TD Calcul Numérique

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5.1	Euler Explicite
a.	
b.	
5.2	Heun
a.	
b.	

Euler Implicite

a. Déterminons un polynôme :

Exercie 1

1

5.3

$$y_{i+1} = y_i + hf(y_{i+1})$$

$$y_{i+1} = y_i + h\frac{1}{2y_{i+1} + 1}$$

$$y_{i+1} = \frac{y_i(2y_{i+1} + 1) + h}{2y_{i+1} + 1}$$

$$y_{i+1}(2y_{i+1} + 1) = y_i(2y_{i+1} + 1) + h$$

$$2y_{i+1}^2 + y_{i+1} = y_i + 2y_{i+1}y_i + h$$

$$2y_{i+1}^2 + y_{i+1} - 2y_{i+1}y_i = y_i + h$$

$$2y_{i+1}^2 + y_{i+1} - 2y_{i+1}y_i - y_i - h = 0$$

$$2y_{i+1}^2 + (1 - 2y_i)y_{i+1} - y_i - h = 0$$

b. Calculons le descriminant :

$$\Delta = b^2 - 4ac$$

$$\Delta = (1 - 2y_i)^2 - [4 * 2 * (-y_i - h)]$$

$$\Delta = (1 - 2y_i)^2 + 8y_i + 8h$$

$$\Delta = 1 - 4y_i + (2y_i)^2 + 8y_i + 8h$$

$$\Delta = 1 + 4y_i + (2y_i)^2 + 8h$$

$$\Delta = (2y_i + 1)^2 + 8h$$

c. Déterminons y_{i+1} en fontion de y_i et h :

$$y_{i+1} = \frac{-b + \sqrt{\Delta}}{2a}$$
$$y_{i+1} = \frac{2y_i - 1 + \sqrt{(2y_i + 1)^2 + 8h}}{4}$$

- 6 Exercie 6
- 7 Exercie 7
- 8 Exercie 8