ocaml 第五期レポート課題

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1 解いた問題

問題 1,2,3,6,4,5

2 問題1

SProlog の生成規則と抽象構文木の対応を参考にしながら, SProlog 処理系を完成させなさい

2.1 プログラムソース

```
module Lexer = struct
3 type token = CID of string | VID of string | NUM of
     string
                 TO | IS | QUIT | OPEN | EOF | ONE of
4
                  char
6
7
  module P = Printf
  exception End_of_system
  let JSTREAM = ref stdin
10
11
12
  let ch = ref | |
13
  let read () = match !ch with [] -> input_char !
14
     LISTREAM
                          | h :: rest \rightarrow (ch := rest; h)
15
16
17
   let unread c = ch := c :: ! ch
18
   let lookahead () = try let c = read () in unread c; c
      with End_of_file -> '$'
20
21
   let rec integer i =
   (* 文字列として数字を構成 *)
22
    let c = lookahead () in
23
       if (c >= '0' \&\& c <= '9') then
24
25
              integer (i^(Char.escaped (read ())))
26
       else i
27
28 and identifier id =
```

```
29
    let c = lookahead () in
        if ((c >= 'a' && c <= 'z') || (c >= 'A' && c <= '
30
          Z') |
           (c >= '0' \&\& c <= '9') || c == '_-') then
31
32
              identifier (id^(Char.escaped (read ())))
33
34
   and native\_token () =
35
36
    let c = lookahead () in
      if (* CID に対する識別子および予約語 *)
37
          (c >= 'a' && c <= 'z') then
38
             let id = identifier "" in
39
                  match id with
"is" -> IS
|"quit" -> QUIT
40
41
42
                  " open" -> OPEN
43
                  " e o f" → EOF
44
                   _{-} \rightarrow CID (id)
45
      else if (* VID に対する識別子 *)
46
47
          (c \ge 'A' \&\& c \le 'Z') then VID (identifier "")
       else if (c >= '0' \&\& c <= '9') then NUM (integer
48
         "")
49
       else if (* :- を認識して TO を返す *)
          (c=':') then (let sub1 = read() in let sub2 = read()
50
              read() in
                            if sub2 = '-' then TO
51
52
                            else ONE (sub1))
53
      else ONE (read ())
54
55
   and gettoken () =
56
   \operatorname{try}
57
   let token = native_token () in
58
     match token with
        ONE ' ' -> gettoken ()
59
        ONE '\t' -> gettoken ()
60
        ONE '\n' -> gettoken ()
61
62
        _ -> token
63
   with End_of_file -> EOF
64
65
   let print_token tk =
   match tk with
   (CID i) \rightarrow P.printf "CID(\%s)" i
67
   (VID i) \rightarrow P. printf "VID(\%s)" i
68
```

```
(NUM i) \rightarrow P.printf "NUM(\%s)" i
69
       (TO) -> P. printf ":-"
70
       (QUIT) -> P. printf "quit"
 71
       (OPEN) -> P. printf "open"
 72
73
       (IS) -> P. printf "is"
       (EOF) -> P. printf "eof"
74
       (ONE c) \rightarrow P. printf "ONE(\%c)" c
75
76
 77
    let rec run () =
 78
       flush stdout;
79
        let rlt = gettoken () in
80
            match rlt with
               (ONE '$') -> raise End_of_system
81
82
              -> (print_token rlt; P.printf "\n"; run())
83
84
   end
85
86
   module Evaluator = struct
    (* 抽象構文木の型宣言 *)
    type ast = Atom of string | Var of string | App of
       string * ast list
89
90
    (* 抽象構文木の印字関数 *)
    module P = Printf
91
    let rec print_ast ast = match ast with
92
        (App(\hat{s}, hd::tl)) \rightarrow (P.printf "App(\"%s\",["s;
93
           print_ast hd; List.iter (fun x -> (print_string)
94
               ";"; print_ast x)) tl;
               print_string "])")
95
          (App(s, [])) \rightarrow P. printf "App(\"%s\",[])" s
96
   | (Atom s) -> P. printf "Atom \"%s\"" | (Var s) -> P. printf "Var \"%s\"" s | let print_ast_list lst = match lst with
97
98
99
        (hd::tl) -> (print_string "["; print_ast hd;
100
           List.iter (fun x -> (print_string ";";
101
           print_ast x)) tl; print_string "]")
102
        | [] -> print_string "[]"
103
104
    (* 関数 sub, mgu, succeed, rename solve eval の定義 *)
105
106
    let sub name term =
        let rec mapVar ast = match ast with
107
           (Atom x) \rightarrow Atom(x)
108
109
           (Var n) -> if n=name then term else Var n
```

```
| (App(n, terms)) \rightarrow App(n, List.map mapVar terms)
110
111
    in mapVar
112
    let mgu (a,b) =
113
114
       let rec ut (one, another, unifier) = match (one,
          another) with
           ([], []) -> (true, unifier)
115
          | (term::t1, Var(name)::t2) ->
116
            let r = \text{fun } x \rightarrow \text{sub name term (unifier } x) in
117
               ut(List.map r t1, List.map r t2, r)
118
          | (Var(name)::t1, term::t2) >
119
            let r = \text{fun } x \rightarrow \text{sub name term (unifier } x) in
120
121
               ut (List.map r t1, List.map r t2, r)
           (Atom(n) :: t1, Atom(m) :: t2) \rightarrow
122
123
            if n=m then ut(t1,t2, unifier) else (false,
               unifier)
            (App(n1,xt1)::t1, App(n2,xt2)::t2) \rightarrow
124
125
            if n1=n2 && List.length xt1 = List.length xt2
               then
               ut(xt1@t1, xt2@t2, unifier)
126
            else (false, unifier)
127
          | (_,_) `-> (false, unifier);
128
       in ut ([a], [b], (fun x \rightarrow x))
129
130
131
    let succeed query = (print_ast query; true)
132
133
    let rename ver term =
      let rec mapVar ast = match ast with
134
135
             (Atom x) \rightarrow Atom(x)
             (Var n) -> Var(n^, #"^ver)
136
             (App(n, terms)) -> App(n, List.map mapVar
137
              terms)
138
      in mapVar term
139
140
    exception Compiler_error
141
142
    let rec solve (program, question, result, depth) =
       match question with
143
       [] -> succeed result
144
     goal::goals ->
        let onestep _ clause =
145
        match List.map (rename (string_of_int depth))
146
```

```
clause with
147
           [] -> raise Compiler_error
148
        | head::conds ->
           let (unifiable, unifier) = mgu(head, goal) in
149
            if unifiable then
150
              solve (program, List.map unifier (
151
                conds@goals),
152
                                      unifier result, depth
                                         +1)
153
            else true
154
       in List.fold_left onestep true program
155
    let eval (program, question) = solve(program, [
156
       question, question, 1)
157
158
    end
159
160
   module Parser = struct
161
   module L = Lexer
162
163
164
   module E = Evaluator
165
166
    let tok = ref (L.ONE', ')
167
    let getToken () = L. gettoken ()
168
169
    let advance () = (tok := getToken())
170
171
172
    exception Syntax_error
173
174
    let error () = raise Syntax_error
175
176
    let check t = match ! tok with
        L.CID_- \rightarrow if (t = (L.CID"")) then () else error
177
        L.VID \longrightarrow if (t = (L.VID "")) then () else
178
          error()
                \sim if (t = (L.NUM "")) then () else
179
        L.NUM
          error()
       tk \rightarrow if (tk=t) then () else error()
180
181
182
    let eat t = (check t; advance())
183
184 let prog = ref [[E. Var ""]]
```

```
185
    let rec clauses () = match ! tok with
186
187
         L.EOF \rightarrow | |
        | - >  let a =  clause() in let b =  clauses() in a
188
189
    and clause() = match !tok with
190
         L.ONE (, -) let a = [term()] in eat(L.ONE (, -));
191
        -> let a = predicate() in let b = to_opt() in
192
           eat (L.ONE '.') ; a::b
193
    and to_opt() = match !tok with
194
195
         L.TO \rightarrow eat(L.TO); let b = terms() in b
196
        | _ -> []
197
    and command() = match !tok with
198
199
         L.QUIT \rightarrow exit 0
        | L.OPEN \rightarrow (eat(L.OPEN);
200
201
           match ! tok with
            L.CID s \rightarrow (eat(L.CID ""); check (L.ONE '.');
202
            L. JSTREAM := open_in (s^".pl"); advance();
203
204
               prog := clauses(); close_in (!L._ISTREAM))
        | _ -> error())
205
        | - \rangle let t = term() in
206
207
               (\operatorname{check}(L.ONE', '); \operatorname{let}_{-} = E.\operatorname{eval}(!\operatorname{prog}, t)
                  in ())
208
    and term () = match !tok with
209
         L.ON\dot{E}''(' -> (eat(L.ONE '(') ; let b = term() in
210
            eat (L.ONE ') ') ; b)
        |L.VID s| \rightarrow (eat(L.VID "") ; eat(L.IS) ; expr())
211
212
        |  \rightarrow let a = predicate() in a
213
    and terms() = (let a = [term()] in let c = terms')
214
       in a @ c)
215
    and terms'() = match !tok with L.ONE',' \rightarrow (eat(L.ONE','); let d = [term()]
216
217
            in let e = terms'() in d@e)
218
        | _ -> []
219
220 and predicate() = match !tok with
```

```
L.CID \ a \rightarrow (eat(L.CID "") ; eat(L.ONE '(') ; let
221
           b = args() in eat(L.ONE')'); E.App (a,b))
222
        _ -> error()
223
    and args() = let a = [expr()] in let c = args'() in a
224
225
226
    and args'() = match !tok with
        L.\breve{ONE}', '-> (eat(L.ONE', '); let d = [expr()] in let e = args'() in d@e
227
228
229
       _ -> []
230
231
    and expr() = match ! tok with
        L.ONE '(' -> (eat(L.ONE '(') ; let b = expr() in
232
              eat(L.ONE, ') ') ; b)
         L.ONE (') (eat (L.ONE ')); let a = list() in
233
            eat (L.ONE ', ', ', a)
         L.CID s \rightarrow (eat(L.CID ""); tail_opt s)
L.VID s \rightarrow (eat(L.VID ""); E.Var s)
234
235
          L.NUM n -> (eat (L.NUM ""); E.Atom n)
236
237
          _ -> error()
238
239
    and tail_opt s = match !tok with
          L.ONE '(' -> (eat(L.ONE '(') ; let a = args() in
240
              eat(L.ONE')); E.App (s\
241
     , a))
242
       _ -> E.Atom s
243
    and list() = match !tok with
244
         L.ONE '] ' -> E.Atom "nil"
245
        | - \rangle E.App ("cons", [expr(); list_opt()])
246
247
    and list_opt() = match !tok with
248
        L.ONE ', ', '-> (eat(L.ONE ', ')); id()
| L.ONE ', '-> (eat(L.ONE ', ')); list()
249
250
        _ -> E.Atom "nil"
251
252
    and id() = match !tok with
253
         L.CID = -> (eat(L.CID "")) ; E.Atom = 
254
        |L.VID| a \rightarrow (eat(L.VID) ""); E.Var a
255
        L.NUM a \rightarrow (eat(L.NUM"")); E.Atom a
256
257
        _ -> error()
```

```
258
259 end
260
261
   let rec run() =
        print_string "?- ";
262
263
        while true do
          flush stdout; Lexer. JSTREAM := stdin;
264
          Parser.advance(); Parser.command();
265
             print_string \n'.\n?-"
266 done
267
268 \, \text{let}_{-} = \text{run}()
```

2.2 左再帰を除いた文法

新しく terms'、args' を定義することで左再帰を除き、右再帰に変換することができる。

```
2.2.1 terms
  terms → term terms'
  terms' → "," term terms'
  terms' →

2.2.2 args
  args → expr args'
  args' → "," expr args'
  args' →
```

2.3 プログラムの説明

第四期の課題で作成した Lexer と Parser を用いて、Parser の中身を与えられた文法に従って構成し直した。前回と同様に右再帰の関数は上記のように文法を作り直した。また、Evaluator に関しては授業プリントを参考にしながら作成した。

3 問題 2

isono プログラムを入力し、いくつかの質問について、振舞いを確認しなさい.

3.1 実行結果

以下のように正しく動作していることがわかる。

```
?- open isono.
?-mother(X,Y).
App("mother",[Atom "sazae";Atom "tara"])App("mother",[Atom "fune";Atom "sazae"])
App("mother",[Atom "fune";Atom "katsuo"])App("mother",[Atom "fune";Atom "wakame"])
?-female(X).
App("female",[Atom "fune"])App("female",[Atom "wakame"])App("female",[Atom "sazae"])
?-
```

4 問題3

第9章で示した関数 succeed では、インスタンス化した質問の構文木を 印字するようになっている.これを、SProlog のソース言語の表現で印字す るようにしなさい

4.1 プログラムソース

Evaluator 内の抽象構文木について以下のような変更を加えた。

```
1 module P = Printf
2 let rec print_ast ast = match ast with
3     (App(s, hd::tl)) -> (P.printf "%s(" s;
4          print_ast hd; List.iter (fun x -> (print_string ";"; pri
5          print_string ")")
6     | (App(s, [])) -> P.printf "%s" s
7     | (Atom s) -> P.printf "%s" s
8     | (Var s) -> P.printf "%s" s
```

9 let print_ast_list lst = match lst with

4.2 プログラムの説明

抽象構文木の印字関数の部分を Sprolog のソース言語の表現と同じになるように変更を加えた。

4.3 実行結果

以下のように正しく動作していることがわかる。

```
end
val run : unit -> unit = <fun>
?- mother(X,Y).
mother(X;Y)
?-open isono.
?-mother(X,Y).
mother(sazae;tara)mother(fune;sazae)mother(fune;katsuo)mother(fune;wakame)
?-female(X).
female(fune)female(wakame)female(sazae)
?-
```

5 問題 6

[,」で並べた複数質問を受け付けられるように拡張せよ

5.1 プログラムソース

```
10
    match question with
     [] -> succeed result a b
11
12
      goal::goals ->
13
       let onestep _ clause =
       match List.map (rename (string_of_int depth))
14
          clause with
          [] -> raise Compiler_error
15
16
         head::conds \rightarrow
          let (unifiable, unifier) = mgu(head, goal) in
17
           if unifiable then
18
             solve (program, List.map unifier (
19
                conds@goals),
20
                                List.map unifier result, a,
21
                                List.map unifier b, depth +
                                   1)
           else true
23 in List.fold_left onestep true program
24
25
   let rec get x =
26
      match x with
27
         | hd :: tl -> match hd with
28
                          Var t \rightarrow Var t :: (get tl)
29
30
                          Atom s -> get tl
31
                         |App(x,y)| \rightarrow (get y) \otimes (get tl)
32
\overline{33}
   let rec find y =
34
      let rec sub n lst =
            match 1st with
35
36
               | | -> | |
37
              |hd :: tl \rightarrow if hd = n then sub n tl
38
                            else hd :: sub n tl
39
      in match y with
40
            | | -> | |
41
           |hd :: tl \rightarrow hd :: (find (sub hd y))
42
   let eval (program, question) =
43
   let l = find (get question)
45
   in solve (program, question, question, l, l, 1)
46
47
   and command() = match !tok with
       L.QUIT -> exit 0
48
       L.OPEN \rightarrow (eat(L.OPEN);
49
          match ! tok with
50
```

5.2 プログラムの説明

抽象構文木の部分と command 関数に変更を加えることで複数質問に答え られるようにした。

5.3 実行結果

以下のように正しく動作していることがわかる。

```
?-grandfather(X,tara),parents(X,Y).
X=namihei
Y=sazae
X=namihei
Y=katsuo
X=namihei
Y=wakame
```

6 問題 4、問題 5

通常の Prolog は、質問が真であったとき、インスタンス化した質問を印字するのではなく、質問に含まれる変数ごとに、対応する項を印字する. SProlog の処理系もそのように拡張せよ

通常の Prolog は、質問が真である単一化代入が得られるたびに、推論を継続するか終了するかを指示することができる. SProlog の処理系も、succeed が呼ばれるたびに、実行を中断し、[;」を打ち込むと継続、[.」を打ち込むと、それ以降の処理を回避するように拡張しなさい

6.1 プログラムソース

```
1 let succeed query a b =
2 (print a b ; print_string "Yes"; flush stdout;
```

6.2 プログラムの説明

問題6から印字関数に手を加えることで表記を正しいものに変更した。

6.3 実行結果

以下のように正しく動作していることがわかる。

```
val run : unit -> unit = <fun>
?- open isono.
?-parents(X,tara).
X=masuo
Yes;
X-sazae
Yes.
No
?-
```