基礎数学

演習問題3

問題1 次の式をなるべく簡単な方法で計算せよ。

(1)
$$\left(\frac{1}{3} - \frac{5}{7}\right) \times (-21) = -7 + 15 = 8$$

$$(2) \left(\frac{3}{11} + \frac{5}{12}\right) \times 396 = \left(\frac{3}{11} + \frac{5}{12}\right) \times 3 \times 11 \times 12 = (3 \times 12 + 5 \times 11) \times 3 = 91 \times 3 = 273$$

(3)
$$\left(\frac{2}{3} - \frac{30}{45}\right) \times 1234 = \left(\frac{2}{3} - \frac{2}{3}\right) \times 1234 = 0$$

(4)
$$23 \times 34.5 + 27 \times 34.5 = (23 + 27) \times 34.5 = 50 \times 34.5 = \frac{3450}{2} = 1725$$

(5)
$$998 \times 12.5 = (1000 - 2) \times 12.5 = 12500 - 25 = 12475$$

(6)
$$0.87 \times 0.54 + 0.26 \times 0.27 = 0.87 \times 0.54 + 0.13 \times 0.54 = (0.87 + 0.13) \times 0.54 = 0.54$$

(7)
$$28 \times 0.25 = 28 \times \frac{1}{4} = 7$$

(8)
$$32 \times 0.125 = 32 \times \frac{1}{8} = 4$$

問題2 次の方程式を解け。

(1)
$$\frac{1}{5}x - \frac{1}{4}x = 1$$
 (答) $x = -20$

(2)
$$4 - \frac{3}{4}x = \frac{1}{2}x + 8$$
 (答) $\frac{5}{4}x = -4$ より、 $x = -\frac{16}{5}$

(3)
$$\frac{x}{2} + 7 = 7 - \frac{x}{2}$$
 (答) $x = 0$

(4)
$$\frac{1}{4}x + \frac{1}{5}x = \frac{1}{2}x - 3$$
 (答) $\frac{x}{20} = 3$ より、 $x = 60$

(5)
$$y + \frac{y}{3} + \frac{y}{4} = 19$$
 (答) $\frac{19}{12}y = 19$ より、 $y = 12$

(6)
$$2 + \frac{4}{x+3} = 6$$
 (答) $\frac{4}{x+3} = 4$, 両辺を 4 で割って、 $\frac{1}{x+3} = 1$, $\therefore x = -2$

(7)
$$\frac{1}{x+1} + \frac{2}{x+1} = \frac{3}{2}$$
 (答) $\frac{3}{x+1} = \frac{3}{2}$, すなわち、 $x+1=2$, $\therefore x=1$

(8)
$$x+3=\frac{4}{x+3}$$
 (答) $(x+3)^2=4$, よって、 $x+3=\pm 2$, ゆえに、 $x=-5$, -1