

F.A.

$$a \in \Sigma^*$$

$$a \in \Sigma^*$$

* Examples :

~~Q1. Q2~~

①

$$S \rightarrow AcaB$$

$$Bc \rightarrow acB$$

$$CB \rightarrow DB$$

$$aD \rightarrow Db$$

since all the given productions $\alpha \rightarrow \beta$, satisfy the conditions.
where,

$$\alpha \in (\Sigma \cup V_n)^* \quad \beta \in (\Sigma \cup V_n)^*$$

$$\beta \in (\Sigma \cup V_n)^+$$

$$|\alpha| \leq |\beta|$$

∴ The above given grammar is of Type 1 grammar
i.e. content sensitive grammar.

It is also Type 0 grammar since i.e. Unrestricted grammar.

$$(2) \quad S \rightarrow Xa$$

$$X \rightarrow a$$

$$X \rightarrow ax$$

$$X \rightarrow abc$$

$$X \rightarrow \epsilon$$

Since all the given productions $\alpha \rightarrow \beta$, satisfy the following conditions where,

$$\alpha \in V_n \quad |A| = |B| = 1$$

$$\beta \in (\Sigma \cup V_n)^*$$

The above given grammar is of Type 2 grammar i.e. Context Free Grammar.

$$(3) \quad X \rightarrow \epsilon$$

$$X \rightarrow a \mid ay$$

$$Y \rightarrow b$$

Since all the given productions $\alpha \rightarrow \beta$, satisfy the conditions where,

$$\alpha \rightarrow \beta$$

$$\text{eg. } A \rightarrow a \mid ab$$

$$A, B \in V_n \quad |A| = |B| = 1$$

$$a \in \Sigma^*$$

The above given grammar is of Type 3 Grammar i.e. Regular grammar.

(4)

$$AB \rightarrow ABBc$$

$$A \rightarrow bc$$

$$B \rightarrow b$$

Since all the given productions are $\alpha \rightarrow \beta$, satisfying the conditions,

$$\alpha \in C^* (\Sigma \cup V_n)^*$$

$$\beta \in (\Sigma \cup V_n)^+$$

$$|\alpha| \leq |\beta|$$

$$(aabb) \rightarrow ab$$

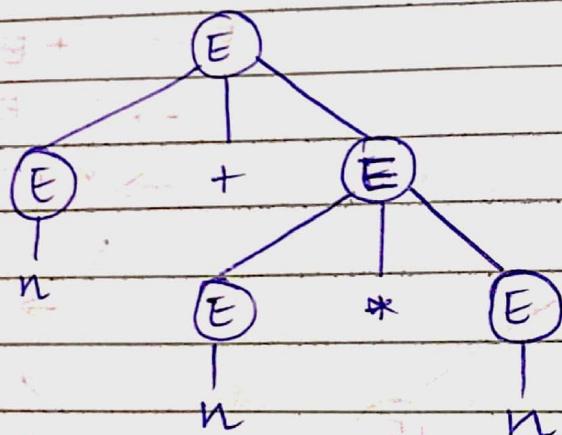
"The above given grammar is of Type 1 grammar."

It is also Type 0 grammar since unrestricted grammar

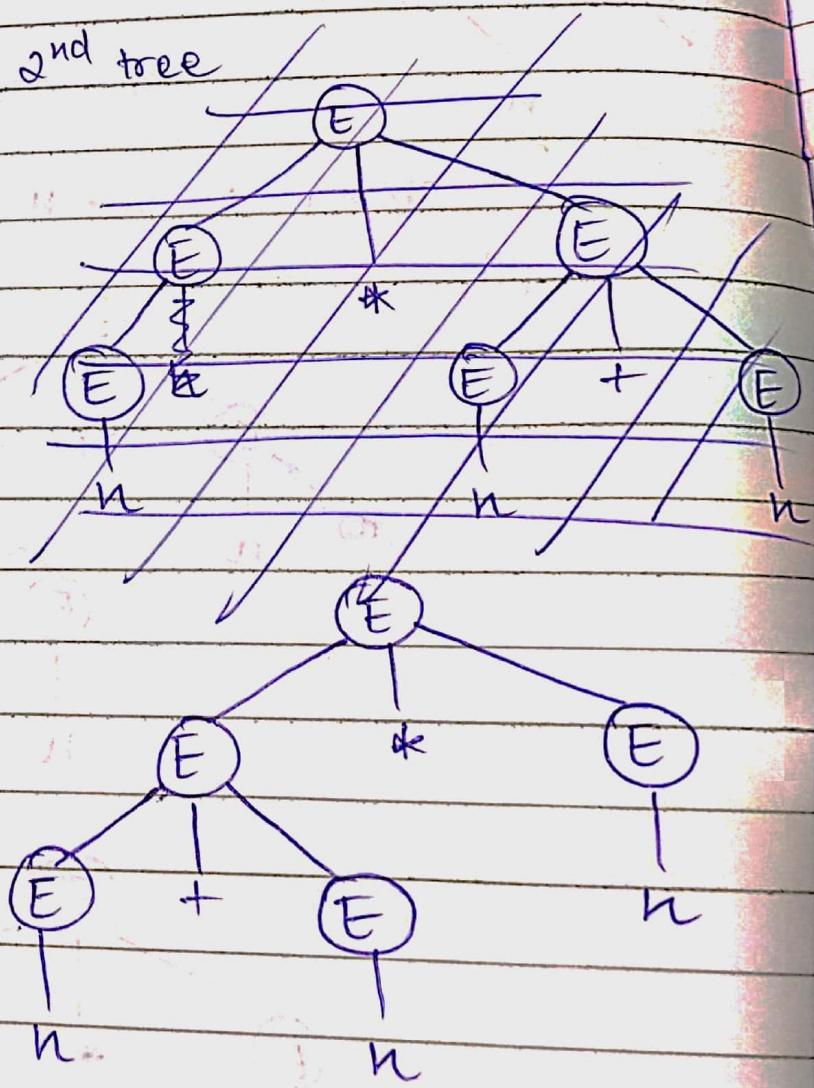
$$\begin{aligned}
 g) \quad E &\rightarrow E+E \\
 &\rightarrow n+E \\
 &\rightarrow n+E^*SE \\
 &\rightarrow n+n^*S \\
 &\rightarrow n+n^*n
 \end{aligned}$$

$$\begin{aligned}
 E &\rightarrow \underline{E^*E} \\
 &\rightarrow E+E^*E \\
 &= n+E^*E \\
 &= n+n^*E \\
 &= n+n^*kn
 \end{aligned}$$

1st tree



2nd tree



Q.B
Q3]

Given grammar :

$$S \rightarrow ASA \mid aB$$

$$A \rightarrow B \mid S$$

$$B \rightarrow b \mid \epsilon$$

Step 1 : Remove null productions .

$$S \rightarrow ASA \mid aB \mid a$$

$$A \rightarrow S \mid \epsilon$$

$$B \rightarrow b \mid \epsilon$$

$$S \rightarrow ASA \mid aB \mid a \mid S \mid AS \mid SA$$

$$A \rightarrow S \mid B$$

$$B \rightarrow b$$

Step 2 : Remove unit productions .

~~$$S \rightarrow SSS \mid ab \mid a \mid s \mid ss \mid ss$$~~

~~$$A \ B \rightarrow b$$~~

~~$$S \rightarrow ASA \mid aB \mid a \mid \epsilon \mid AS \mid SA$$~~

~~$$A \rightarrow b \mid ASA \mid aB \mid a \mid \epsilon \mid AS \mid SA$$~~

~~$$B \rightarrow b$$~~

Step 3 : Remove useless symbols .

since there are no useless symbols -
we move on . further .

Step 4: Chomsky converter.

$$S \rightarrow AD_1 | B_a B | a | AS | SA$$

$$D_1 \rightarrow SA$$

$$B_a \rightarrow a$$

$$A \rightarrow AD_1 | SA | b | a | B_a B | AS$$

$$B \rightarrow b$$

$$\therefore S \rightarrow AD | CB | a | AS | SA$$

$$D \rightarrow SA$$

$$C \rightarrow a$$

$$A \rightarrow AD | SA | b | a | CB | AS$$

$$B \rightarrow b$$

This is the required grammar.

~~QB~~
Q4

$$A \rightarrow BAB \mid B \mid \epsilon$$

$$B \rightarrow OO \mid \epsilon.$$

Step 1 : Remove null productions.

Nullable variables = { A, B } .

$$A \rightarrow BAB \mid B \mid \epsilon \mid BA \mid AB \mid A.$$

$$B \rightarrow OO$$

$$A \rightarrow BAB \mid B \mid BA \mid AB \mid A \mid BB$$

$$B \rightarrow OO.$$

Step 2 : Remove unit production.

$$A \rightarrow BAB \mid OO \mid BA \mid BB \mid AB.$$

$$B \rightarrow OO.$$

Step 3 : Remove useless production

since there are no useless productions.
 we move on further.

Step 4 : Chomsky converter.

$$A \rightarrow BD \mid OO \mid BA \mid BB \mid AB$$

$$B \rightarrow OO$$

$$D \rightarrow AB.$$

$$A \rightarrow BD \mid CC \mid BA \mid BB \mid AB$$

$$B \rightarrow CC$$

$$D \rightarrow AB.$$

$$C \rightarrow O$$

*

Pumping lemma for CFL

Let L be a CFL

Let n be a constant.

Any string z in L $|z| \geq n$

split $z = uvwx$ such that

$$|vwx| \leq n$$

$$|vx| \leq 1 \quad \text{or} \quad vx \neq \epsilon$$

(iii) For all $i=0, 1, 2, \dots, k$ $v^iwx^i \in L$



Q6.] $L = \{x^n y^n z^n \mid n \geq 1\}$ is content free or not

Step 1: let L be a content free language

Step 2: let $Z = \underline{\text{uvwxy}} x^n y^n z^n$ such that
 $\underline{\text{Q}} = Q^*$ $|Z| \geq n$. where n is the pumping lemma constant.

Step 3: As per ~~vwxyz~~ pumping lemma, $Z = \underline{uvwx}y$
 where $|\underline{vwx}| \leq n$ and $i \geq 0$, $|vwx| \geq 1$
 such $uv^iw^xv^iy$ where $i \geq 0$ would
 belong to L

Step 3c let $n = 3$.

$$L = \{a^m y z, a m y y z z, a m m y y y z z z, \dots\}$$

$$\therefore Z = \underline{a^3 b^3 c^3} a^3 y^3 z^3$$

$$|Z| \geq n$$

$$|a^3 b^3 c^3| \geq 3$$

$$a \geq 2$$

n n n y y y z z z
 u v w x y

$$u = nn$$

$$v = n$$

$$w = y$$

$$x = y$$

$$y = y z z z$$

Condⁿ 1:

$$\therefore |VWx| \leq n$$

$$|nyy| \leq 3$$

$$3 \leq 3. \checkmark$$

Condⁿ 2:

$$\cancel{(|U| > 0)} \quad \cancel{|U| < n} \quad |Vx| \geq 1$$

$$1 < n \cdot y \leq 1$$

$$2 \geq 1. \checkmark$$

For $i \geq 0$ $uv^iw^nx^iy \in L$.

$$i=0 \quad nnx^0y^0y^0z z z \in L.$$

$$z = nnyy^0z z z \notin L.$$

\therefore Our assumption that L is a context free language is wrong.

* closure properties of CFL.

- ① Union ✓
- ② Concatenation ✓
- ③ Kleene closure. ✓

→ If L_1 and L_2 are CFL and G_1 , and G_2 be their grammar respectively.

Proof :

(i) Union

$$\text{let } L_1 = \{a^n b^n, n \geq 1\}$$

then there exist a corresponding grammar.

$$G_1 = \{S_1 \rightarrow aS_1b \mid ab\}$$

$$\text{let } L_2 = \{c^m d^m, m \geq 1\}$$

$$G_2 = \{S_2 \rightarrow cS_2d \mid cd\}$$

then there exists a

the union of $L_1 \& L_2$ is $L_1 \cup L_2$

then corresponding grammar is $G : S \rightarrow S_1 \mid S_2$

$$\therefore S \rightarrow S_1 \mid S_2$$

$$S_1 \rightarrow aS_1b \mid ab$$

$$S_2 \rightarrow cS_2d \mid cd$$

(ii) concatenation

let $L_1 = \{a^n b^n \mid n \geq 1\}$

Be corr grammar,

$G_1 : S_1 \rightarrow aS_1b \mid ab$

let $L_2 = \{c^n d^n \mid n \geq 1\}$

corr grammar

$G_2 : S \rightarrow cS_2d \mid cd$.

then concatenation of L_1 and L_2 is $L_1 \cdot L_2$

then $G : S \rightarrow S_1 \cdot S_2$.

$S_1 \rightarrow aS_1b \mid ab$

$S_2 \rightarrow cS_2d \mid cd$.

(iii) Kleene closure:

let $L_1 = \{a^n b^n, n \geq 1\}$

then corr grammar

$G_1 : S_1 \rightarrow aS_1b \mid ab$

L_1^* is $(a^n b^n)^* = \{\epsilon, (a^n b^n)^1, (a^n b^n)^2, \dots, n \geq 1\}$

$S \rightarrow SS_1 \mid \epsilon$.

$S_1 \rightarrow aS_1b \mid ab$.

Module 11

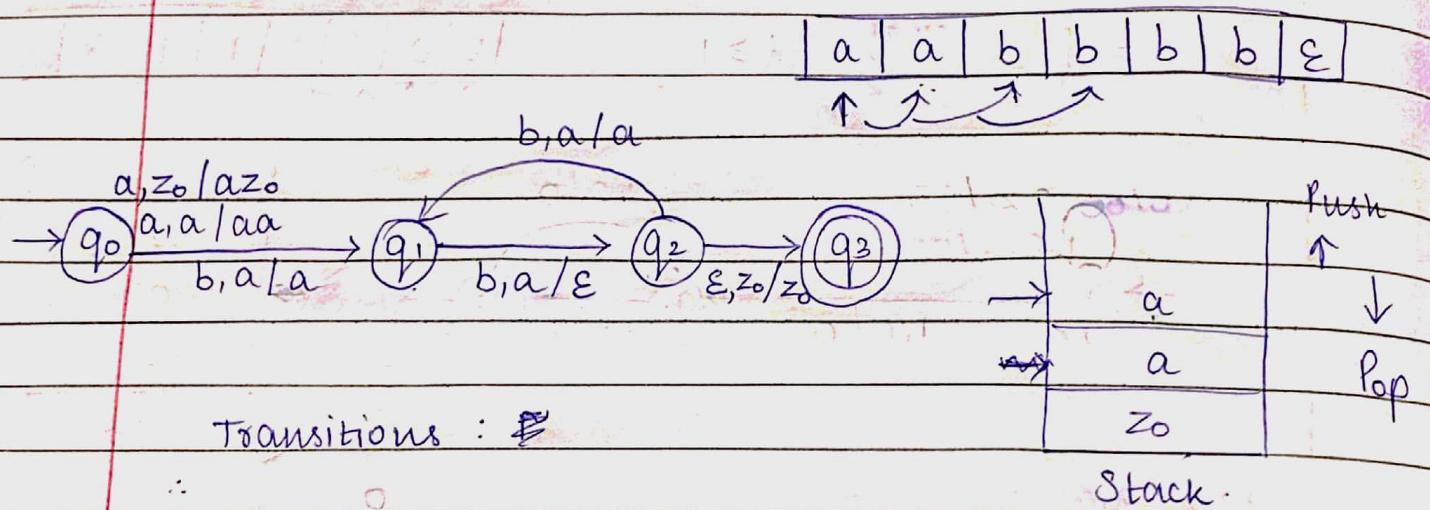
Q.B

Q11

$\{ a^n b^{2n} \mid n \geq 1 \}$

P = { Q, Σ, Δ, S, F, z₀, q₀ }

L = { abb, aabb, aabbbb, ... }



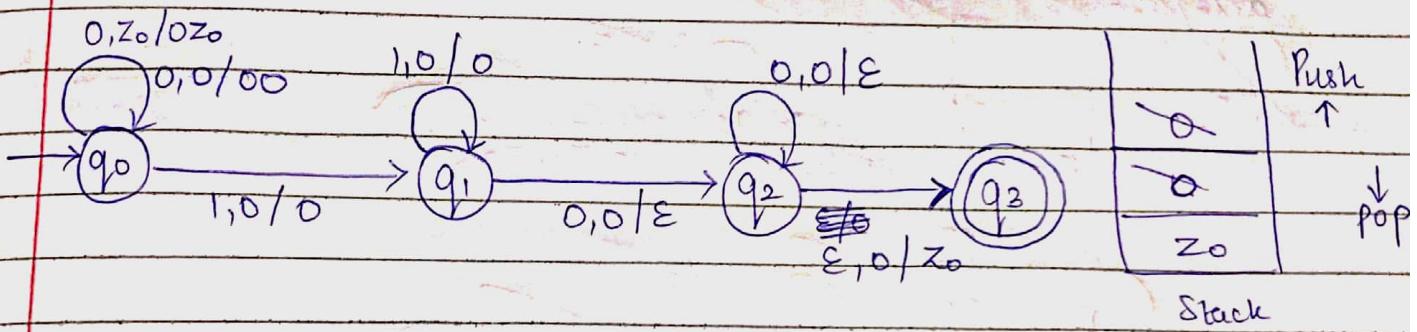
- $q_0, a, z_0 \rightarrow q_0, a z_0$
- $q_0, a, a \rightarrow q_0, aa$
- $q_0, b, a \rightarrow q_1, a$
- $q_1, b, a \rightarrow q_2, \epsilon$
- $q_2, b, a \rightarrow q_1, a$
- $q_2, \epsilon, z_0 \rightarrow q_3, z_0$

module 4
 QB
 QB

Ques $\{0^n 1^m 0^n \mid m, n \geq 1\}$

$L = \{010, 00100, 0110, \dots\}$

| 0 | 0 | 1 | 1 | 1 | 0 | 0 | ε



$$\delta(q_0, a, z_0) \rightarrow (q_0, az_0)$$

$$\delta(q_0, a, a) \rightarrow (q_0, aa)$$

$$\delta(q_0, 1, 0) \rightarrow (q_1, 0)$$

$$\delta(q_1, 1, 0) \rightarrow (q_1, 0)$$

$$\delta(q_1, 0, 0) \rightarrow (q_2, \epsilon)$$

$$\delta(q_2, 0, 0) \rightarrow (q_2, \epsilon)$$

$$\delta(q_2, \epsilon, z_0) \rightarrow (q_3, z_0)$$

PDA, $P = \{q_0, q_1, q_2, q_3\}, \Sigma = \{0, 1\}$

QB MU
Q47

DPDA

NPDA

- | | |
|---|--|
| 1) It is less powerful than NPDA.
eg) It can be used to construct only odd-length palindromes and not even-length palindromes. | 1) It is more powerful than DPDA.
eg) It can be used to construct both odd and even length palindromes. |
| 2) It is possible to convert every DPDA into corresponding NPDA. | 2) It is not possible to convert every NPDA into corresponding DPDA. |
| 3) The language accepted by DPDA is a subset of the language accepted by NPDA. | 3) The language accepted by NPDA is not a subset of the language accepted by DPDA. |
| 4) The language accepted by DPDA is called DCFL (Deterministic Content Free language) | 4) The language accepted by NPDA is called NCFL (Non-deterministic content free language) |
| 5) There is only one state transition from one state to another state for an input symbol | 5) There may or may not be more than one state transition from one state to another state for some input symbol. |

in both left, right.

~~QB~~ MB
~~Q2~~

$L = \{a^n b^n \mid n \geq 1\}$

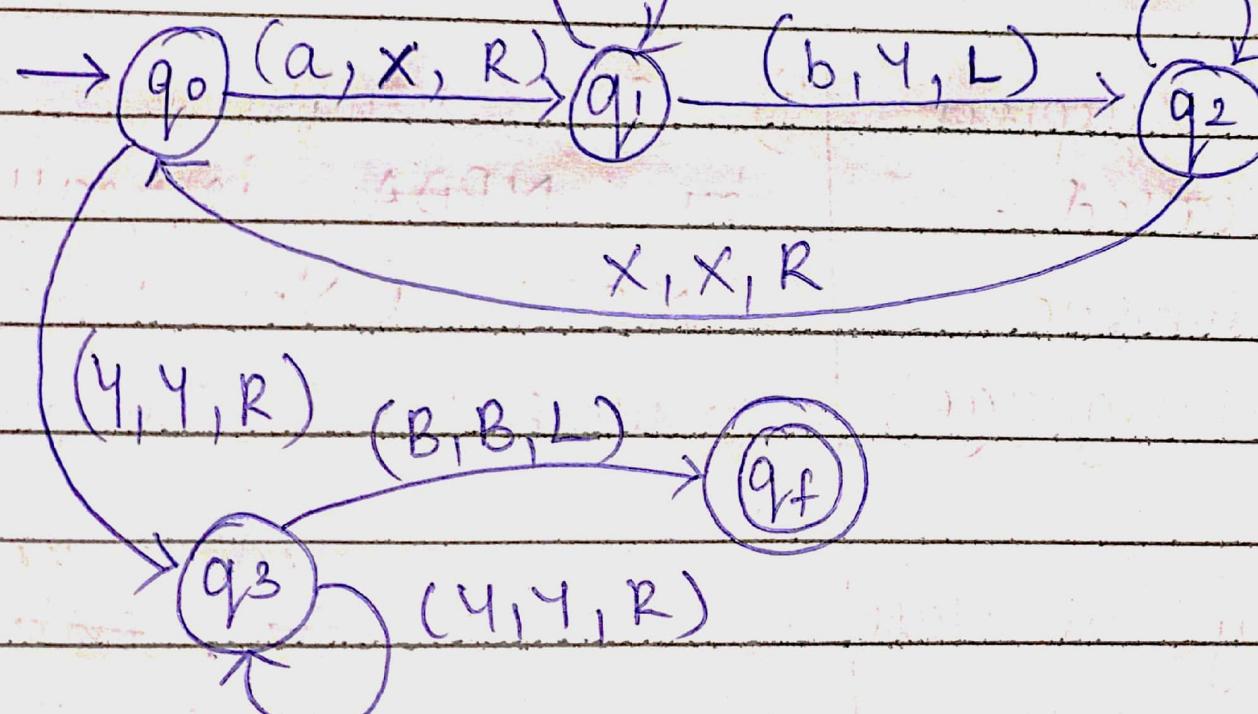
for $n=3$

T	B	B	X	X	a	X	b	b	B	B
			X	X	a	X	b	b	B	B
			a	a	L	a	a	L	B	B

(Y, Y, R)
(a, a, R)

(b, Y, L)

q_2



~~QF Q1~~ M5

Timing machine is complement of binary number.

01011000

Let the input = 01011000

