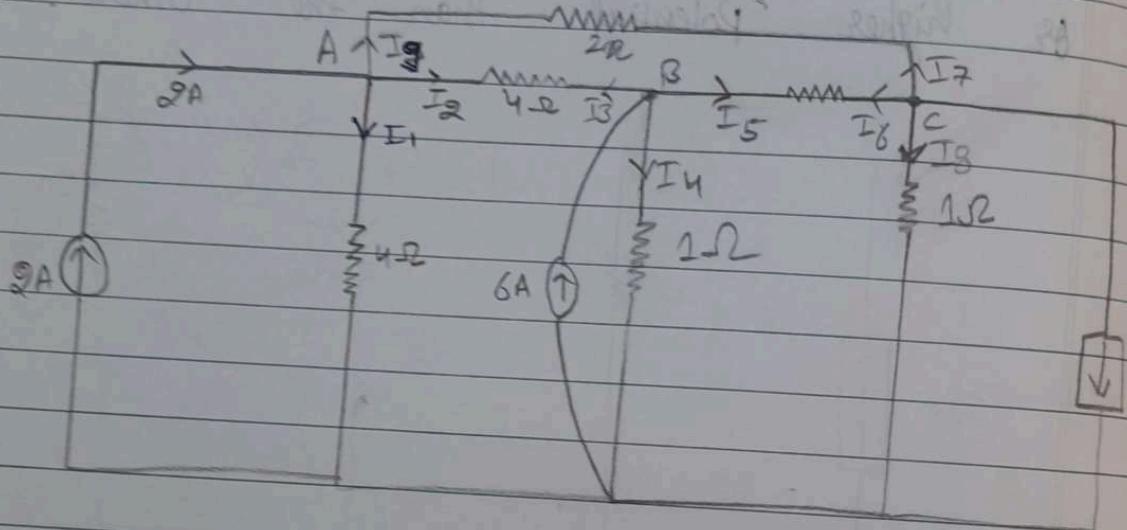
$$I_{1x} = \frac{V_A}{R_1} + \frac{V_A - V_B}{R_2} \quad (4)$$

$$0 = \frac{V_B - V_A}{R_2} + \frac{V_B}{R_3} + \frac{V_B - V_C}{R_4} \quad (5)$$

$$I_y = \frac{V_c - V_B}{R_4} + \frac{V_c}{R_5} - \textcircled{6}$$

find $V_A, V_B, V_c = ?$

Q.



$$\text{Soh} \quad \textcircled{1} \quad 2 = I_1 + I_2 + I_3$$

$$\textcircled{2} \quad 0 = I_3 + I_4 + I_5$$

$$\textcircled{3} \quad 0 = 10 + I_8 + I_6 + I_7$$

$$I_1 = \frac{V_A}{4}, \quad I_3 = \frac{V_B - V_A}{4}, \quad I_5 = \frac{V_B - V_C}{2}$$

$$I_2 = \frac{V_A - V_B}{4}, \quad I_4 = \frac{V_B - 0}{1}, \quad I_6 = \frac{V_C - V_B}{2}$$

$$I_7 = \frac{V_C - 0}{1}, \quad I_8 = \frac{V_C - V_A}{2}, \quad I_9 = \frac{V_A - V_C}{2}$$

$$\Rightarrow Q = \frac{V_A}{4} + \frac{V_A - V_B}{4} + \frac{V_B - V_A}{2}$$

$$V_B = 8$$

$$\Rightarrow Q = \frac{V_A}{4} + \frac{V_A - V_B}{4} + \frac{V_A - V_C}{2}$$

$$8 = V_A + V_A - V_B + 2V_A - 2V_C$$

1

$$4V_A - 2V_C - V_B = 8$$

$$\Rightarrow 0 = \frac{V_B - V_A}{4} + \frac{V_B}{1} + \frac{V_B - V_C}{2}$$

$$V_B - V_A + 4V_B + 2V_B - 2V_C = 0$$

$$[7V_B - V_A - 2V_C = 0]$$

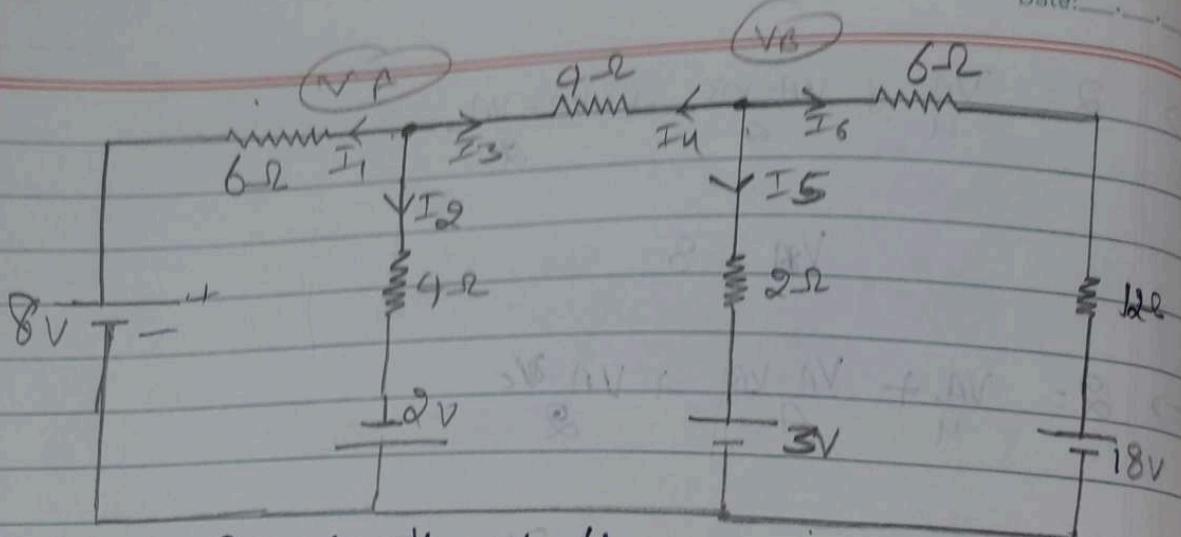
$$\Rightarrow 0 = 10 + \frac{V_C - V_A}{2} + \frac{V_C - V_B}{2} + \frac{V_C}{1}$$

$$20 + V_C - V_A + V_C - V_B + 2V_C = 0$$

$$\text{So } V_A \Rightarrow 0.39 \text{ Volt}$$

$$V_B \Rightarrow 0.243 \text{ Volt}$$

$$V_C = -4.34 \text{ Volt}$$



Find the current through the various resistance by using the nodal analysis.

So $\underline{I_n}$

$$I_1 + I_2 + I_3 = 0 \quad (1)$$

$$I_4 + I_5 + I_6 = 0 \quad (2)$$

$$I_1 = \frac{VA - 8}{6}, \quad I_2 = \frac{VA + 2}{4}$$

$$I_3 = \frac{VA - VB}{4}, \quad I_4 = \frac{VB - VA}{4}$$

$$I_5 = \frac{VB - 3}{2}, \quad I_6 = \frac{VB - 18}{12 + 6}$$

Put value of I_1, I_2, I_3 in eq ①

$$\frac{VA - 8}{6} + \frac{VA + 2}{4} + \frac{VA - VB}{4} = 0$$

$$2VA - 16 + 3VA + 6 + 3VA - 3VB = 0 \\ 8VA - 3VB - 10 = 0 \quad (3)$$

Put value of I_4, I_8, I_6 in eq(9)

$$\frac{V_B - V_A}{4} + \frac{V_B - 3}{2} + \frac{V_B - 18}{18}$$

$$\Rightarrow 29V_B - 9V_A - 90 = 0 \quad (2)$$

On Solving $\Rightarrow (3)$ and (4)

$$8 \times 29V_B - 9V_A - 90 = 0$$

$$9 \times -3V_B + 8V_A - 10 = 0$$

$$205V_B - 810 = 0$$

$$V_B = \frac{810}{205} \quad \boxed{V_B = 3.95}$$

Put value of V_B in eq(3)

$$I_1 = \frac{V_A - 8}{6} = \frac{2.74 - 8}{6} = -0.87$$

$$I_2 = \frac{V_A + 2}{4} = 1.185, \quad I_3 = \frac{V_A - V_B}{4} = -0.30$$

$$I_4 = \frac{V_B - V_A}{4} = 0.30 \quad I_5 = \frac{V_B - 3}{2} = 0.47$$

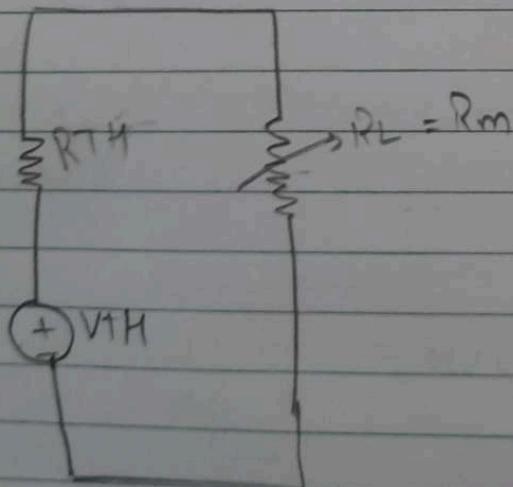
$$I_6 = \frac{V_B - 18}{18} = 0.78$$

Maximum Power \Rightarrow

Transfer Theorem \Rightarrow

Maximum Power transfer theorem determines the value of load resistance which result maximum power transfer across the terminals of an active network.

Statement: The Theorem State that when the load resistance is equal to the internal resistance of the system, Maximum power is transferred to the load. This Internal resistance is the Thvenin Equivalent Resistance of the network as seen from the load terminal.



Let a generator having voltage V_{TH} an internal resistance R_{TH} delivers power to the load resistance R_L .

$$I_L = \frac{V_{TH}}{R_{TH} + R_L}$$

The current through the load R_L \rightarrow Q1

$$\frac{1}{(R_{TH} + R_L)}$$

The Power supplied to the load R_L

$$P_L = I_L^2 R_L \quad \text{--- (2)}$$

Put value of I_L from eq(1) in eq(2)

$$P_L = \left(\frac{V_{th}}{R_{th} + R_L} \right)^2 \times R_L \quad \text{--- (3)}$$

\Rightarrow For the Power transferred to the load to be max.

differentiate eq(3) w.r.t R_L and equate it at 0.

$$\frac{d P_L}{d R_L} = 0.$$

$$P_L = \left(\frac{V_{th}}{R_{th} + R_L} \right)^2 \times R_L$$

$$\Rightarrow \frac{d \left(\frac{V_{th}}{R_{th} + R_L} \right)^2 \times R_L}{d R_L} = 0. \Rightarrow \frac{(V_{th})^2}{(R_{th} + R_L)^2} \times R_L = 0.$$

by using Product Rule

$$\Rightarrow \left[\frac{V_{th}}{R_{th} + R_L} \right]^2 \times 1 + \left[\frac{(R_{th} + R_L)^2 (V_{th})^2}{(R_{th} + R_L)^4} - 2(R_{th} + R_L)(0+1) \right] R_L = 0$$

$$\left[\frac{V_{th}}{R_{th} + R_L} \right]^2 + \left[\frac{0 - 2(R_{th} + R_L) R_L}{(R_{th} + R_L)^4} \right] = 0$$

$$\frac{1}{(R_{th} + R_L)^2} \left[\frac{(V_{th})^2 (R_{th} + R_L)^2 - 2(R_{th} + R_L) \times R_L}{(R_{th} + R_L)^2} \right] = 0$$

$$\left[\frac{V_{th}}{R_{th} + R_L} \right]^2 = \frac{2(R_{th} + R_L)(V_{th})^2 \times R_L}{(R_{th} + R_L)^4}$$

$$\left[\frac{V_{th}}{R_{th} + R_L} \right]^2 = \frac{2(R_{th} + R_L)(V_{th})^2 \times R_L}{(R_{th} + R_L)^2 (R_{th} + R_L)^2}$$

$$R_{th} + R_L = 2RL$$

$$R_{th} = RL$$

The value of maximum Power

$$P_{max.} = \left[\frac{V_{th}}{R_{th} + R_L} \right]^2 \times R_L$$

$$P_{max.} = \frac{(V_{th})^2}{4(R_{th})} \times R_L$$

$$P_{max.} \rightarrow \frac{(V_{th})^2}{4(R_{th})}$$

Under Condition of max. Power transfer. Power output for the Source is gain

$$\eta = \frac{P_{Lmax.}}{P} = \frac{1}{2}$$

~~$$\text{or } \eta = r$$~~

$$P_L = V_{th} \times \frac{V_{th}}{2R_{th}}$$

The Efficiency of power transfer is defined by the ratio of average Power Consumed by the load and total Power Supplied to the load.

$$\eta = \frac{P_{Lmax.}}{P} = \frac{1}{2}$$

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Date: _____

Notes

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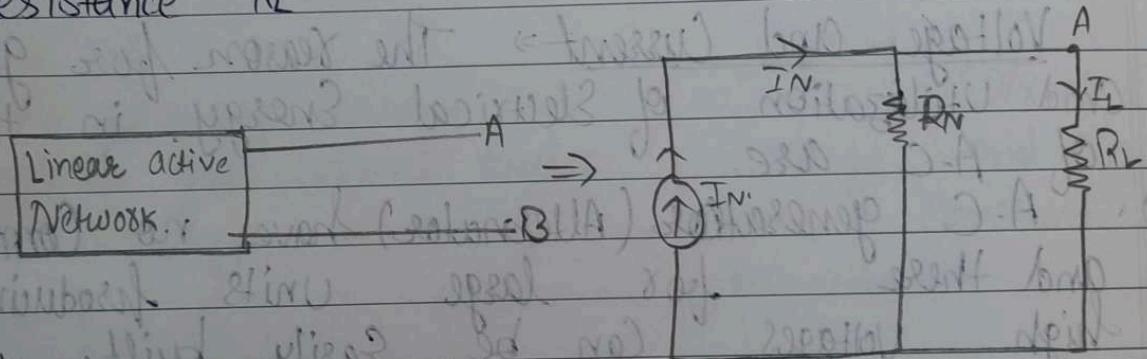
④

⑤

R

$$\text{or } m = 50 \cdot 1.$$

Norton's Theorem \Rightarrow This theorem state that any linear active network (having voltage and current sources and resistances) with output terminal "AB" can be replaced by a single current source I_N in parallel with resistance R_N . through The Current to the Load resistance R_L



$$I_L = \frac{I_N \cdot R_N}{R_N + R_L}$$

Procedure: (1) Remove the Load Element.

(2) Calculate the Short Circuit Current or Norton's Current I_N .

(3) Cal. the Norton's resistance R_N as seen from the load terminal AB

(4) Draw Norton's Equivalent Circuit.

(5) Re connect the load resistance R_L .

15/11/2021

UNIT-II^{nd.}

Sinusoidal (A.C)

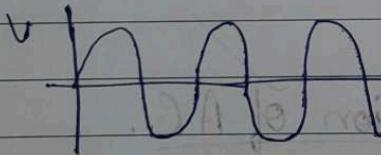
Voltage and Current \Rightarrow The reason for generation and utilization of Electrical Energy, in the form of A.C are

- ① A.C generator (Alternator) have no Commutator and these for large units producing high voltages can be easily built.
- ② It is very easy to change the voltage level by use of transformer. Hence high transmission efficiency can be achieved in transferring electric energy from one place to another.
- ③ Cost wise the generation of A.C. is cheap.
- ④ The A.C motors are cheap robust and single ~~as~~ compare to D.C motors.

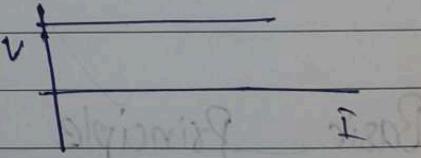
5. The Switch gear Equipment used in Sub-Station for e.g., Circuit breaker, Switches, etc. are also simple in Case of A.C as Compared to D.C.
6. The maintenance requirement and the Cost of A.C. machine and equipment is almost negligible as Compared to D.C.

~~If~~ Even If A.C. Unsuitable for certain applications it can be easily converted to D.C by using Rectifiers.

✓ Alternating Current
 \Rightarrow 1 Voltage and Current Reverses periodically.



✓ Direct Current
 \Rightarrow Voltage and Current remains Constant

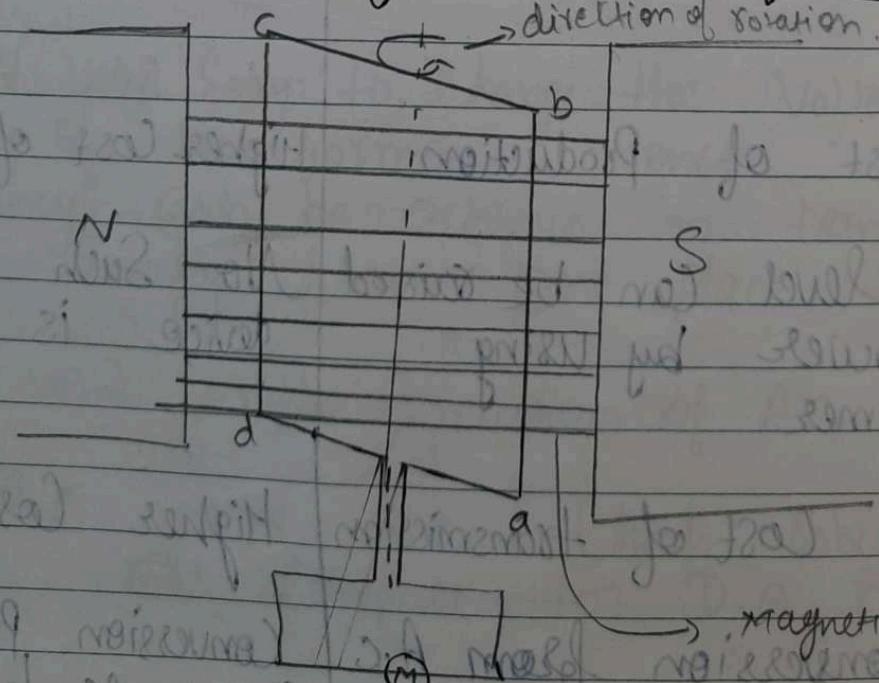


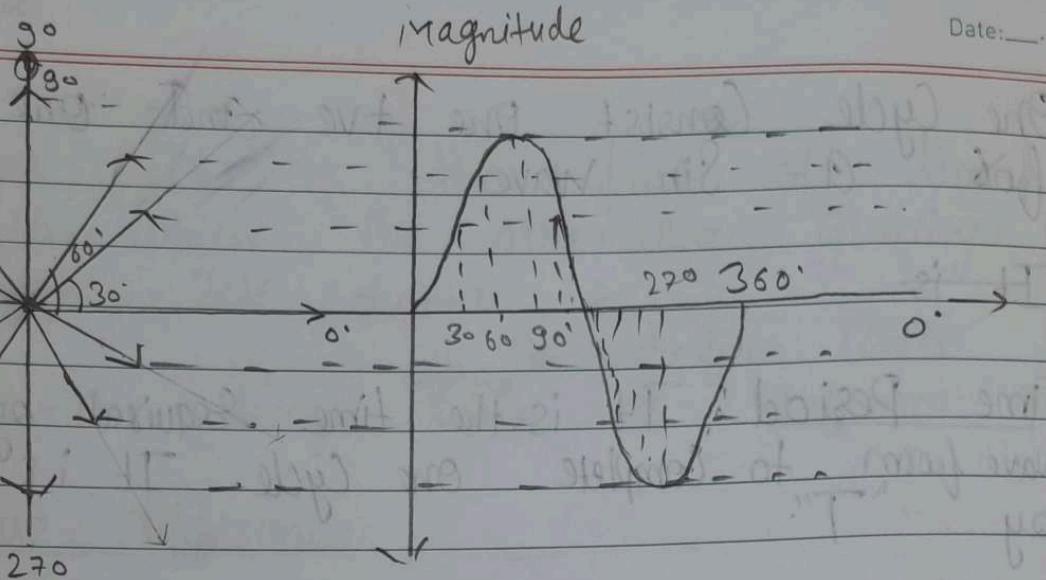
generation
form
ulater

2 \Rightarrow Low Cost of Production	Higher Cost of Production
3 \Rightarrow Voltage level can be raised \Rightarrow Or lower by using Transformer	No Such Equivalent device is available
4. Lower Cost of transmission	Higher Cost of transmission
5. Easy conversion from A.C to D.C by using Rectifiers.	Conversion possible from D.C to A.C by using Converters

6. A.C. Motors are simple, robust, almost maintenance free
- D.C. Motors require regular maintenance and therefore are less durable.
7. A.C. Cannot be used in certain Applications like Electroplating, Electrolyzing, etc.
- D.C. is used directly for carrying such operations.
8. In Case a person comes in contact with A.C Supply, It has a tendency to attract Hence the person will get Electric Shock.
- In Case a person comes in contact with D.C Supply It gives repelling shock Hence it is somewhat less dangerous.
9. Frequency of A.C. is 50 Hz
- Frequency of D.C. is 0

\Rightarrow Basic Principle of Generation of A.C.





15/11/2021

Terms Related to Sinosoidal :

Instantaneous Fv Value: It is the quantity (Voltage or Current) which changes with time "t". It has different value at every instant of time. These quantities are represent by small case letters "V or i"

$$V = V_m \sin\theta$$

$$i = I_m \sin\theta$$

Peak Value: It is the maximum value of Voltage or Current of the Sinusoidal waveform whose value is maximum at $\theta = 90^\circ$. V_m and I_m are the Peak values of Voltage and Current respectively.

Cycle: The Shape of Sin Wave repeat itself after 360° . One repetition of the wave form is termed as Cycle.

One Cycle Consist One +ve and one -ve Set
for a Sin Wave

It is

Time Period: It is the time required by the wave form to complete one cycle. It is represented by "T".

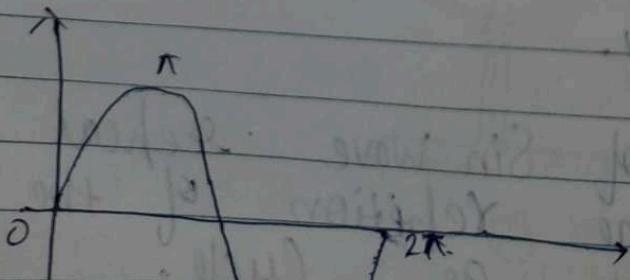
Frequency: It is defined as no. of repetition of wave form or no. of cycles per second. It is represented by "f".

$$f = \frac{1}{T}$$

Angular Velocity: We observed that each cycle spans 2π radians. If it is divided by the time period, angular velocity of the sin function.

It is represented by " ω ".
Its unit is Radian / sec.

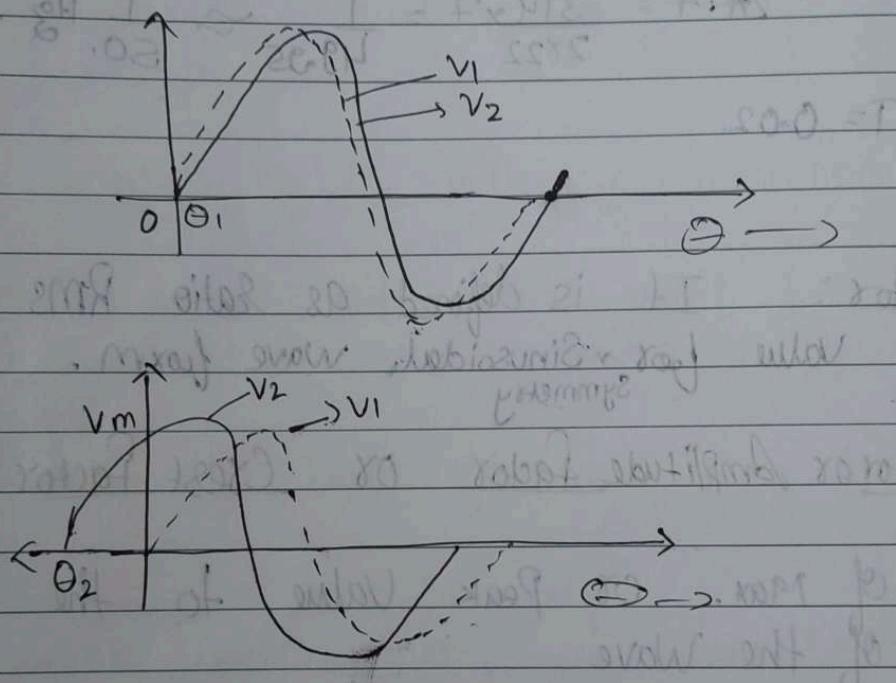
$$\text{Angular Velocity} = \frac{\text{Angle turned}}{\text{Time period}} = \frac{2\pi}{T} = \frac{2\pi f \text{ rad}}{\text{sec}}$$



Phase: It is the part of time period after which the alternating quantity passed through zero position.

The waveforms which start at zero are always referred to as reference quantity.

Phase difference:



Power factor: It is defined as the cosine of the angle between Voltage and Current of the same circuit.

It is also defined as ratio of active power to the apparent power.

$$\cos \phi = \frac{\text{Active power}}{\text{Apparent power}}$$

Q For an Instantaneous Value of Current $I = 10\sqrt{2} \sin(314t)$
 Cal. Peak value. Freq. Time Period,
 Average value.

Soln

$$I_0 = 10\sqrt{2} \sin(314t)$$

$$\text{Peak value} = 10\sqrt{2}$$

$$\text{Angular Velocity} = 314 \text{ Rad/sec.}$$

$$\text{Freq.} = 2\pi f = 314$$

$$2\pi f = \frac{314 \times 7}{2 \times 22} = \frac{1}{49.95} \approx \frac{1}{50} \text{ Hz.}$$

$$T = 0.02$$

Form factor: It is defined as ratio RMS value to average value for Sinusoidal wave form.

Peak Factor or Amplitude factor or Crest Factor.

Ratio of Max. or Peak Value to the RMS value of the Wave

Average Value Sinosoidal waveform: The average or mean value V_{av} of an alternative voltage is expressed as that DC voltage which when applied to any circuit transfer the same charge as is transferred by the alternative quantity.

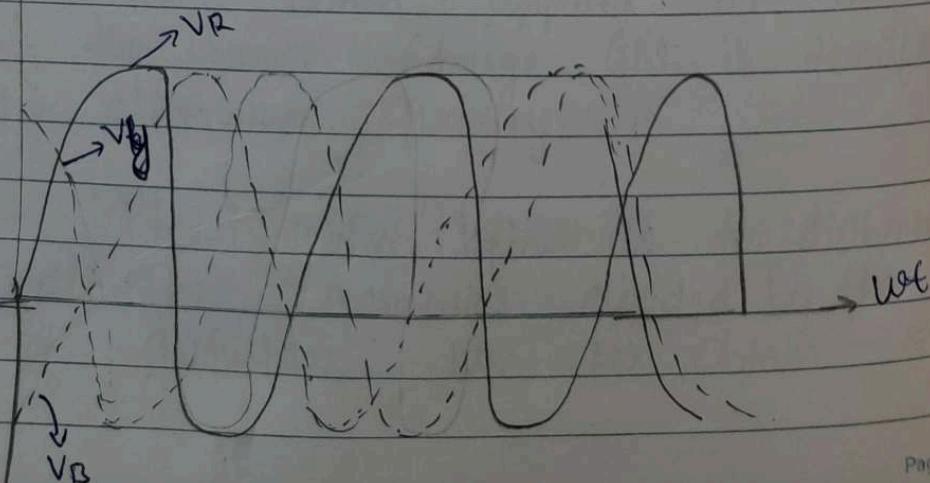
It is also defined as the arithmetic sum of all the quantities divided by the total no. of quantities used to obtain the sum.

It can also be defined as area under the curve divided by the time for which area is calculated.

Three Phase of A.c Circuit.

Advantages of Three Phase System:

- 1) The amount of conductor material needed to transfer same amount of power is lesser for three phase system. Thus it is more economical.
- 2) Domestic Power and industrial or commercial power can be provided from the same source.
- 3) Voltage regulation of three phase system is better.
- 4) As three phase induction motor are self starting while single phase motor's are not.
- 5) The torque produced by three phase motor is more.
- 6) For a given size of the ~~phase~~ frame three phase generator provide more output.

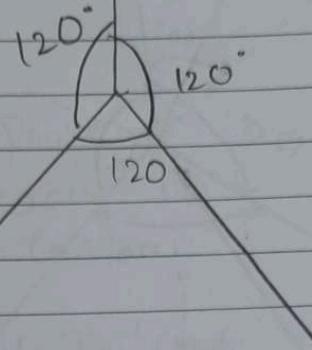


$$V_R = V_L 0^\circ \text{ volt}$$

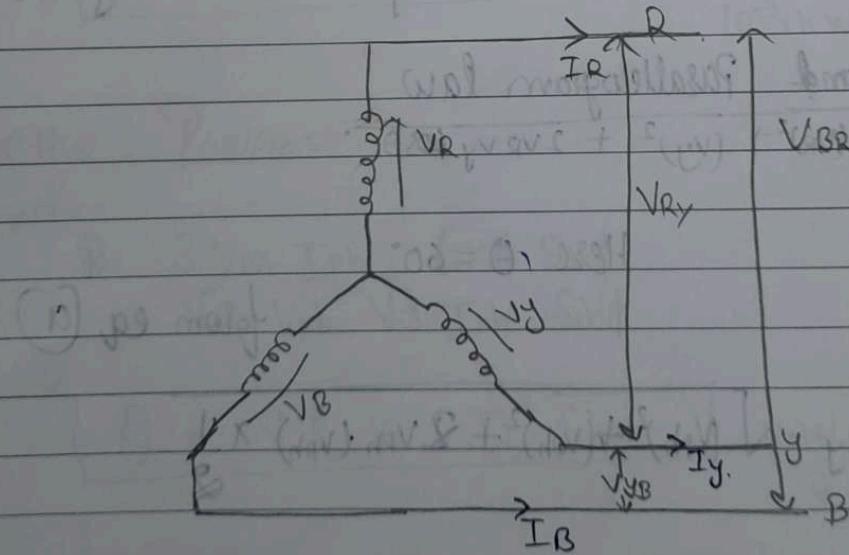
$$V_y = V_L - 120^\circ \text{ volt}$$

$$V_B = V_L + 120^\circ \text{ volt}$$

$$= V_L - 240^\circ \text{ volt.}$$



Relationship between line and phase generally
Quantity in Star Connected System.

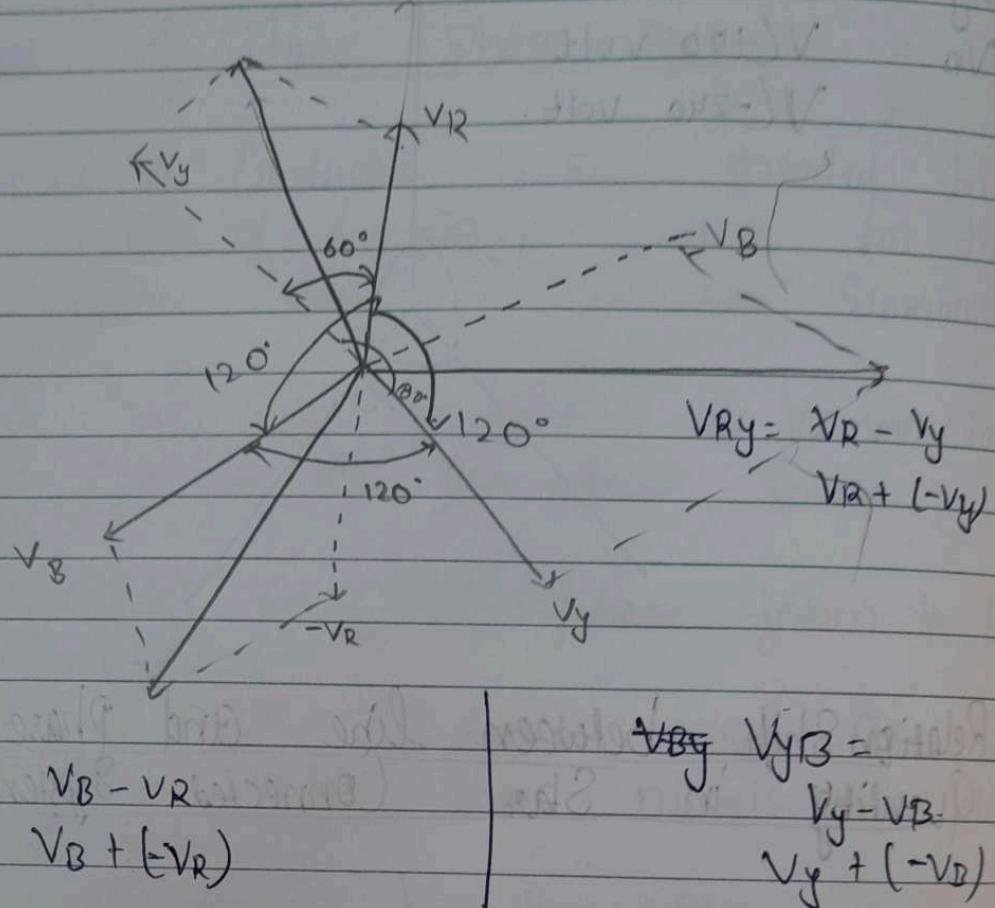


Let V_R , V_y , & V_B represent the phase voltages while line voltages are given by V_{RY} , V_{YB} , and V_{BR} .

$$V_R = V_y = V_B = V_{ph} \rightarrow \text{eq(a)}$$

$$V_{RY} = V_{YB} = V_{BR} = V_L \rightarrow \text{eq(b)}$$

Phasor diagram:



by using Resultant & parallelogram law

$$V_{Ry} = \sqrt{(V_R)^2 + (V_y)^2 + 2V_R V_y \cos\theta}$$

Here $\theta = 60^\circ$

from eq (a)

so.

$$V_{Ry} = \sqrt{V_{ph}^2 + (V_{ph})^2 + 2V_{ph}(V_{ph}) \times \frac{1}{2}}$$

$$[V_{Ry} = \sqrt{3} V_{ph}]$$

Similar as $V_{B\beta}$ and V_{BR} .

Since the line is connected in Series with it on Phase. Therefore Current remains the same.

$$[I_L = I_{Ph}] \rightarrow \text{eq(c)}$$

Line Current = Phase Current

Power Active

Total Active Power

$$P = 3V_{Ph} I_{Ph} \cos\phi$$

$$P = \underbrace{\sqrt{3} V_{Ph}}_{\text{from previous eqn's eqc}} \underbrace{\sqrt{3} I_{Ph} \cos\phi}_{\text{from previous eqn's eqc}}$$

$$P = V_L \times \sqrt{3} \times I_L \times \cos\phi$$

$$P = \sqrt{3} V_L I_L \cos\phi \quad \text{W.}$$

$$\times 10^{-3} \text{kW.}$$

Reactive Power:

$$Q = 3V_{Ph} I_{Ph} \cos\phi \sin\phi$$

$$\sqrt{3} V_{Ph} \sqrt{3} I_{Ph} \sin\phi$$

$$Q = \sqrt{3} V_L I_L \sin\theta \quad \text{Volt Ampere Reactive} \times 10^{-3} \text{kVAR.}$$

Apparent Power:

$$S = \sqrt{P^2 + Q^2}$$

$$S = 3V_{Ph} I_{Ph}$$

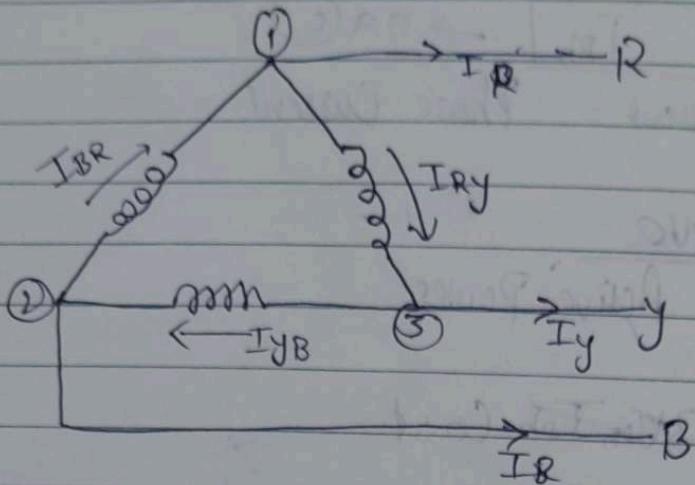
$$= \sqrt{3} V_{Ph} \sqrt{3} I_{Ph}$$

$$S = \sqrt{3} V_L I_L \quad \text{VA} \cdot \text{volt Ampere}$$

$$\times 10^{-3} \text{ volt Ampere}$$

Relationship between Line and Phase quantity in Delta Converted System

→



$I_{ph} = I_{Ry}$, I_{yB} , and I_{BR} are Phase Current

$I_L = I_R, I_B$ & I_y are line current.

at ① by using KCL.

$$I_{BR} = I_R + I_{Ry}$$

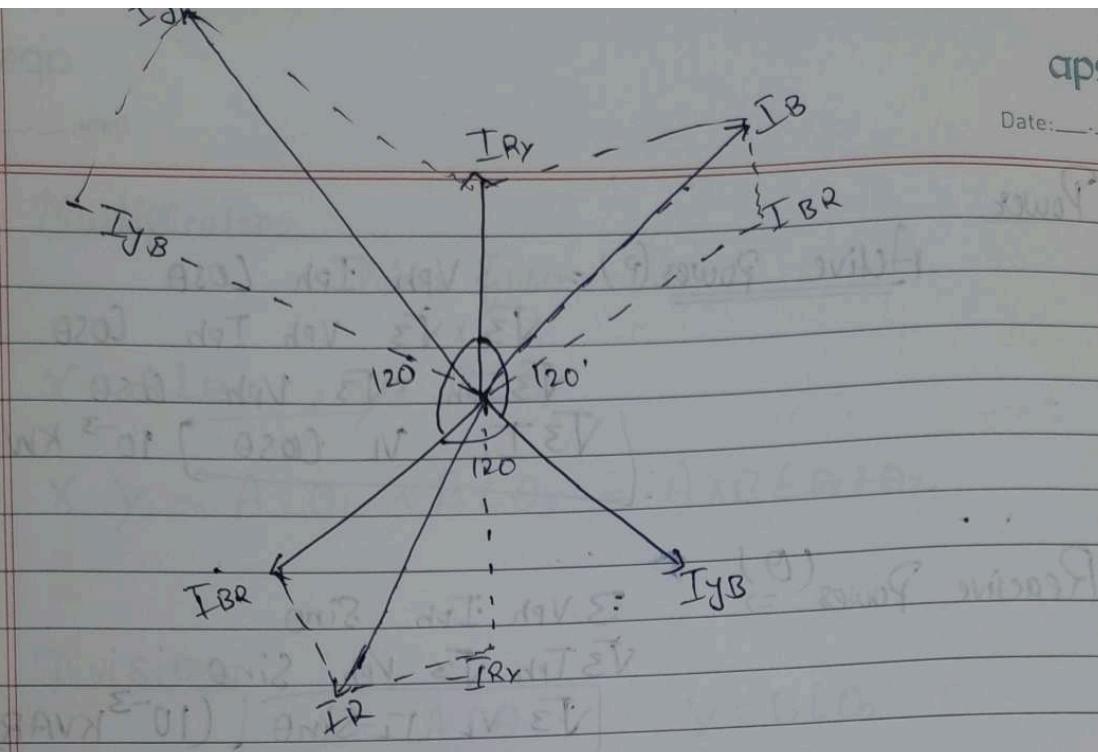
$$I_R = I_{BR} - I_{Ry} \quad \text{--- Eq. (4)}$$

at ② $I_{yB} = I_{BR} + I_B$

$$I_B = I_{yB} - I_{BR} \quad \text{--- (5)}$$

at ③ $I_{Ry} = I_{yB} + I_y$

$$I_y = I_{Ry} - I_{yB} \quad \text{--- (6)}$$



→ For eq (a)

$$I_R = I_{BR} + (-I_{RY})$$

$$\text{For eq (b)} \quad I_B = I_{YB} + (-I_{BR})$$

$$\text{For eq (c)} \quad I_Y = I_{RY} + (-I_{YB})$$

$$\text{So } I_R = \sqrt{(I_{RY})^2 + (I_{BR})^2 + 2I_{RY}I_{BR} \cos 60^\circ}$$

$$I_R = \sqrt{(I_{ph})^2 + (I_{ph})^2 + 2(I_{ph})^2 \times \frac{1}{2}}$$

$$I_R = \sqrt{3(I_{ph})^2}$$

$$I_L = \sqrt{3} I_{ph}$$

Since the neutral does not exist in Delta Connection
i.e. Therefore line voltage = Phase voltage

$$V_L = V_{ph}$$

Power

$$\text{Active Power (P)} = 3 V_{ph} I_{ph} \cos\theta$$

$$\sqrt{3} \times \sqrt{3} V_{ph} I_{ph} \cos\theta$$

$$\sqrt{3} I_{ph} \times \sqrt{3} V_{ph} \cos\theta$$

$$\boxed{\sqrt{3} I_L V_L \cos\theta} [10^{-3} \text{ kW}]$$

Reactive Power (Q)

$$3 V_{ph} I_{ph} \sin\theta$$

$$\sqrt{3} I_{ph} \sqrt{3} V_{ph} \sin\theta$$

$$\boxed{\sqrt{3} V_L I_L \sin\theta} [10^{-3} \text{ kVAR}]$$

Apparent Power (S)

$$\sqrt{3} V_{ph} I_{ph}$$

$$\boxed{\sqrt{3} \cancel{V_{ph} I_L}} [10^{-3} \text{ kVA}]$$

$$(\cancel{V_{ph} I_L} + \sqrt{3} V_L I_L)$$

30/11/2021

Addition:

Rectangular.

$$X = A + iB, \quad Y = C + iD$$

$$X+Y = A + iB + C + iD$$

$$(A+C) + i(B+D)$$

Subtraction:

$$X = A + iB$$

$$Y = C + iD$$

$$X-Y = (A+iB) - (C+iD) =$$

$$(A-C) + i(B-D)$$

Multiplication

Polar form

$$x = A \angle \theta_1, y = B \angle \theta_2$$

$$x - y = A \angle \theta_1 \times B \angle \theta_2 = AB \angle \theta_1 + \theta_2$$

Division

$$x = A \angle \theta_1, y = B \angle \theta_2$$

$$\frac{x}{y} = \frac{A \angle \theta_1}{B \angle \theta_2} = \frac{A}{B} \angle \theta_1 - \theta_2$$

Q. $x = 3+i5 \rightarrow$ Rectangular.
 $y = 8+i3$

① + $x+y = 3+i5 + 8+i3$
 $= 3+8 + i(5+3)$
 $= 11+8i$

② - $x-y = 3+i5 - 8+i3$
 $= (3-5) + i(5-3)$
 $= -2 - 4i$

③ (X) Multiplication

on Converting into Polar

$$A = (3, 5) \Rightarrow r = \sqrt{3^2 + 5^2} = \sqrt{34} \approx 5.83, \theta = \tan^{-1}(5/3) \approx 59.03^\circ$$

$$B = (8, 3) \Rightarrow r = \sqrt{8^2 + 3^2} = \sqrt{65} \approx 12.041, \theta = \tan^{-1}(3/8) \approx 48.36^\circ$$

Now

$$X = 5.83 / 59.03 \rightarrow A$$

$$Y = 12.041 / 48.36 \rightarrow B$$

$$X * Y = A * B \Rightarrow 5.83 \times 12.041 [59.03 + 48.36] \\ 70.199 / 107.39$$

Division

$$X = 5.83 / 59.03$$

$$Y = 12.041 / 48.36$$

$$X / Y = 0.4841 / 10.67$$

- Q. A Star Connected load has impedance of $(3+iy)$ and is connected across a balanced three phase Delta connected alternator having a line voltage of 120 Volt. Obtain the phase current and the line current.

Solutions

In Star Connection

$$I_{ph} = I_L$$

$$V_L = \sqrt{3} V_{ph}$$

$$Z_{ph} = (3+iy)$$

$$I_{ph} = \frac{V_{ph}}{Z_{ph}} = \frac{V_L / \sqrt{3}}{Z_{ph}}$$

$$I_{Ry} = \frac{120 \angle 0^\circ}{\sqrt{3}(3+iy)}$$

$$I_{YB} = \frac{120 \angle -120^\circ}{\sqrt{3} \times (3+iy)}$$

$$I_{BR} = \frac{120 L_{240}}{\sqrt{3}(3+i4)}$$

$$I_{RY} = \frac{120 L_0}{3\sqrt{3} + i4\sqrt{3}}$$

$$I_{RY} = \frac{120 L_0}{8.66 L 53.13}$$

$$I_{RY} = 13.85 L - 53.13$$

$$I_{yB} = \frac{120^\circ L - 120}{(3\sqrt{3} + i4\sqrt{3})}$$

$$I_{yB} = \frac{120^\circ L - 120}{8.66 L 53.13}$$

$$13.85 L - 173.13$$

$$I_{BR} = \frac{13.85 L}{8.66 L} 120^\circ L - 240$$

$$I_{BR} = 13.85 L - 293.13$$

- Q. A Three Phase balanced system Supplies 110 volt to a Delta Connected load whose phase impedance's are equal to $(3.54 + i354)$ determine the line Current and draw the phasor Diagram.

Soh

$$V_{ph} \cdot Z_{ph} = 3.54 + i 3.54$$

$$V = 110 \text{ volt}$$

For delta $V_2 = V_{ph}$

$$\& [I_L = \sqrt{3} I_{ph}]$$

$$I_{Ry} = \frac{V_{ph}}{Z_{ph}} = \frac{110 L 0^\circ}{3.54 + i 3.54} = 110 L 0^\circ - 5.00 L 45^\circ$$

$$I_{RB} = \frac{110 L - 120^\circ}{3.54 + i 3.54} = \frac{110 L - 120^\circ}{5.00 L 45^\circ} = 22 L - 165^\circ$$

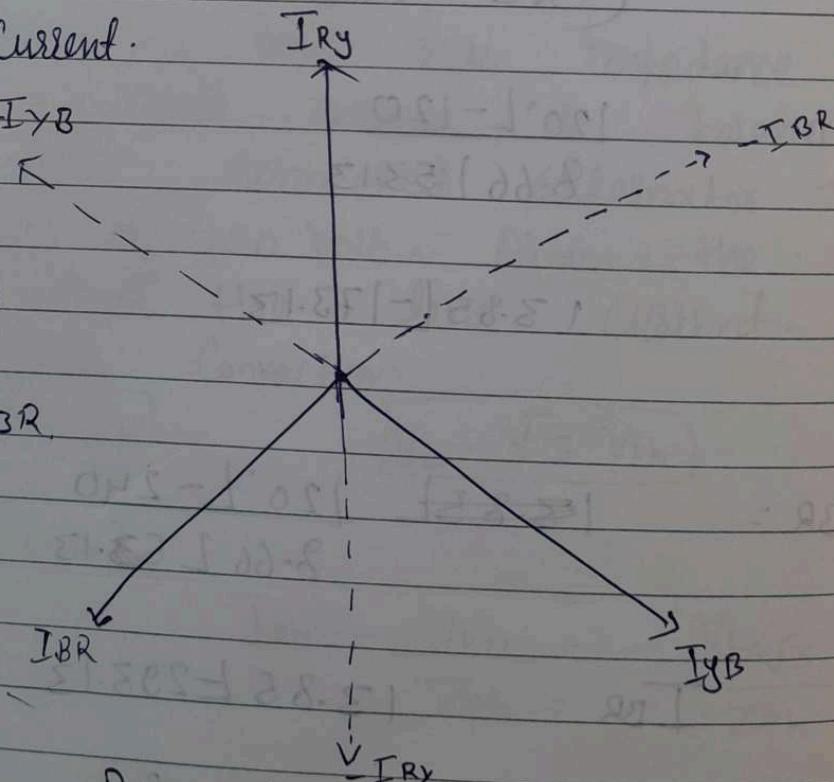
$$I_{BR} = \frac{110 L - 240^\circ}{3.54 + i 3.54} = \frac{110 L - 240^\circ}{5.00 L 45^\circ} = 22 L - 285^\circ$$

by Calculating line Current.

$$\Rightarrow I_R = I_{BR} - I_{Ry}$$

$$I_{Ry} = I_{Ry} - I_{yB}$$

$$I_B = I_{yB} - I_{BR}$$



By Converting Polar into rectangular

$$I_{BR} = 15 - 15i$$

$$I_{yB} = 21 - 5i$$

$$I_B = 5 + 21i$$

$$I_R = \frac{-21 - 5i - 15 + 15i}{-17 - 36 + 10i}$$

$$I_R = -15.55 + 15.55i = -21.25 - 5.69i$$

$$\underline{I_R} = I_{BR} - I_{yB}$$

Now

$$I_{RY} = 22L - 45^\circ$$

$$\text{on converting into rec.} \Rightarrow x = 15.55 - 15.55i$$

$$I_{yB} = 22L - 285^\circ$$

$$= x = -21.25$$

$$y = -5.69$$

$$\text{So } -21.25 - 5.69i$$

$$\text{and } I_{BR} = 22L - 285^\circ$$

so

$$5.69 + 21.25i$$

Therefore

$$I_R = I_{BR} - I_{RY}$$

$$5.69 + 21.25i - 15.55 + 15.55i$$

$$I_R = -9.86 + 36.8i$$

$$\boxed{I_R = -9.86 + 36.8i}$$

$$I_y = \underline{I_{RY} - I_{yB}}$$

$$I_{RY} = 15.55 - 15.55i$$

$$I_{yB} = -21.25 - 5.69i$$

$$I_y = 15.55 - 15.55i - (-21.25 - 5.69i)$$

$$15.55 - 15.55i + 21.25 + 5.69i$$

$$\boxed{I_y = 36.74 - 9.83i}$$

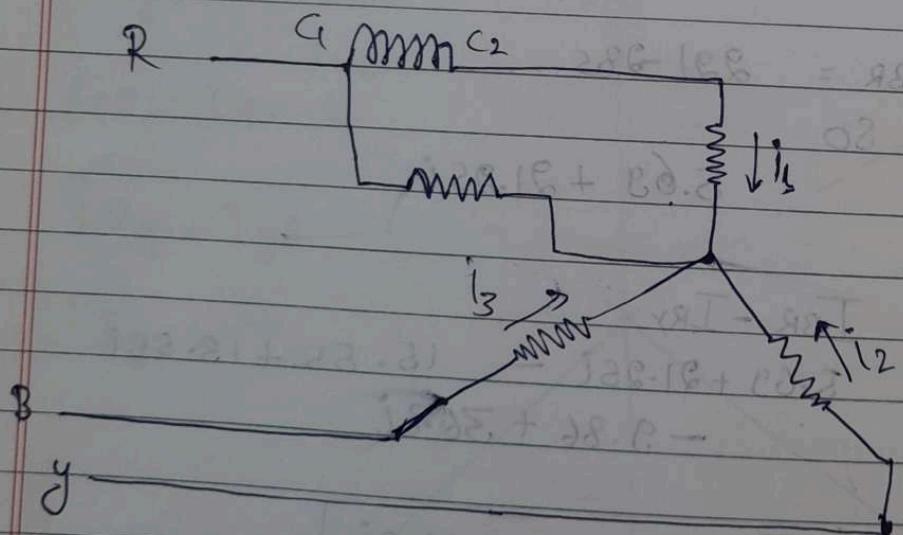
$$I_B = I_{yB} - I_{BR}$$

$$I_{yB} = 22L-16S - 22L-28S \\ = (-21.25 - 5.69i) - (5.69 + 21.25i)$$

$$I_B = -21.25 - 5.69 - 5.69 - 21.25i$$

→ Measurement of Power

(1) One Wattmeter Method

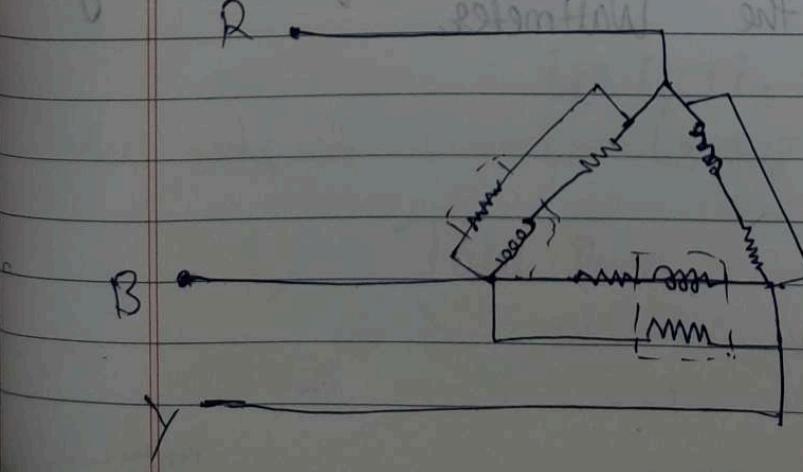
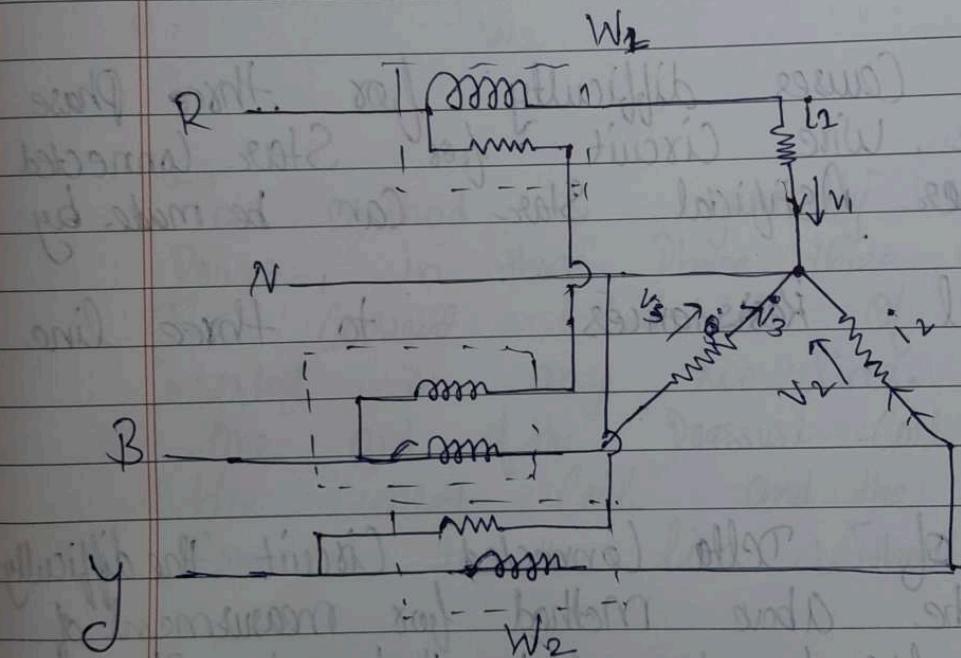


In balanced Three Wire Three Phase load Circuits the Power in Each Phase is Equal. Therefore The total Power of the Circuit can be determined by multiplying the Power measured in any one phase by three.

Total Power of 3 Phase = $3 \times$ Power Measured by one Wattmeter.

Demerit: One wattmeter method has a demerit that Even a slight difference of unbalance in the load Produces a large Error in the measurement.

Three Wattmeter Method:



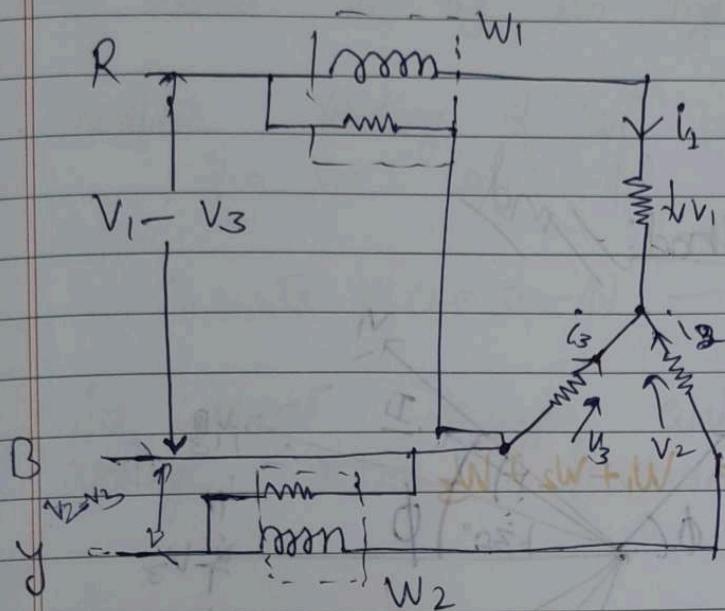
The Three Wattmeter Method is used for the measurement of power in three phase four wire circuit. In this method the neutral wire is common to three phases. Each wattmeter sense reads power in its own phase and the total power of the load circuit is given by the sum of the readings of three wattmeters w_1 , w_2 and w_3 .

$$\text{Total Power } P = w_1 + w_2 + w_3$$

Demerit: It causes difficulty for three phase three wire circuit for star connected load. However artificial star can be made by connecting three equal resistances to three line conductors.

In case of delta connected circuit the difficulty in adopting the above method for measurement of power is due to the fact that the phase coils are required to be broken for inserting current coil of the wattmeter.

Two Wattmeter Method



This method is generally used for measurement of Power in three phase three wire load circuit. The Current Coil of two Wattmeter are inserted in any two lines.

One end of the Pressure Coil is connected to the Current Coil and the other End is connected to the line without a current coil

Apply KCL at point P'

$$i_1 + i_2 + i_3 = 0$$

$$i_3 = -(i_1 + i_2)$$

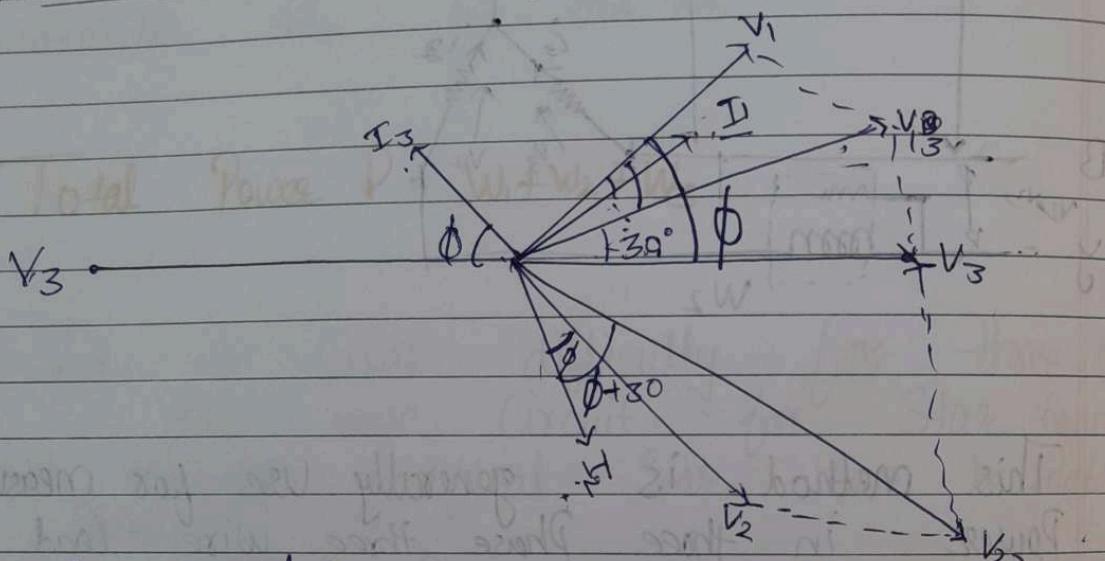
$$\begin{aligned} \text{Total Power} &= V_1 i_1 + V_2 i_2 + V_3 i_3 \\ &= V_1 i_1 + V_2 i_2 + V_3 (-i_1 - i_2) \\ &= V_1 i_1 + V_2 i_2 - V_3 i_1 - V_3 i_2 \end{aligned}$$

$$= (V_1 - V_3) i_1 + (V_2 - V_3) i_2$$

$$P = W_1 + W_2$$

$$P = P_1 + P_2$$

Two Wattmeter Method:



As load is balanced therefore phase voltages $V_1 = V_2 = V_3 = V$
 $V_3 = V$ and Line voltages $V_{12} = V_{23} = V_{31} = \sqrt{3} V$

Phase Current = $I_1 = I_2 = I$
 and

Line Current

$$I_1 = I_2 = I_3 = I$$

Power factor = $\cos\phi$

The phase current lag corresponding the phase voltage ϕ

⇒ The Current through Voltmeter
 $P_1 = I_1 \times$ voltage across it is passive

Coil (0) is $V_{13} - [(\phi - 30^\circ)] IV \text{ ev} = 8.9$

$\Rightarrow I$ leads V_{13} by an angle

Therefore reading of "W₁" Wattmeter

$$P_1 = V_{13} I \cos(30 - \phi)$$

$$V_1 = \sqrt{3} VI \cos(30 - \phi) \quad \text{--- (1)}$$

The current through wattmeter W₂ is I₂ and voltage across pressure coil is V₂₃

I₂ leads V₂₃ by an angle $(30 + \phi)$ Therefore Reading of wattmeter W₂ is

$$P_2 = V_{23} I_2 \cos(30 + \phi)$$

$$P_2 = V_{23} I_2 \cos(30 + \phi)$$

$$P_2 = \cancel{\sqrt{3} VI} \sqrt{3} VI \cos(30 + \phi) \quad \text{--- (2)}$$

$$P_1 + P_2 = \sqrt{3} VI \cos(30 - \phi) + \sqrt{3} VI \cos(30 + \phi)$$

$$\sqrt{3} VI [\cos(30 - \phi) + \cos(30 + \phi)]$$

$$\sqrt{3} VI \cdot 2 \cos \left[\frac{30 - \phi + 30 + \phi}{2} \right] \cos \left[\frac{30 + \phi - 30 - \phi}{2} \right]$$

$$2\sqrt{3} VI \cos 30 \cos \phi$$

$$2\sqrt{3} VI \frac{\sqrt{3}}{2} \times \cos \phi$$

$$P_1 + P_2 = 3VI \cos \phi \quad \text{eq (1)}$$

$$P_1 - P_2 = \sqrt{3} VI [\cos(30 - \phi)] - \cos(30 + \phi)$$

$$2\sqrt{3} VI \left[\sin\left(\frac{30 - \phi + 30 + \phi}{2}\right) - \sin\left(\frac{30 - \phi - 30 - \phi}{2}\right) \right]$$

$$2\sqrt{3} VI \sin 30 \sin \phi$$

$$P_1 - P_2 = \boxed{\sqrt{3} VI \sin \phi} - eq(2)$$

\Rightarrow Divide eq(2) & eq 1

$$\frac{\sqrt{3} VI \sin \phi}{3 VI \cos \phi} = \frac{P_1 - P_2}{P_1 + P_2}$$

$$\tan \phi = \sqrt{3} \left[\frac{P_1 - P_2}{P_1 + P_2} \right]$$

$$\phi = \tan^{-1} \left[\sqrt{3} \left[\frac{P_1 - P_2}{P_1 + P_2} \right] \right]$$

Power factor $\cos \phi$

$$\cos \left[\tan^{-1} \left[\sqrt{3} \left[\frac{P_1 - P_2}{P_1 + P_2} \right] \right] \right]$$

Effect of Power factor on reading of watt meter

① When Power factor is Unity

$$\cos \phi = 1 \quad \& \quad \phi = 0$$

$$P_1 = \frac{3}{2} \cos VI$$

$$P_2 = \frac{3}{2} VI$$

$$\text{Total Power} = P_1 + P_2 = 3VI \cos\phi$$

When Power factor is 0.5

$$\phi = 60^\circ$$

$$\text{then } P_1 = \frac{3}{2} VI \cos 60^\circ = \frac{3}{2} VI \cdot \frac{1}{2} = \frac{3}{4} VI$$

$$P_2 = 0$$

Total power $P_1 + P_2$ is $\frac{3}{4} VI$

$$\frac{3}{2} VI \cos 60^\circ$$

③ When P.f. is 0

$$\text{then } \phi = 90^\circ$$

$$P_1 = \sqrt{3} VI \cos(30^\circ - 90^\circ)$$

$$\sqrt{3} VI \cdot \frac{1}{2}$$

$$\frac{\sqrt{3}}{2} VI$$

$$P_1 + P_2 = 0$$

A Three phase balanced load power was measured by two Wattmeter method.

- Q The reading of two Wattmeter is so connected are 5kW and 0.5kW. The latter later reading being obtained after reversal of current coil connection. Calculate the power factor of the total load.

$$P_1 = 5 \text{ kW}$$
$$P_2 = -0.5 \text{ kW}$$

$$\phi_1 = \tan^{-1} \sqrt{3} \left[\frac{5+0.5}{5-0.5} \right]$$

$$\phi = \tan^{-1} \left[\sqrt{3} \times \frac{5.05}{4.5} \right]$$

$$\tan^{-1} \left[\sqrt{3} \times 1.12 \right]$$

$$\tan^{-1} [1.943]$$

$$= 62.76$$

Power factor will be

$$\cos\phi = 0.4577 \dots$$

Transformer: A transformer is an AC static device which transfers electric power from one circuit to another without changing its frequency. Hence the main function of transformer is to raise or lower voltage in a circuit with a corresponding decrease or increase in current at the same frequency.

Any transformer has two coils electrically insulated from each other and wound on a common core that is magnetically coupled. The energy from the coil is transformed

The coil which receives energy from an A.C. source k/a Primary (P) and the coil which delivers the energy to the node is called Secondary (S)

If the primary coils has smaller number of turns of a thick wire. While the secondary coil has large no. of turns of thin wire then that is called Step-up transformer.

Similarly in Step-down transformer the primary (P) consists of large no. of turns of thin wire while the secondary has smaller no. of turns of thick wire

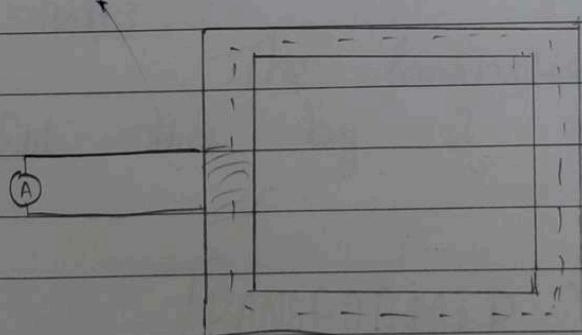
Transformer operate on the principle of mutual Induction.

Energy induction can be efficiently transferred by induction from one set of a coil to another by means of a varying magnetic flux provided that both sets of coils are on a common magnetic circuit.

According to "Faraday law" of Electromagnetic Induction, The rate of change of flux is directly proportional to Induced Emf.

"Lenz" law give the direction of Induced Emf to be the opposite of the cause producing it.

$$e = -N \frac{d\phi}{dt}$$



OPERATION

When an alternative current is applied to the primary, an alternative current set up. As the winding is linked with the magnetic core, it produces a alternating flux in the core.

This alternating flux is linked with the turns of the secondary coil, since the flux is alternating in nature, it induces the mutually induced "Emf" in secondary of the same frequency.

Then according to Faraday law of electro magnetic induction an Emf is induced in Secondary coil. Due to this induced Emf the secondary coil is capable of supplying current and enhance the load.

- The main Elements of Construction's are
- (1) Magnetic Circuit. Comprising. limbs , yoke . Clamping Structure.
 - (2) Electric Circuit. Comprising Primary & Secondary Winding , former's , Insulation devices
 - (3) Terminals Comprising tapping and tapping Switches, terminal bushings and leads.
 - (4) Tank Comprising of Oil and Cooling apparatus, conservator , Breather , And auxiliary apparatus Such as Oil gauge , temperature gauge and bulb

TRANSFORMER CORE

In all type of transformer , Core is constructed of the Sheets , Steel , lamination, assembled to provide a continuous magnetic path with a min. of air gap. The thickness of Lamination varies from 0.35 mm for a freq. of 50 Hz to 0.55 mm for a frequency of 25 Hertz .

The laminations are insulated from each other by a thin coating of varnish.

TRANSFORMER WINDING

A transformer assembly consist of two Windings , The Windings are made up of high conductivity copper wire of suitable cross sectional area. Each winding is split up into two equal number of coils & wrapped and are

on both limbs of the core.

By dividing the winding in two half there is reduction in leakage flux. By wrapping high voltage winding on low voltage winding the amount of high voltage insulation is minimized.

TERMINALS AND LEADS

The connection to the winding are of insulated copper bars. They are brought through the tank by means of bushing.

TANK

A suitable container for the assembled core and winding is the transformer tank. Insulating medium is oil which is generally 16/18 transformer oil. The tank has ~~#~~ a No. of radiators tubes or fins which increases the area for heat dissipation.

TEMPERATURE GAUGE

This gives the temperature of the hot oil where as level of oil is indicated by oil gauge situated in the conservator.

- 1) The function of valve one is for taking out transformer oil during maintenance.

to check the determination of oil

→ Valve (1) & valve (2) are connected together to the centrifugal machine for removing the moisture content from the oil even while the transformer is ON.

BUCHHOLZ Relate is a protective device which is gas actuated Relay

When (+) Some minor volt is developed this relay senses the fault and a alarm is given to the operator. In case of major fault this relay will trip the transformer.

Conservative & Breather

The oil of the transformer should not come in contact with atmospheric air as it may take a moisture which may spoil its insulating property. Also air may cause acidity and sludging of oil. To prevent this the transformer is provided with conservator which take a contraction and expansion of oil without allowing it to work come in contact with air.

EMF Equation

15/12/2021

Date: _____

$$\text{Induced EMF} \Rightarrow e = -N \frac{d\phi}{dt}$$

$e \rightarrow$ instantaneous value of Emf induced.

$\phi \rightarrow$ instantaneous flux of mutual flux

$N \rightarrow$ Number of turns in coil.

Let N_1 & N_2 be the Number of turns of primary or Secondary.

$$e_i = -N \frac{d\phi}{dt} = -N_1 \frac{d}{dt} (\Phi_m \sin \omega t)$$

$$= -N_1 \frac{d}{dt} (\Phi_m \sin 2\pi f t)$$

$$= -N_1 \Phi_m 2\pi f \cos 2\pi f t$$

$$= -N_1 \Phi_m 2\pi f \sin(2\pi f t - \frac{\pi}{2}) \text{ Radian}$$

$$\text{Now } E_{\text{max}} = N_1 \Phi_m 2\pi f \text{ volt}$$

$$E_{\text{rms}} = \frac{E_{\text{max}}}{\sqrt{2}} = E_i = \frac{2\pi f N_1 \Phi_m}{\sqrt{2}}$$

$$E_i = 4.44 \Phi_m N_1 f \text{ Volts}$$

$$E_2 = 4.44 \Phi_m N_2 f \text{ Volts}$$

Transformer Ratio

$$\underline{E_1} = 4.44 \Phi_m f N_1$$

$$\underline{E_2} = 4.44 \Phi_m f N_2$$

$$\frac{E_1}{E_2} = \frac{N_1}{N_2} = a$$

Ideal transformer

Initial VA = Output VA

$$V_1 I_1 = V_2 I_2$$

08

$$\frac{V_1}{V_2} = \frac{I_2}{I_1} = \frac{1}{a}$$

Efficiency: The efficiency of a transformer at a particular load and power factor is defined as the ratio of output to the input (The two being measured in the same unit) Either watt or Kilowatt)

Efficiency $\eta = \frac{\text{Output}}{\text{Input}}$

$$= \frac{\text{Output}}{\text{Output} + \text{loss}} = \frac{\text{Output}}{\text{Output} + \text{Iron loss} + \text{Copper loss}}$$

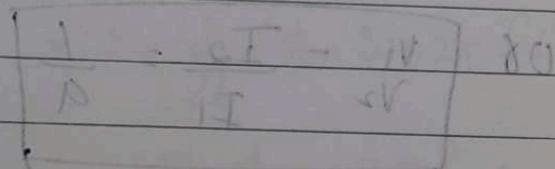
$$= \frac{V_2 I_2 \cos \phi}{(V_2 + E_2 \cos \phi) + W_i + W_w}$$

Here, $V_2 I_2$ is the Volt amperes of transformer
When it is given KVA.

$$\eta = \frac{(KVA \text{ rating} \times 1000) \cos\phi}{(KVA \text{ rating} \times 1000 \times \cos\phi) + w_i + w_w}$$

$$\eta_f = \frac{KVA \times 1000 \times \cos\phi \times n}{(KVA \times 1000 \times \cos\phi \times n) + w_i (n^2 w_w)}$$

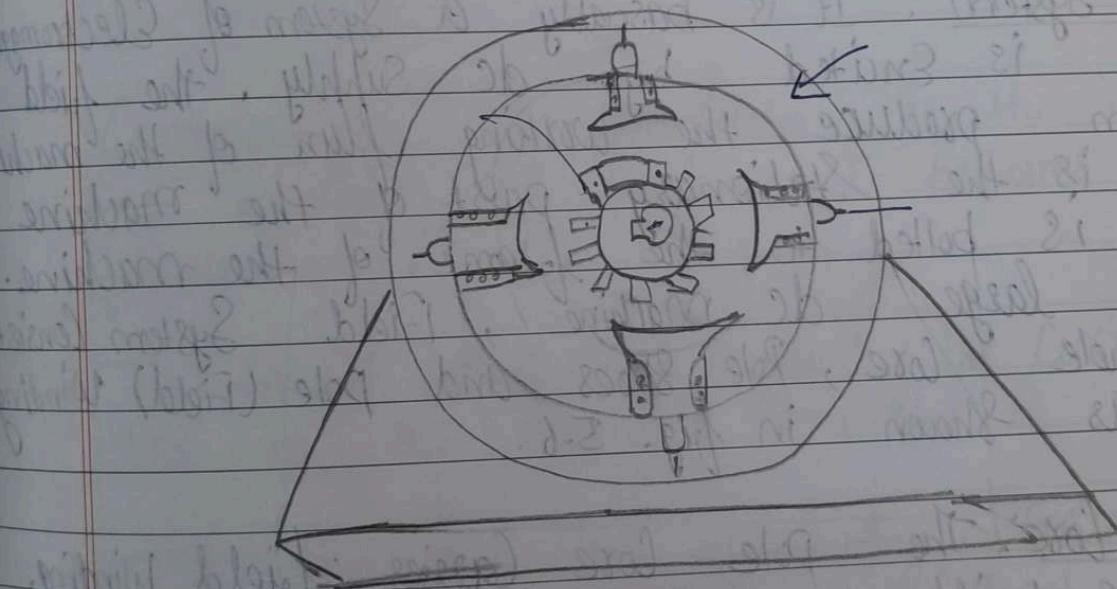
Where $n = \frac{\text{given load}}{\text{full load}}$



Conductors from the direction of induced Emf in a Flemming Left hand Rule. This

and if fore finger point in the dirⁿ of flux, middle finger in the dirⁿ of current then thumb will be point the direction of force

Construction of DC. Machine



View of DC Machine.

A dc machine consist of the following parts

- 1) Yoke or Frame
- 3) Armature
- 5) Brushes

- 2) Field System
- 4) Commutator
- 6) Bearings

Yoke: It is the outer frame of the machine. It serves the following purposes

- It acts as protective cover for the machine.
- It houses field system and supports the armature through bearings.
- It carries the working flux.

The material of yoke should have high permeability and high mechanical strength. Generally yoke is made of cast steel.

Field System: It is basically a system of electromagnets which is excited by dc supply. The field system produces the working flux of the machine. It is the stationary part of the machine and is bolted to the frame of the machine. For large dc machine, field system consists of pole core, pole shoes and pole (field) winding as shown in fig. 5-6.

(a) Pole Core: The pole core carries field winding. It is built using thin steel laminations one end of the pole core is bolted to the frame and other end has pole shoe.

(b) Pole Shoes: The pole shoe is projected part of the pole core. It has large cross-sectional area. It serves following purposes

i) It spreads the flux uniformly in the air gap and offers low reluctance path to the flux.

Field Coils: Field Coils are made of Copper wire or copper strip. They are former wound and inserted around the pole core. When field windings are excited by DC supply, they become Electromagnets and produce the working flux.

Armature: Armature is a system of conductor or coil which is free to rotate on the supported bearings. EMF's and torques are developed in the armature coils. The armature consists of the following parts.

Commutator: The commutator is the important part of the DC machine. It performs the following functions.

- To collect (or to allow) the current from (or to) the armature conductor.
- To convert the alternating current of the armature into Unidirectional current in the External circuits with the help of brushes and Vice-versa.

Brushes: The function of brushes is to collect current from moving Commutator. They are usually made of Carbon or graphite. They are housed in brush holds and are in contact with Commutator surface with the help of Shoeing pressure.

Bearings: The function of bearings is to support the machine shaft with minimum friction. For dc machines, generally ball bearing or roller bearing are used.