

## Arithmetic Calculation

————— - Addition —————

$$-5 + 3 = -2$$

$$-3.2 + 1.6 = -1.6$$

$$0.1 + 0.1 = 0.2$$

$$0.24 + 0.36 = 0.6$$

$$-12 + 2.3 + 3.45 = -6.25$$

————— - Subtraction —————

$$2.3 - 1.2 = 1.1$$

$$0.1 - 0.1 = 0$$

$$0.5 - 0.72 = -0.22$$

$$3.2 - 1.6 = 1.6$$

$$7.5 - 1.6 - 2.1 = 3.8$$

$$10 - 73 - 28 = -91$$

————— - Multiplication —————

$$1.2 \times (-2.3) = -2.76$$

$$0.1 \times 0 = 0$$

$$0.5 \times 0.5 = 0.25$$

$$3.2 \times 1.6 = 5.12$$

$$0.5 \times 0.7 = 0.35$$

$$-3.2 \times 1.6 \times 0.7 = -3.584$$

———— Division ————

$$3.7 \div (-1.4) = -2.643$$

$$2 \div 3 = 0.667$$

$$1 \div 3 = 0.333$$

$$10 \div 7 = 1.429$$

$$5.12 \div 1.6 = 3.2$$

$$(-5.12) \div 1.6 \div (-0.8) = 4$$

$$9 \div 3 \div 2 = 1.5$$

———— Arithmetic Calculation in General ————

$$(22 \times 12) + (486 \div 6) = 345$$

$$(8.63 + 7.05) \times (6.5 - 1.6) = 76.832$$

## Combinatorics

———— Factorials ————

$$7! = 5040$$

———— Permutations ————

$${}_9P_4 = 3024$$

———— Combinations ————

$${}_9C_9 = 1, {}_9C_8 = 9, {}_9C_7 = 36, {}_9C_6 = 84, {}_9C_5 = 126,$$

$${}_9C_4 = 126, {}_9C_3 = 84, {}_9C_2 = 36, {}_9C_1 = 9, {}_9C_0 = 1$$

$${}_{20}C_0 = 1, {}_{20}C_1 = 20, {}_{20}C_2 = 190, {}_{20}C_3 = 1140, {}_{20}C_4 = 4845, {}_{20}C_5 = 15504, {}_{20}C_6 = 38760,$$

$${}_{20}C_7 = 77520, {}_{20}C_8 = 125970, {}_{20}C_9 = 167960, {}_{20}C_{10} = 184756, {}_{20}C_{11} = 167960,$$

$${}_{20}C_{12} = 125970, {}_{20}C_{13} = 77520, {}_{20}C_{14} = 38760, {}_{20}C_{15} = 15504, {}_{20}C_{16} = 4845, {}_{20}C_{17} = 1140,$$

$${}_{20}C_{18} = 190, {}_{20}C_{19} = 20, {}_{20}C_{20} = 1$$

———— Binomial Expansion ————

$$(x + y)^2 = x^2 + 2xy + y^2$$

$$(x - y)^2 = x^2 - 2xy + y^2$$

$$(x + y)^3 = x^3 + 3x^2y + 3xy^2 + y^3$$

$$(x - y)^3 = x^3 - 3x^2y + 3xy^2 - y^3$$

$$(a + b)^4 = a^4 + 4a^3b + 6a^2b^2 + 4ab^3 + b^4$$

$$(\alpha + \beta)^9 = \alpha^9 + 9\alpha^8\beta + 36\alpha^7\beta^2 + 84\alpha^6\beta^3 + 126\alpha^5\beta^4 + 126\alpha^4\beta^5 + 84\alpha^3\beta^6 + 36\alpha^2\beta^7 + 9\alpha\beta^8 + \beta^9$$

$$(\alpha - \beta)^9 = \alpha^9 - 9\alpha^8\beta + 36\alpha^7\beta^2 - 84\alpha^6\beta^3 + 126\alpha^5\beta^4 - 126\alpha^4\beta^5 + 84\alpha^3\beta^6 - 36\alpha^2\beta^7 + 9\alpha\beta^8 - \beta^9$$