

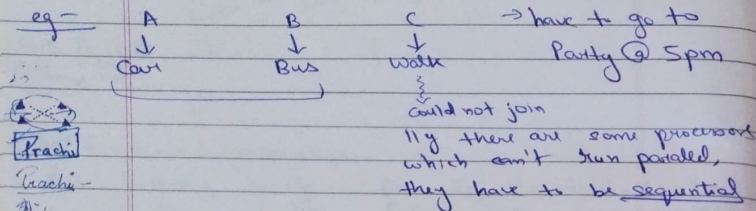
03/04/23

Unit-4 → Performance laws

Amdahl's Law

It is a law governing the speed-up by using parallel processors on a problem,
 vs

using only one serial processor, under the assumption that the problem size remains the same when parallelized



$$\text{Speedup} = \frac{T(1)}{T(n)}$$

= Time taken to execute the program using single processor (sequential)

Time taken to execute the prog using n no. of processors.

eg-
 If $T(1) = 1 \text{ sec}$
 $n = 2$, then you take = 0.5 sec

$$S = \frac{T(1)}{T(n)} = \frac{1}{0.5} = 2 \quad (\text{speedup increases by 2 times})$$

Characterizations

① It is based on fixed problem size
 (But ideally, if no. of processors ↑, we ↑ the work load - problem size) For maintaining efficiency of the system

* Amdahl's law tells that for a given problem size the speed up doesn't ↑ linearly as the no. of processors.
 The speedup tends to become saturated - doesn't ↑ after a point.

* It states that a small portion of the prog, which cannot be parallelized (serial part) will limit the overall speedup.

* Computation problem = serial part + Parallel part

Let 'f' be the fraction of operations in a computer that must be performed sequentially where $0 \leq f \leq 1$. The max. speedup achievable by a parallel computer with n processors is :-

Learn

$$S(n) \leq \frac{1}{f + \frac{(1-f)}{n}}$$

Serial part $\rightarrow f$
 Parallel part $\rightarrow \frac{(1-f)}{n}$

$$\rightarrow \frac{n}{1 + (n-1)f}$$

Ques 70% of a program's execution time occurs inside a loop that can be executed in parallel and rest 30% in serial. What is the max speedup we should expect from a parallel version of the program executing on 8 CPUs.

Solⁿ

$$f = 0.3 = \text{serial part}$$

$$n = 8$$

$$S(n) \leq \frac{8}{1 + (0.3 \times 7)}$$

$$S(8) \leq 2.58$$

For 80% : 20%
speedup = 3.33

⇒ speedup ises when processors are doing parallel processing

Ques 2 Let a program have 40% of its code enhance to yield a system speedup 2.3 times faster. What is the factor of improvement of the portion enhanced?

Ans 2 40% enhanced → 2.3 times faster
(use formula of next page)

$$S = \frac{1}{(1 - 0.4) + \left(\frac{0.4}{2.3}\right)} = 1.292$$

Ques - Let a program have 40% of its code enhanced to run 2.5 times faster. What is the overall system speedup?

Zohra TTT

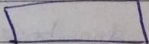
T = execution time before improvement

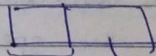
P = fraction of part benefited from improvement

06/04/24

workload is fixed in Amdahl's

let's

CPV old  1 (takes 1 cycle)

CPV new  Enhanced (fraction enhanced portion of data)

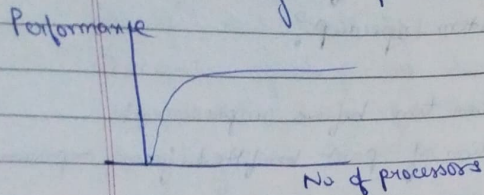
1-Enhanced (unenhanced) $\frac{F}{S}$ → at what scale it will be enhanced?
takes same time (1-F) $\frac{F}{S}$ → time taken by enhance part

#

$$S_{all} = \frac{\text{old}}{\text{new}} = \frac{1}{(1-F) + \frac{F}{S}}$$

unenhanced enhanced

Performance becomes saturated as you keep on increasing the processors. as overhead also increases.



But ideally, workload also increases as the no. of processors ↑

This was the drawback of Amdahl's bcz it kept the workload constant and only used the speedup, not dynamic workload.

Gustafson's Law

- used for scaled programs
- we are scaling for higher accuracy
- Fixed time speedup (speedup doesn't change, workload & no. of processor change)

$$T_p = t_s^* + t_p^*$$

Computational time needed for sequential part

Computational time needed for parallel part

- workload changes here

$$S = f^* + N(1 - f^*)$$

speedup no. of processors dynamic workload = f^*

Ques 1- 10% of time on a 32 processor machine is spent on one single processor. Compute the scaled speedup using Gustafson's Law.

$$f^* = 0.1 \quad N = 32 \quad S = 0.1 + 32(1 - 0.1)$$

$$S = 28.9$$

x

Sun & Lee → Nahi karva X

x

Performance Benchmarks

Benchmarking?

It is measuring how the performance of something varies as you change the parameters.

In HPC systems, things that can vary are →

- ① no. of parallel processes
- ② no. of threads
- ③ distribution of processors / threads
- ④ i/p parameters.

→ All these result in performance variations.

Benchmarking - used for scaling

- Dhrystone Benchmark
- Whetstone Benchmark

Dhrystone Benchmark

- This benchmark is used to measure and compare the performance of different computers, or the efficiency of the code generated for the same computer by different compilers.

- code gives same approx same performance irrespective of the compiler.

☆☆ - It uses no floating point operations.

Advantages ① You can compare results of processors of different architecture.

② Easy to compile & port (works on micro controller)

Disadv - from PPT

- ① uses a limited set of features.
- ② Doesn't allow you to use all the capabilities of the processor.
- ③ Strange code
- ④ The results are very dependent on compiler optimizations.

Whetstone Benchmark

- It is used for evaluating the performance of both int & floating point nos. in CPU.

Unit - 4 done

06/04/24

Unit - 5

Memory & Cache Coherency

(completely theoretical)

Consistency

needs to be maintained when sharing data.

where?

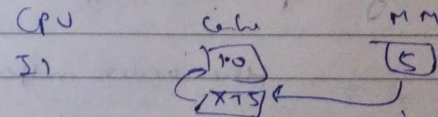
CPU	Cache	MM
	$x=10$	$x=5$

Not consistent X

Memory Consistency Model

A Consistency Model refers to the d. -

from PPT



IR → read $x=10$ \leftarrow $x=5$
C
in memory

→ next read should be from where there was last write to avoid inconsistency