- · Shonak Shah
- A13497236
- COGS118C Assignment 3

This notebook has [50 + 5 Bonus] points in total

The number of points for each question is denoted by []. Make sure you've answered all the questions and that the point total add up.

Lab 3 - Time-Frequency Analysis and Filtering

In this lab, we will cover time-frequency (TF) analysis, and the two main ways of doing this (short-time Fourier transform (STFT) and filtering). In particular, we will motivate why TF analysis is performed, rather than just applying Fourier Transform to your whole recording once. We will code for ourselves the operations required to perform STFT and filtering, then explore parameter choice considerations when applying these methods. From the time-frequency representation, we will compute the spectrogram, power spectral density, and phase coherence. We will also explore the effect of windowing on your spectral estimates. Finally, there is a practical tutorial on filtering and visualizing the frequency response of filters.

Key concepts:

- Short Time Fourier Transform (STFT)
- (Symmetry and orthogonality of DFT complex exponentials)
- Time-frequency uncertainty principle
- Power spectral density (PSD), event-related spectral response (ERSP) and phase coherence
- Windowing
- Convolution and filtering
- · Filter parameter choices

Note: in this lab, the written responses are entered in the cell immediately below the question, so that when you write your response, it doesn't screw up the formatting of the question. Thank you for this suggestion.

```
In [1]: # make the imports
%matplotlib inline
import matplotlib.pyplot as plt
import numpy as np
from scipy import io, signal # we will also import the signal module, from scipy
```

```
In [2]:

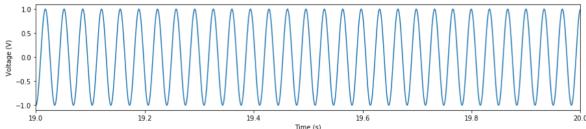
    def plot_spectrogram(spg, t, f, freq_lims=[0,100], plot_db=False):

                Utility function for plotting the spectrogram for you.
                spg: spectrogram, 2D real-numbered array, dimensions are [frequency x time]
                t: time axis of spectrogram
                f: frequency axis of spectrogram
                freq lims (optional): limits the frequency axis, defaults to 0-100Hz
                plt.figure(figsize=(15,4))
                if plot db:
                    plt.imshow(10*np.log10(spg), aspect='auto', extent=[t[0], t[-1], f[-1],
                else:
                     plt.imshow(spg, aspect='auto', extent=[t[0], t[-1], f[-1], f[0]])
                plt.xlabel('Time'); plt.ylabel('Frequency(Hz)');
                plt.ylim(freq lims)
                plt.colorbar()
                plt.tight_layout()
```

Time and Frequency Resolution

At the heart of time-frequency analysis is the ability to resolve how frequencies change over time, whereas a single Fourier transform (or power spectrum) is unable to. Below, we will simulate a 20-second signal to analyze. I plot the data in time for you already.

```
In [3]: I
```



[5] Q1: Computing Power Spectrum

[3] 1.1: Compute the power spectrum of the signal (store in variable ps), starting from its Fourier transform (np.fft.fft). Plot the power spectrum and label your axes. Remember, plot x-axis as frequency in Hz, this is now an implicit requirement moving forward for all frequency domain to adding [MathJax]/extensions/Safe is otherwise stated. You can use np.fft.fftfreq). Zoom into 0-50Hz.

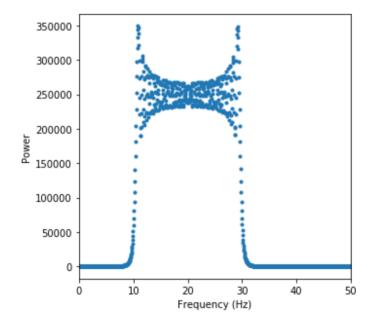
- [1] 1.2: Comment on the frequency content of the signal based on the power spectrum (i.e., what frequencies are present and/or domninant).
- [1] 1.3: Does what you see in the time-seres plot (above) match what you see in the power spectrum, in terms of frequency content? Feel free to manipulate the x-limits of the time series plot to explore.

Response for 1.2: Frequencies are between 8 and 32 with 2 dominant ones at each end around 10 and 30.

Response for 1.3: Yes, since the longest frequencies were those with the most power.

```
In [4]: #_YOUR_CODE_HERE
    coef = np.fft.fft(sig)
    ps = coef.real**2 +coef.imag**2
    freqs = np.fft.fftfreq(len(ps), 1/fs)
    plt.figure(figsize=(5,5))
    plt.plot(freqs, ps, '.')
    plt.xlim([0,50])
    plt.xlabel("Frequency (Hz)")
    plt.ylabel("Power")
```

Out[4]: Text(0,0.5,'Power')



[5] Q1 - Continued

- [1] 1.4: You'll be doing this a lot in the following section, so create a function that computes the power spectrum (pwsp) given a signal and it's sampling frequency, as well as returning the frequency axis (freqs).
- [1] 1.5: Using your function, compute the power spectrum of the **first second** of the signal, i.e., where t=[0,1) (this notation means inclusive of t=0, and exclusive of t=1, i.e. t>=0 and tfs=1000. Plot the power spectrum and zoom into 0-50Hz (you'll be doing this a lot too, so consider making an addition <u>functional for plotting</u>, though this is not required).

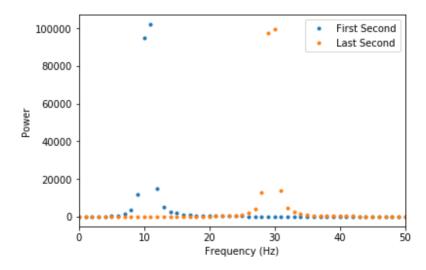
[1] 1.6: Repeat 1.5, but for the last second of the data. You can plot them on the same plot. Remember to label your traces as well using plt.legend().

[2] 1.7 Comment on the similarities and differences between the two power spectrum plotted for 1.5 and 1.6, and your interpretation of this in terms of the frequency content. Compare this plot with the plot for Question 1.1, what are their similarities and differences?

Response for 1.7: The spectrums are similar in shape but occur at different frequencies showing that roughly the 10Hz and 30Hz frequencies contribute equally to the signal. This gets rid of the middle band of frequencies by just focusing on the first and last seconds. It is the same as 1.1 in that those frequencies clearly contribute the most as their powers are much higher than those of surrounding frequencies.

```
In [5]:
            def compute pwsp(sig, fs):
                # YOUR CODE HERE
                coef = np.fft.fft(sig)
                pwsp = coef.real**2 +coef.imag**2
                freqs = np.fft.fftfreq(len(pwsp), 1/fs)
                return pwsp, freqs
            pwsp first, freqs win = compute pwsp(sig[:1000], 1000) # YOUR CODE HERE
            pwsp_last, _ = compute_pwsp(sig[-1000:],1000)
            plt.figure(figsize=(6,4))
            # YOUR CODE HERE
            plt.plot(freqs_win, pwsp_first,'.', label= 'First Second')
            plt.plot(freqs_win, pwsp_last,'.', label= 'Last Second')
            plt.xlim([0,50])
            plt.xlabel("Frequency (Hz)")
            plt.ylabel("Power")
            plt.legend()
```

Out[5]: <matplotlib.legend.Legend at 0x235c15dcc88>

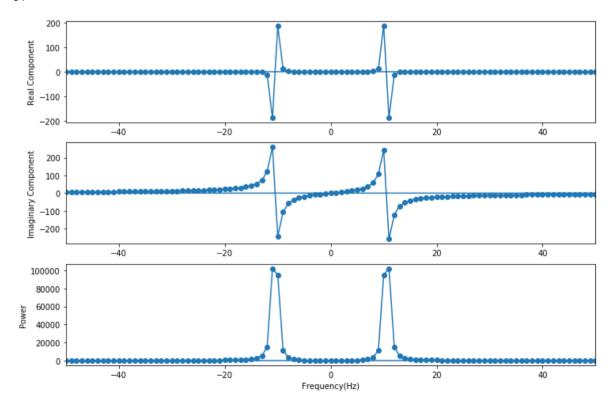


Symmetry and Nyquist Frequency in DFT

Loading [MathJax]/extensions/sale: to explain it in code, see L9 slides for derivation.

```
In [6]:
         ft win = np.fft.fft(sig[0:1000])
            plt.figure(figsize=(12,8))
            plt.subplot(3,1,1)
            plt.plot(freqs_win, ft_win.real, '-o')
            plt.xlim([-50,50]); plt.ylabel('Real Component')
            plt.subplot(3,1,2)
            plt.plot(freqs win, ft win.imag, '-o')
            plt.xlim([-50,50]); plt.ylabel('Imaginary Component')
            plt.subplot(3,1,3)
            plt.plot(freqs_win, abs(ft_win)**2, '-o')
            plt.xlim([-50,50]);
            plt.xlabel('Frequency(Hz)'); plt.ylabel('Power');
            # print a few pairs just to see that it's true
            print(ft_win[10], ft_win[-10])
            print(ft_win[20], ft_win[-20])
            print(ft_win[100], ft_win[-100])
            (187.99436742034507+244.66949839282594j) (187.9943674203451-244.66949839282591
            j)
            (0.970857231288467-21.998168671646166j) (0.9708572312884642+21.99816867164617
            j)
```

(0.9999834335126278-3.113229835816976j) (0.9999834335126241+3.113229835816978 j)



If you recall, in A2, you were asked to compute the frequency in Hz from the wave numbers, k. There was a bonus question to make your frequencies match np.fft.fftfreq(), as that function returns Loading [MathJax]/extensions/Sale_ist uencies after fs/2 . fs/2 is also known as Nyquist frequency, the fastest frequency

you can resolve given a sampling rate of fs (not to be confused with Nyquist rate, which is the minimum sampling rate, 2B, required to accurately capture a signal with a maximum frequency of B).

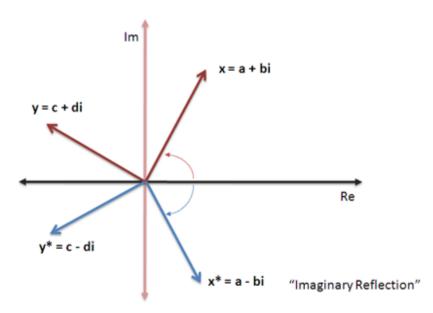
In addition, you were asked to plot the real and imaginary component of the Fourier Transform. I didn't make a comment on it then, but you may have noticed something a little funny, and again in the plots above as you plot the power spectra before zooming into 0 to 50Hz. In the cell above, I plot the real and imaginary components of the FT, and power spectrum you computed in Q1.1, zooming into -50 to 50Hz instead.

Notice that in the first plot (real component), the dots are symmetric about 0Hz, as if they are mirrored. The imaginary components (second plot), on the other hand, are anti-symmetric - mirrored but flipped about 0Hz. This means that for any frequency and its negative, their Fourier coefficients form a conjugate pair (symmetric about the real number line). As a byproduct, since the power is just the power squared magnitude of the vectors, it's also symmetric, while the phase (not plotted) are again anti-symmetric. This is a property of the DFT when applied to **real-valued signals**. We will go through the details in lecture, but for a formal proof, see here

(https://dsp.stackexchange.com/questions/8715/symmetry-of-real-and-imaginary-parts-in-fft).

Practically, what this means is that half of the Fourier transform for a real-valued signal (the only kind you will work with in this class) is redundant. We can simply reconstruct the negative half from the positive half by inverting the imaginary component (or phase). This will become relevant in Q3, where I return for you only the positive halves of the Fourier coefficients, up to fs/2, as that's the last (fastest) positive frequency represented.

Complex Conjugates



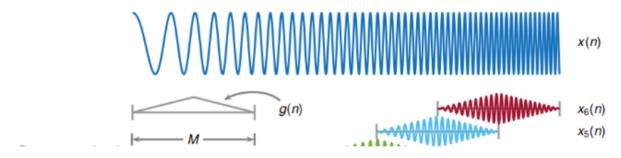
In the diagram above, the complex vectors \mathbf{x}^* and \mathbf{x}^* represent the complex coefficients at one frequency and its negative, while \mathbf{y}^* and \mathbf{x}^* are another pair of frequencies. Diagram from here (https://betterexplained.com/articles/intuitive-arithmetic-with-complex-numbers/).

Okay, back on track. Q1 should have demonstrated to you that simply taking a power spectrum is not sufficient for some signals. In particular, when a signal violates stationarity, it may have frequency content that changes over time. This is **important**, as most signals in nature are NOT stationary. It would be like taking an average of all the frames in a movie to see what the movie is about.

How do we overcome this? Using **Short Time Fourier Transforms (STFT)**. The principle behind this method is already demonstrated in the last part of Q1. Instead of taking one big Fourier transform across time, STFT takes snippets of the signal to measure its frequency content over time, giving us both frequency and time resolution (hence the name, time-frequency analysis).

Instead of picking two arbitrary time windows, however, STFT does this more systematically. Specifically, it's parameterized by two additional parameters: window length (len_win), which corresponds to the length of the small window of data you want to compute over, and step length (len_step), which corresponds to how much you step forward to compute the FT of the next window. In the diagram below, len_win =M, and len_step =R.

Instead of step length, some implementations use the parameter overlap length (len_overlap), which is how much the next window overlaps with the current one (L in diagram). This is simply the complement of R, i.e., L = M-R. This is what scipy.signal.stft() uses, so we will adopt that as well to minimize confusion.



(Image from MATLAB (https://www.mathworks.com/help/signal/ref/stft.html))

Below, we will walk through the steps of constructing the STFT yourself. I will first ask you some math questions to consolidate the concept, then guide you through implementing the operation in code.

[8] Q2: Step By Step

There's really nothing fancy about the STFT: forget about the Fourier transform part for a second. The fundamental component (and difference to the regular FT) is the stepping operation, taking a window (or chunk) of your data at regularly sized intervals - that's all! This operation is exactly analogous to what you did in A1 to find trial indices for ERPs, except at a regular interval. However, instead of acquiring the time indices from the experiment itself, you will compute them based on the parameters of the STFT.

- [1] 2.1: In Q1.5, we took a 1-second window of data, which is 1000-points (since fs=1000 Hz). If we were to compute the STFT, how many windows would the entire signal be divided into with no overlap? (Remember, T=20 seconds)
- [1] 2.2: What would be the timestamp (in seconds) of the zeroth data point in the 10th, 11th. and 12th window?
- [1] 2.3: What would be the corresponding array indices (in terms of the full data array) of those points from Q2.2? What is the formula you used to compute this?
- [1] 2.4: If now we want to overlap each window by 0.5 seconds (500 data points), how many **full** windows would we end up with? What would be the time index of the zeroth data point in the 10th, 11th, and 12th window then?
- [1] 2.5: What would be the array index (in terms of the full data array) of those points in Q2.4?

Response for 2.1: 20

Response for 2.2: 10, 11, 12

Response for 2.3: 10000, 11000, 12000. timestamp*fs

Response for 2.4: 39. 5, 5.5, 6

Response for 2.5: 5000, 5500, 6000

- [1] 2.6: Complete the function <code>slide_window_time()</code> below, which returns an array that contains the zeroth timestamp of every window. E.g., if <code>len_win=1s</code> and <code>len_win=0.5s</code>, the first 3 elements of the array should be [0., 0.5, 1.0 ...]. Note that the last timestamp should be the start of a valid (full) data window, i.e., it has to be at least <code>len_win</code> less than the total signal time, <code>T</code>. Hint: one easy way to do this is to call <code>np.numpy()</code>, and throw out all the times values that cross into the last window.
- [1] 2.7: Complete the function slide_window_index() below, which returns an array (of integers) that contains index of the zeroth data point of each window. E.g., if len_win=1s and len_win=0.5s, the first 3 elements of the array should be [0, 500, 1000 ...]. Note that it requires an additional argument, fs. Again, you can do this by stepping through as you do in 2.6, or just use the output of slide window time().
- [1] 2.8: Use the above two functions to confirm your response for Q2.2-2.5. t_stft should store the array of timestamps, while ind_stft, indices.

```
    def slide window time(T,len win,len overlap):

       # T is total signal time, len win is window length in seconds, len overlap
       # YOUR CODE HERE
       t steps = np.arange(0,T,len win-len overlap)
       return t steps[t steps<=(T-len win)] #removes nonfull windows</pre>
   def slide window index(T,fs,len win,len overlap):
       # YOUR CODE HERE
       return np.round(slide window time(T,len win,len overlap)*fs)
   # 02.2-3
   len win = 1 # seconds
   len overlap = 0 # seconds
   t stft = slide window time(T, len win, len overlap)
   ind stft = slide window index(T, fs, len win, len overlap)
   print(len(t_stft)) # print the number of windows
   print(t_stft[10:13], ind_stft[10:13]) # print the zeroth timestamps and correst
   # 02.4-5
   len win = 1 # seconds
   len_overlap = 0.5 # seconds
   t stft = slide window time(T, len win, len overlap)
   ind_stft = slide_window_index(T, fs, len_win, len_overlap)
   print(len(t stft)) # print the number of windows
   print(t_stft[10:13], ind_stft[10:13]) # print the zeroth timestamps and correst
  20
   [10 11 12] [10000 11000 12000]
   [5. 5.5 6. ] [5000. 5500. 6000.]
```

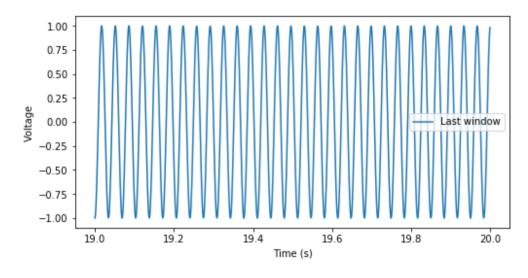
[2] Q3: Short-Time Fourier Transform

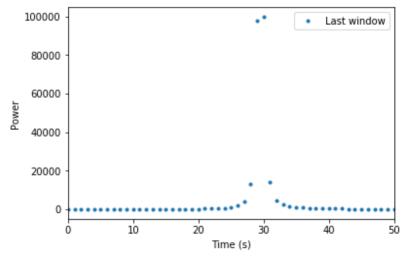
At this point, you have an array of data indices in <code>ind_stft</code>, which represents the index of the first data point of every window. The next step is very similar to what you did for computing an ERP: grab a window of data around those indices. Only it's even simpler here: you don't grab any data before that index, since it's the start of the window, and you grab <code>len_win</code> seconds worth of data following.

- [1] 3.1: Using array indexing and the values stored in ind_stft from Q2.5 (len_win=1 & len_overlap=0.5), grab the last data window, which should be win_len long. Store that in the variable data_win. Do the same for the time indices (from t), and store it in t_win. Plot that window of data against its time indices. (Hint: it should start at t=19.)
- [1] 3.2: Compute it's FT using numpy.fft.fft(), and plot the power spectrum. It should look the same as your (orange) trace from Q1.6.

```
In [8]:
         ▶ # grab a window of the signal and the corresponding time vector
            sig win = sig[int(ind stft[-1]):]
            t_win = t[int(ind_stft[-1]):]
            # plot time series window
            plt.figure(figsize=(8,4))
            # YOUR CODE HERE
            plt.plot(t win, sig win, label = 'Last window')
            plt.xlabel('Time (s)'); plt.ylabel('Voltage')
            plt.legend()
            # compute power spectrum
            fft = np.fft.fft(sig win)
            # plot power spectrum
            plt.figure(figsize=(6,4))
            #_YOUR_CODE_HERE
            plt.plot(freqs_win, abs(fft)**2,'.', label = 'Last window')
            plt.xlabel('Time (s)'); plt.ylabel('Power')
            plt.xlim([0,50])
            plt.legend()
```

Out[8]: <matplotlib.legend.Legend at 0x235c1695780>





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[3] 3.3: The last two steps guides you on how to grab a single time window given it's starting index and compute the Fourier transform (and power spectrum). Complete the function <code>my_stft()</code> below, which should iterate over all window-start indices and grab the corresponding window of data and compute each Fourier Transform. Use the functions you've built previously.

You need to return 3 output arguments: f_stft , the corresponding frequency axis for the STFT; t_stft , the time stamps for the zeroth data point of each window; and stft, the short time Fourier transform (2D matrix). stft should have shape ($len(f_stft)$), $len(t_stft)$). Note here f_stft and stft should contain only the positive frequencies (I actually do that for you in the function, assuming you computed the variables correctly).

You can either loop through the time series and compute the Fourier transform of each window and store that in a matrix, or collect all the time series data in one go, and call <code>np.fft.fft()</code> once - it will perform a 1-dimensional FFT along the axis specified.

- [1] 3.4: Compute the spectrogram from the STFT, which is the squared magnitude of every value in STFT. Store that in spg.
- [1] 3.5: Plot the spectrogram you have computed using the helper function plot_spectrogram(). Set freq_lims to [0,50] Hz. I plot the spectrogram generated using signal.spectrogram for you, they should look identical.
- [1] 3.6: Comment on the spectrogram and what you can interpret from it about the signal.
- [2] 3.7: Compute the power spectral density (PSD) from your spectrogram spg , as well as scipy's spectrogram spg_sp and plot them. They should look identical. Remember to label the traces and the axes appropriately. Note: don't worry about the normalization for spectral density for now, just take the average over time.

Response for 3.6: The spectrograms show that the frequency increases with time so if it is a brain wave, that area is getting more strongly activated over time. It could also be increasing from noise through sweat conduction during an EEG.

```
In [9]: M

def my_stft(data, fs, len_win, len_overlap):
    T = len(data)/fs #_YOUR_CODE_HERE
    inds_stft = slide_window_index(T,fs,len_win,len_overlap) #_YOUR_CODE_HERE
    t_stft = inds_stft/fs #_YOUR_CODE_HERE #avoids redoing method
    #did len to get total number of data point since freq points is same amount
    f_stft = np.fft.fftfreq(int(len(np.fft.fft(data,fs))*len_win), 1/fs) #_YOUR_
    #cast to get indices for data window. Transposed to make it fit
    stft = np.fft.fft([data[int(x):int(x)+int(len_win*fs)] for x in inds_stft]))

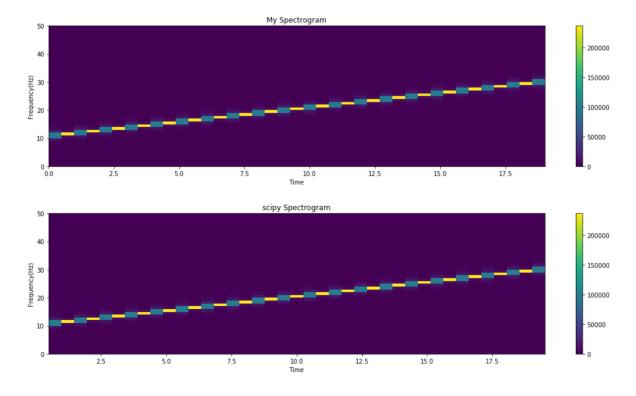
# print(len(f_stft), len(t_stft), stft.shape)
# clip the frequency axis to return just the non-negative frequencies
# np.fft.fftfreq returns the nyquist frequency as negative, which we also not positive_fs = np.logical_or(f_stft>=0, f_stft==-fs/2)

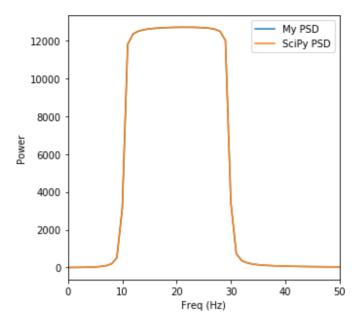
# I return for you just the positive frequencies
    return abs(f_stft[positive_fs]), t_stft, stft[positive_fs,:]
```

```
In [10]:
          N len win = 1.
             len overlap = 0.5
             # computing and plotting your spectrogram
             f stft, t stft, stft = my stft(sig,fs,len win,len overlap) # YOUR CODE HERE
             print(len(f_stft), len(t_stft), stft.shape) # print the shape of the STFT to col
             spg = abs(stft)**2 # YOUR CODE HERE
             plot spectrogram(spg, t stft, f stft, freq lims=[0,50], plot db=False)
             plt.title('My Spectrogram')
             # I compute the spectrogram using scipy and plot it for you
             f_sp, t_sp, spg_sp = signal.spectrogram(sig, fs, window='rect', nperseg=int(fs*)
             # I undo scipy's normalization for you so they will look the same
             spg_sp = spg_sp*fs**2*len win/2
             plot_spectrogram(spg_sp, t_sp, f_sp, freq_lims=[0,50], plot_db=False)
             plt.title('scipy Spectrogram');
             # computing and plotting your PSDs
             plt.figure(figsize=(5,5))
             # YOUR CODE HERE
             plt.plot(f stft, np.array([(x.real**2 + x.imag**2).mean() for x in stft]), label
             plt.plot(f_sp, np.array([x.mean() for x in spg_sp]), label = 'SciPy PSD')
             plt.legend()
             plt.xlim([0,50])
             plt.xlabel('Freq (Hz)'); plt.ylabel('Power')
```

501 39 (501, 39)

Out[10]: Text(0,0.5,'Power')





Now let's try it on some real brain signals

We'll be working with the same LFP data as last time, recorded in the rat hippocampus. This dataset comes from an openly accessible neuroscience database. For more information on this particular dataset, see here (https://crcns.org/data-sets/hc/hc-2/about-hc-2).

We will use a slightly longer snippet of data to start (1fp_short , 2min), for the purpose of demonstrating the spectrogram.

```
In [11]:
             data = io.loadmat('./data/LFP.mat', squeeze me=True)
             print(data.keys())
             # unpack the variables
             fs = data['fs'] # sampling rate
             print('Sampling rate = %iHz'%fs)
             lfp = data['lfp'][0,:]/1000 # this file contains two channels, we'll only work w
             lfp short = lfp[:int(120*fs)] # make a variable that has only the first two second
             t_short = np.arange(0, len(lfp_short)/fs, 1/fs) # create the corresponding time
             plt.figure(figsize=(15,3))
             plt.plot(t_short,lfp_short, 'k', alpha=0.8)
             plt.xlim([0,10])
             plt.xlabel('Time (s)');plt.ylabel('Voltage');
             dict_keys(['spike_fs', '__globals__', 'lfp', '__header__', '__version_
             ke_indices', 'fs'])
             Sampling rate = 1250Hz
```

[6 + 2 Bonus] Q4: Applying STFT & PSD

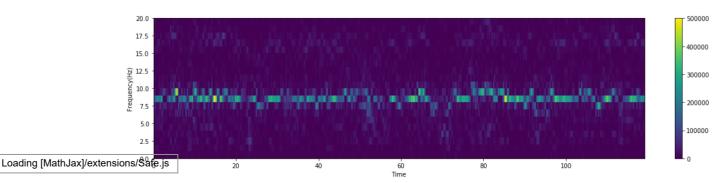
- [3] 4.1: **Using a window length of 1s, and overlap of 0.8s**, compute the STFT (using my_stft), spectrogram (**normalized/spectral density**), and PSD. Plot the spectrogram and PSD. I compute the PSD using sp.signal for you in f_welch and p_welch. Plot that to confirm you have the right answer (the PSDs should overlap). Zoom into 0 to 20Hz for both the spectrogram and PSD.
- [1] 4.2: Repeat the above analyses and plots in a new cell, but **using a window length of 5s, and overlap of 4s**. You can literally copy and paste the entire block of code, changing just the variable values for len win and len overlap.
- [2] 4.3: Discuss similarities and differences for two spectrograms, especially with respect to temporal and frequency resolution. Also compare the two sets of PSDs, noting the frequency content of the signal represented in both cases.
- [BONUS: 2] 4.4: There is a known cause for the change in frequency for this neural oscillation in rats. What is the name of this oscillation, and what is the cause for the frequency change? Reference your source here.

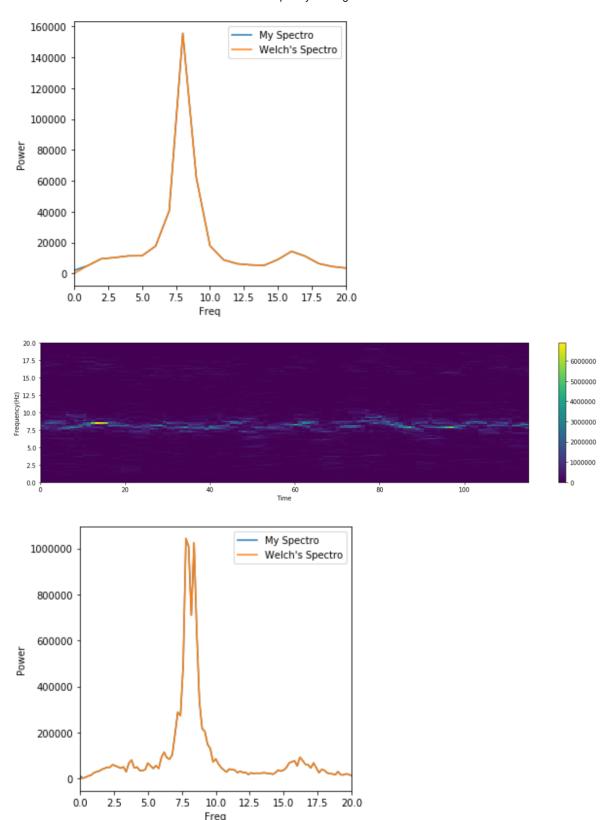
Response for 4.3: They show similar frequencies contribute to the power but have differing time and frequency resolutions. As the time window increased from 1 to 5s, the spectrogram got harder to tell but the PSD showed more finely the frequencies that had the most power.

Response for 4.4: Gamma to Beta frequency shift caused by information processing. Referenced from "On the Mechanism of the gamma to beta Frequency Shift in Neuronal Oscillations Induced in Rat Hippocampal Slices by Tetanic Stimulation" by Roger D. Traub, Miles A. Whittington, Eberhard H. Buhl, John G. R. Jefferys, and Howard J. Faulkner.

```
In [12]:
          ▶ len win = 1 #1,5 # YOUR CODE HERE
             len overlap = 0.8 #0.8,4 # YOUR CODE HERE
             f stft, t stft, stft = my stft(lfp short,fs,len win,len overlap)
             spg = abs(stft)**2# YOUR CODE HERE
             psd = np.array([(x.real**2 + x.imag**2).mean() for x in stft]) # YOUR CODE HERE
             # use plot spectrogram
             plot spectrogram(spg, t stft, f stft, plot db=False, freq lims=[0,20])
             # computing welch's spectrogram for you
             f welch, p welch = signal.welch(lfp short,fs,window='boxcar',nperseg=int(fs*len
             # p welch *= 0.5*len win # again, undoing scipy's normalization
             p welch = p welch*fs**2*len win/2
             # plot the PSDs
             plt.figure(figsize=(5,5))
             plt.plot(f stft,psd, label='My Spectro')
             plt.plot(f_welch, p_welch, label='Welch\'s Spectro')
             plt.xlim([0,20])
             plt.xlabel('Freq'); plt.ylabel('Power')
             plt.legend()
             #_YOUR_CODE_HERE
             ######### 5 and 4
             len win = 5 #1,5 # YOUR CODE HERE
             len overlap = 4 #0.8,4 # YOUR CODE HERE
             f stft, t stft, stft = my stft(lfp short,fs,len win,len overlap)
             spg = abs(stft)**2#_YOUR_CODE_HERE
             psd = np.array([(x.real**2 + x.imag**2).mean() for x in stft]) #_YOUR_CODE_HERE
             # use plot spectrogram
             plot_spectrogram(spg, t_stft, f_stft, plot_db=False, freq_lims=[0,20])
             # computing welch's spectrogram for you
             f welch, p welch = signal.welch(lfp short,fs,window='boxcar',nperseg=int(fs*len
             # p welch *= 0.5*len win # again, undoing scipy's normalization
             p welch = p welch*fs**2*len win/2
             # plot the PSDs
             plt.figure(figsize=(5,5))
             plt.plot(f_stft,psd, label='My Spectro')
             plt.plot(f_welch, p_welch, label='Welch\'s Spectro')
             plt.xlim([0,20])
             plt.xlabel('Freq'); plt.ylabel('Power')
             plt.legend()
```

Out[12]: <matplotlib.legend.Legend at 0x235c1871208>





Intermission & scipy.signal

Q4 is an example of what practical (neural) signal processing is about: making informed parameter decisions based on your data and the question you want to answer. We've covered most of the math details already, so from this point on, the labs will shift focus from implementing the analysis toolkits to applying them and making sound judgements for your analysis parameters.

In the exercises above, I call functions from the scipy.signal module to check your answers for you, which has most of the functions relevant for digital signal processing, especially for this class. As we progress through more complex material, you will be asked to use them directly to speed things up, and certainly for your final project, so it's important to be familiar with the documentation for them. To view documentation, put your cursor inside the brackets of the function call in a code cell, and press shift+tab+tab.

In particular, the following functions are relevant for you for this lab:

- signal.stft():computing STFT
- signal.welch(): computing PSD using STFT with optional overlapping windows
- signal.windows: a sub-module that contains windowing functions
- signal.firwin(): computing FIR filter coefficients
- signal.hilbert(): computing the Hilbert transform

Note: most of the functions above take in the **number of points** as it's length arguments, such as nperseg (number of data points per window) and noverlap. We still want to define our length parameters in units of seconds because that's more intuitive, so take note to convert them to number of points (and they have to be integers) by multiplying by the sampling rate.

[6] Q5: Windowing & PSD

This question illustrates how windowing with different window functions can give rise to slightly different spectral estimates. As a reminder, windowing is multiplying your short-time data segments with a windowing function, and is done regardless whether you perform it explicitly (in that case, a "boxcar" window is equivalently used). This is equivalent to convolving the "true" signal power spectrum with the spectral profile of the window.

- [1] 5.1: Since all the scipy.signal functions specify window length in terms of points, complete the function secs_to_points that converts the length variables in time (len_win, len_overlap) to number of points. Remember to return ints. We will still specify parameters in units of second, but convert them to points before using for scipy calls from this point on.
- [1] 5.2: With window length of 2s and overlap length of 1s, compute the PSD using signal.spectrogram() by averaging the spectrogram, as well as using signal.welch(), specifying fs, nperseg, and noverlap from above. Plot the two PSDs and zoom into 0-30Hz. They should **not look identical**, and I print the percentage difference at the maximum point for you, it should be around 3.49%.
- [1] 5.3: Find the default windows used signal.welch() and signal.spectrogram(). Create them both using signal.windows, where n=nperseg, and plot them.
- [1] 5.4: Estimate their spectral response by simply taking the squared magnitude of their Fourier Transform. Plot them in frequency domain and zoom into [-5, 5] Hz. Remember to label the traces and the axes for this and the above plots!

[2] 5.5: Describe the differences between the two spectral responses. In particular, note the height of the center point, and the main lobe. Is this consistent with the differences in the PSD estimates from Q5.2? Why or why not? Hint: convolution.

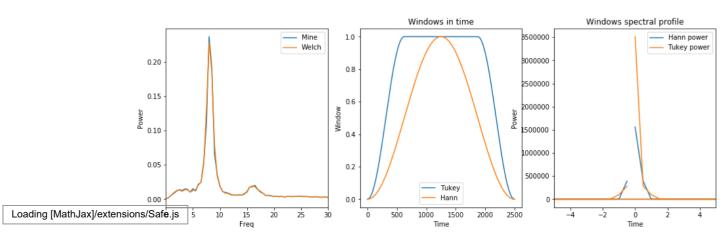
Response for 5.5: No, it is not consistent since they differed by about 3.5% and the Tukey's peak is over 100% larger than that of Hann's. This is probably caused by differing IRF's leading to largely differing powers.

```
In [13]:

    def secs to points(fs, len win, len overlap):

                 nperseg = int(len_win*fs) # YOUR CODE HERE
                 noverlap = int(len overlap*fs) # YOUR CODE HERE
                 return nperseg, noverlap
             nperseg, noverlap = secs_to_points(fs, len_win=2, len_overlap=1)
             f spg, t spg, spg = signal.spectrogram(lfp short,fs,nperseg=nperseg,noverlap=nov
             p spg = [x.mean() for x in spg] # YOUR CODE HERE for computing your PSD
             f_welch, p_welch = signal.welch(lfp_short,fs,nperseg=nperseg,noverlap=noverlap)
             print(100*(p spg[16]-p welch[16])/p welch[16])
             plt.figure(figsize=(15,5))
             plt.subplot(1,3,1)
             # YOUR CODE HERE for plotting PSDs
             plt.plot(f_spg,p_spg, label="Mine")
             plt.plot(f welch,p welch,label = 'Welch')
             plt.xlabel('Freq'); plt.ylabel('Power')
             plt.legend()
             plt.xlim([0,30])
             win_tukey = signal.tukey(nperseg)#_YOUR_CODE_HERE
             win hann = signal.hann(nperseg)# YOUR CODE HERE
             plt.subplot(1,3,2)
             # YOUR CODE HERE for plotting windows
             plt.plot(win tukey, label="Tukey")
             plt.plot(win_hann, label= 'Hann')
             plt.xlabel('Time'); plt.ylabel('Window')
             plt.legend(); plt.title('Windows in time')
             freq = np.fft.fftfreq(nperseg,1/fs)
             power hann = abs(np.fft.fft(win hann,n=nperseg))**2
             power tukey = abs(np.fft.fft(win tukey,n=nperseg))**2
             plt.subplot(1,3,3)
             # YOUR CODE HERE for plotting windows in frequency
             plt.plot(freq,power_hann, label='Hann power')
             plt.plot(freg,power tukey, label = "Tukey power")
             plt.xlabel('Time'); plt.ylabel('Power')
             plt.xlim([-5,5])
             plt.legend(); plt.title('Windows spectral profile');
```

3.4914214629796034



[8 + 2 Bonus] Q6: Coherence

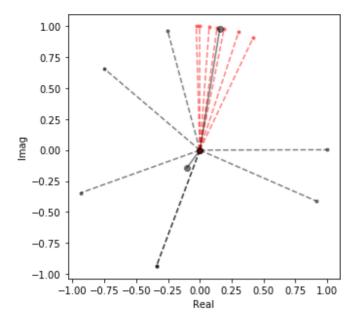
Now we will look at inter-trial coherence: in this experiment, the rat is freely running around. At some points, there will be events that prompts it to do something, or be given a reward, similar to the stimulus in the ERP experiment. I have given you the time points of those events in t_trials. We will look at how stimulus in those trials affect the strong rhythm we saw in the PSD, at 8.5Hz.

- [1] 6.1: Compute the STFT using signal.stft, using a 'hann' window.
- [1] 6.2: We will be looking at the coherence of the dominant oscillation, which is about 8.5Hz. Find the index of the frequency vector where it equals to 8.5Hz. Equivalently, compute the wave number k for the 8.5Hz oscillation. 8.5Hz.
- [1] 6.3: To start, we will look at the coherence of 7 random trials. This is often done to establish a null for what to expect by chance. You will notice that the individual complex vectors (dashed) have different lengths. To compute coherence, which we will define to be the magnitude (length) of the averege complex vector, we want to remove the effect of individual trial powers. In the for loop, add a line to normalize the complex coefficient of each trial, X_trial, by its length. Do the same for the average, X_mean.
- [1] 6.4: Compute and print the coherence value. Again, we define that here as the magnitude of the average **length-normalized** vector. This should be around 0.1765.
- [1] 6.5: Repeat the analyses for the real trials, given the trial times t_trials. This is similar to what you did for the ERP analysis. To make your life easier, these trial times can be matched exactly to the STFT window times. Your first task is to find the STFT indices (in the time dimension) that correspond to these trial times. Store that in trial inds.
- [2] 6.6: Repeat the plotting and coherence computation in Q7.3-4, but using the trial indices you just found. Plot these in the same figure, but in red. (Just change the $\,k$ in 'k.--' to r). Don't forget the normalization. The single trial vectors should be cluster around pi/2, and the coherence value should be very high (0.988).
- [BONUS: 2] 6.7: Repeat 6.5-6, but for the STFT window immediately before the onset of the trial. This should allow you to compute the *change* in coherence.
- [1] 6.8: What is your interpretation of this result, in the context of the experiment? i.e., how does the stimulus affect the oscillation, compared to the randomly chosen time windows?

Response for 6.8: The stimulus affects the oscillation which is shown through the resulting averaged vector at the end. In the randomized sample, the vector was almost zeroed out. However, when it was not randomized, the averaged vector had a large magnitude due to the vectors all going in the same directions showing that it does have an effect.

```
In [14]:
          ₩ # Trial times
             t trials = np.array([6., 22., 45., 63., 78., 111., 118.])
             # Use these Length settings for STFT
             nperseg, noverlap = secs to points(fs, len win=2, len overlap=1)
             # compute stft
             f stft, t stft, stft = signal.stft(lfp short,fs, nperseg=nperseg, noverlap=nove
             # find the index (k) of 8.5Hz.
             f ind = np.where(f stft==8.5)[0]# YOUR CODE HERE
             # grab random slices of the STFT to compute coherence
             np.random.seed(0)
             trial inds = np.random.randint(0,len(t stft), size=len(t trials))
             plt.figure(figsize=(5,5))
             plt.xlabel('Real'); plt.ylabel('Imag')
             vectors = 0
             # plot all trial vectors
             for trial_ind in trial_inds:
                 X trial = stft[f ind, trial ind].squeeze()
                 # normalize by vector length
                 X_trial = X_trial/np.abs(X_trial)#_YOUR_CODE_HERE
                 vectors = X trial+vectors
                 plt.plot([0,X_trial.real], [0, X_trial.imag], 'k.--', alpha=0.5)
             # plot mean vector
             X mean = vectors/len(t trials)# YOUR CODE HERE
             plt.plot([0,X_mean.real], [0, X_mean.imag], 'ko-', alpha=0.5)
             coherence = abs(X mean)# YOUR CODE HERE
             print(coherence)
             # ----- now do it for real -----
             # get trial indices from trial times
             trial_inds = [np.where(x==t_stft)[0][0] for x in t_trials]#_YOUR_CODE_HERE
             vectors = 0
             for trial_ind in trial_inds:
                 X trial = stft[f ind, trial ind].squeeze()
                 # normalize by vector length
                 X trial = X trial/np.abs(X trial)# YOUR CODE HERE
                 vectors = X_trial+vectors
                 plt.plot([0,X_trial.real], [0, X_trial.imag], 'r.--', alpha=0.5)
             # plot mean vector
             X_mean = vectors/len(t_trials)#_YOUR_CODE_HERE
             plt.plot([0,X mean.real], [0, X mean.imag], 'ko-', alpha=0.5)
             coherence = abs(X_mean)#_YOUR_CODE_HERE
             print(coherence)
```

```
Loading [MathJax]/extensions/$4765326643025391
```



FIR Filtering & Filter Response

There are 4 types of filters: lowpass, highpass, bandpass, and bandstop. They refer to the frequency response of the filter, e.g., lowpass means to allow low frequencies through (from 0Hz to the cutoff) and filter out high frequencies, the opposite for highpass. Bandpass allows through a narrow band frequency and filters out the rest, while bandstop does the opposite, which is commonly used for filtering out a specific frequency of noise (such as 60Hz line noise). Filter design is an art that will take many such labs to cover extensively, so we will just introduce the idea here and give you the tools to explore that at a later stage (such as for your project).

Finite Impulse Response

The filter response can be examined in both time and frequency domain. If we plot the coefficients of an FIR filter in time, that's quite literally its impulse response function, i.e., if you tried to filter a delta with this function, it will output itself. FIR stands for finite impulse response, which means the impulse response function has finite time. Infinite impulse response (IIR) filters, on the other hand, have feedback, and thus will continue out to infinity even for a single delta input. We will only be using FIR filters for this course.

signal.firwin()

A quick tutorial on signal.firwin(): this function designs the FIR filter based on your frequency requirements, and return the filter coefficients. The 4 critical parameters are numtaps, fs, cutoff, and pass_zero.

- numtaps is the filter "order", basically, how many points are in the filter. The longer the filter is, the better frequency resolution you will have, but worse temporal resolution.
- fs is the sampling rate of your signal
- · cutoff defines the frequency to pass/block
- pass_zero defines whether 0Hz is passed or blocked

cutoff and pass_zero , in conjunction, defines the filter type. If your cutoff is at 20Hz and define pass_zero=True , then firwin() interprets that to be a lowpass filter. If pass_zero=False , then it's a highpass filter. Same idea applies to bandpass and bandstop, except cutoff is now required to be a tuple.

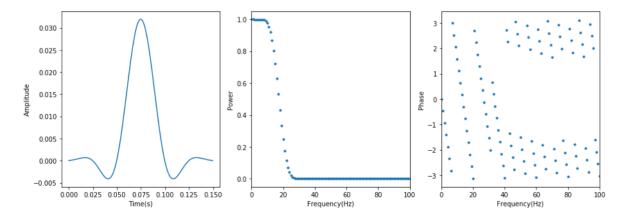
np.convolve()

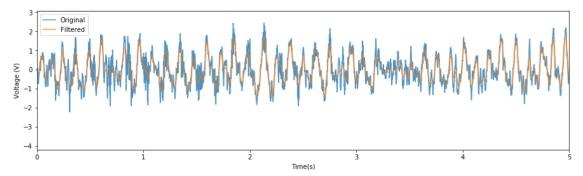
Finally, to apply the filter, we simply convolve the signal with the filter, using <code>np.convolve()</code>. Remember, convolution in time domain is multiplication in frequency domain, and actually, I believe <code>np.convolve()</code> is implemented via FFT and multiplication in the frequency domain.

Below, I will demonstrate an example of a lowpass filter, plotting its IRF in time and frequency.

```
cutoff = 20 #Hz
In [15]:
             # we typically want a filter order to be at least as long as 3 periods (cycles)
             # the slowest frequency in the cutoff.
             # so if cutoff is 20Hz, we want 3*0.05s = 0.15s long, which is 0.15*fs points
             # the larger this number is, the better frequency resolution you will have
             filt order = int(3*fs/cutoff)+1
             filt coefs = signal.firwin(filt order, cutoff, fs=fs, pass zero=True)
             # compute the magnitude and phase response of the filter
             freq resp = np.fft.fft(filt coefs, n=int(fs))
             mag resp = abs(freq resp)**2
             ph resp = np.angle(freq resp)
             freqs = np.fft.fftfreq(int(fs),1/fs)
             plt.figure(figsize=(15,5))
             plt.subplot(1,3,1)
             # plot impulse response
             t filt = np.arange(0,len(filt coefs))/fs
             plt.plot(t filt,filt coefs)
             plt.xlabel('Time(s)'); plt.ylabel('Amplitude');
             plt.subplot(1,3,2)
             plt.plot(freqs, mag_resp, '.')
             plt.xlabel('Frequency(Hz)'); plt.ylabel('Power');
             plt.xlim([0,100])
             plt.subplot(1,3,3)
             plt.plot(freqs, ph resp, '.')
             plt.xlabel('Frequency(Hz)'); plt.ylabel('Phase');
             plt.xlim([0,100])
             plt.figure(figsize=(15,4))
             lfp filt = np.convolve(lfp short, filt coefs, mode='same')
             plt.plot(t_short, lfp_short, alpha=0.8, label='Original')
             plt.plot(t short, lfp filt, alpha=0.8, label='Filtered')
             plt.xlim([0,5])
             plt.legend()
             plt.xlabel('Time(s)');plt.vlabel('Voltage (V)')
```

Out[15]: Text(0,0.5,'Voltage (V)')





[4 + 1 Bonus] Q7: Filter Decisions

Following the template from above, do the following:

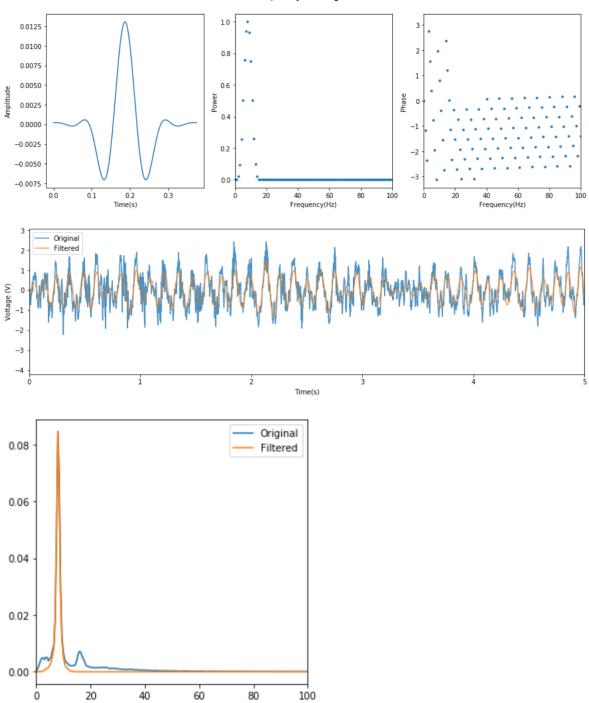
- construct filter coefficients using signal.firwin()
- plot the IRF in time and frequency domain (both magnitude and phase)
- filter the lfp signal using np.convolve, and plot both signals in time (zoom into first 5 seconds)
- plot the power spectrum of both the original and filtered signal. (I didn't do this for you)
- [1] 7.1: a band-pass filter, with cut-off between 4-12Hz.
- [1] 7.2: a band-stop filter, with cut-off between 4-12Hz.
- [1] 7.3: a high-pass filter, with a cut-off at 0.1Hz.
- [1] 7.4: Which of the above is most suitable for isolating (keeping) the dominant frequency in the LFP.

[BONUS 1] 7.5: since you will be doing the same sequence of operations above multiple times, it's useful to think about how to construct them into functions. You will be rewarded 2 bonus points if, after your function definition, each of the points above is completed in one line of code (to your function call).

Response for 7.4: The band-pass filter is the best based on how much of the power it contained.

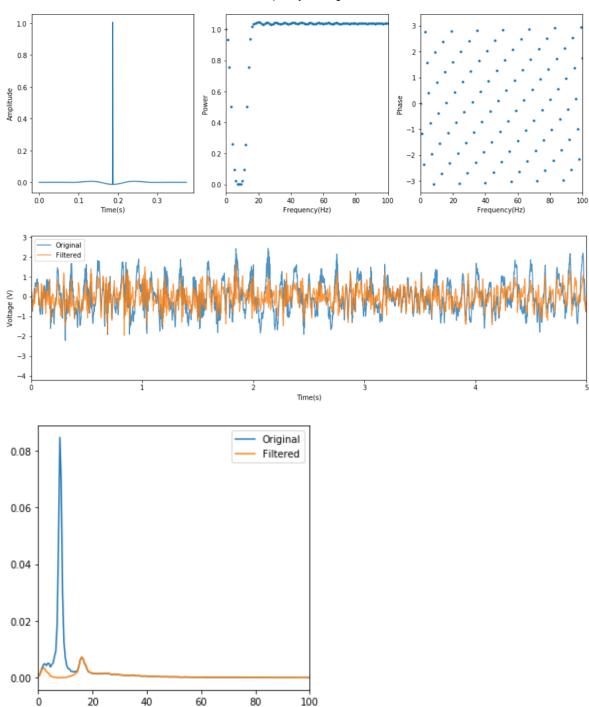
```
In [16]:
          # Code for 7.1-3. You can use more than one cell.
             #########7.1
             cutoff = (4,12) #Hz
             # we typically want a filter order to be at least as long as 3 periods (cycles)
             # the slowest frequency in the cutoff.
             # so if cutoff is 20Hz, we want 3*0.05s = 0.15s long, which is 0.15*fs points
             # the larger this number is, the better frequency resolution you will have
             filt order = int(3*fs/(cutoff[1]-cutoff[0]))+1
             filt coefs = signal.firwin(filt order, cutoff, fs=fs, pass zero=False)
             # compute the magnitude and phase response of the filter
             freq resp = np.fft.fft(filt coefs, n=int(fs))
             mag resp = abs(freq resp)**2
             ph resp = np.angle(freq resp)
             freqs = np.fft.fftfreq(int(fs),1/fs)
             plt.figure(figsize=(15,5))
             plt.subplot(1,3,1)
             # plot impulse response
             t filt = np.arange(0,len(filt coefs))/fs
             plt.plot(t_filt,filt_coefs)
             plt.xlabel('Time(s)'); plt.ylabel('Amplitude');
             plt.subplot(1,3,2)
             plt.plot(freqs, mag_resp, '.')
             plt.xlabel('Frequency(Hz)'); plt.ylabel('Power');
             plt.xlim([0,100])
             plt.subplot(1,3,3)
             plt.plot(freqs, ph resp, '.')
             plt.xlabel('Frequency(Hz)'); plt.ylabel('Phase');
             plt.xlim([0,100])
             plt.figure(figsize=(15,4))
             lfp_filt = np.convolve(lfp_short, filt_coefs, mode='same')
             plt.plot(t_short, lfp_short, alpha=0.8, label='Original')
             plt.plot(t short, lfp filt, alpha=0.8, label='Filtered')
             plt.xlim([0,5])
             plt.legend()
             plt.xlabel('Time(s)');plt.ylabel('Voltage (V)')
             filt_f_stft, filt_t_stft, filt_stft = signal.stft(lfp_filt,fs, nperseg=nperseg,
             plt.figure(figsize= (5,5))
             plt.plot(f_stft,np.array([(x.real**2 +x.imag**2).mean() for x in stft]),label='(
             plt.plot(filt f stft,np.array([(x.real**2 +x.imag**2).mean() for x in filt stft]
             plt.legend()
             plt.xlim([0,100])
```

Out[16]: (0, 100)



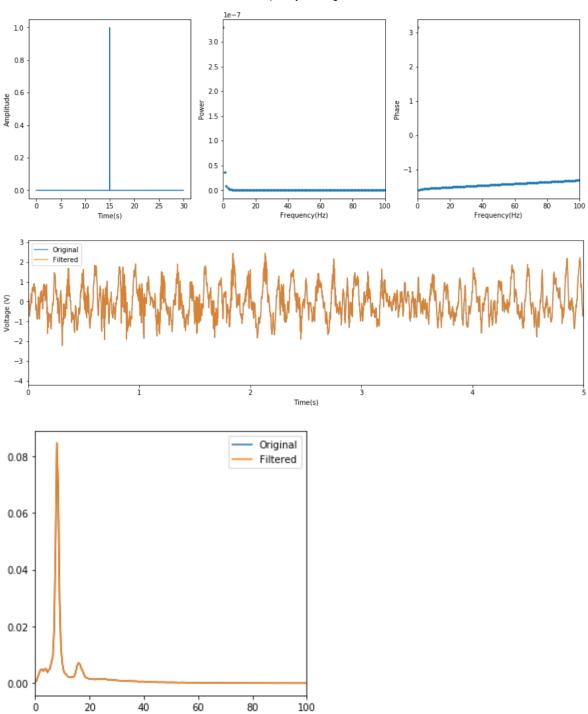
```
In [17]:
          H #################7.2
             cutoff = (4.12) #Hz
             # we typically want a filter order to be at least as long as 3 periods (cycles)
             # the slowest frequency in the cutoff.
             # so if cutoff is 20Hz, we want 3*0.05s = 0.15s long, which is 0.15*fs points
             # the larger this number is, the better frequency resolution you will have
             filt order = int(3*fs/(cutoff[1]-cutoff[0]))+1
             filt coefs = signal.firwin(filt order, cutoff, fs=fs, pass zero=True)
             # compute the magnitude and phase response of the filter
             freq resp = np.fft.fft(filt coefs, n=int(fs))
             mag resp = abs(freq resp)**2
             ph resp = np.angle(freq resp)
             freqs = np.fft.fftfreq(int(fs),1/fs)
             plt.figure(figsize=(15,5))
             plt.subplot(1,3,1)
             # plot impulse response
             t filt = np.arange(0,len(filt coefs))/fs
             plt.plot(t filt,filt coefs)
             plt.xlabel('Time(s)'); plt.ylabel('Amplitude');
             plt.subplot(1,3,2)
             plt.plot(freqs, mag resp, '.')
             plt.xlabel('Frequency(Hz)'); plt.ylabel('Power');
             plt.xlim([0,100])
             plt.subplot(1,3,3)
             plt.plot(freqs, ph resp, '.')
             plt.xlabel('Frequency(Hz)'); plt.ylabel('Phase');
             plt.xlim([0,100])
             plt.figure(figsize=(15,4))
             lfp filt = np.convolve(lfp short, filt coefs, mode='same')
             plt.plot(t short, lfp short, alpha=0.8, label='Original')
             plt.plot(t short, lfp filt, alpha=0.8, label='Filtered')
             plt.xlim([0,5])
             plt.legend()
             plt.xlabel('Time(s)');plt.ylabel('Voltage (V)')
             filt_f_stft, filt_t_stft, filt_stft = signal.stft(lfp_filt,fs, nperseg=nperseg,
             plt.figure(figsize= (5,5))
             plt.plot(f stft,np.array([(x.real**2 +x.imag**2).mean() for x in stft]),label='(
             plt.plot(filt f stft,np.array([(x.real**2 +x.imag**2).mean() for x in filt stft
             plt.legend()
             plt.xlim([0,100])
```

Out[17]: (0, 100)



```
In [18]:
          H #################7.3
             cutoff = 0.1 \#Hz
             # we typically want a filter order to be at least as long as 3 periods (cycles)
             # the slowest frequency in the cutoff.
             # so if cutoff is 20Hz, we want 3*0.05s = 0.15s long, which is 0.15*fs points
             # the larger this number is, the better frequency resolution you will have
             filt order = int(3*fs/cutoff)+1
             filt coefs = signal.firwin(filt order, cutoff, fs=fs, pass zero=False)
             # compute the magnitude and phase response of the filter
             freq resp = np.fft.fft(filt coefs, n=int(fs))
             mag resp = abs(freq resp)**2
             ph resp = np.angle(freq resp)
             freqs = np.fft.fftfreq(int(fs),1/fs)
             plt.figure(figsize=(15,5))
             plt.subplot(1,3,1)
             # plot impulse response
             t filt = np.arange(0,len(filt coefs))/fs
             plt.plot(t filt,filt coefs)
             plt.xlabel('Time(s)'); plt.ylabel('Amplitude');
             plt.subplot(1,3,2)
             plt.plot(freqs, mag resp, '.')
             plt.xlabel('Frequency(Hz)'); plt.ylabel('Power');
             plt.xlim([0,100])
             plt.subplot(1,3,3)
             plt.plot(freqs, ph resp, '.')
             plt.xlabel('Frequency(Hz)'); plt.ylabel('Phase');
             plt.xlim([0,100])
             plt.figure(figsize=(15,4))
             lfp filt = np.convolve(lfp short, filt coefs, mode='same')
             plt.plot(t short, lfp short, alpha=0.8, label='Original')
             plt.plot(t short, lfp filt, alpha=0.8, label='Filtered')
             plt.xlim([0,5])
             plt.legend()
             plt.xlabel('Time(s)');plt.ylabel('Voltage (V)')
             filt_f_stft, filt_t_stft, filt_stft = signal.stft(lfp_filt,fs, nperseg=nperseg,
             plt.figure(figsize= (5,5))
             plt.plot(f stft,np.array([(x.real**2 +x.imag**2).mean() for x in stft]),label='(
             plt.plot(filt f stft,np.array([(x.real**2 +x.imag**2).mean() for x in filt stft
             plt.legend()
             plt.xlim([0,100])
```

Out[18]: (0, 100)



```
In [19]:

    def filtering(lfp short, fs, cutoff, nperseg,noverlap, stop):

                 # we typically want a filter order to be at least as long as 3 periods (cycl
                 # the slowest frequency in the cutoff.
                 # so if cutoff is 20Hz, we want 3*0.05s = 0.15s Long, which is 0.15*fs point
                 # the larger this number is, the better frequency resolution you will have
                 filt_order = int(3*fs/cutoff)+1 if not isinstance(cutoff,tuple) else int(3*f
                 filt coefs = signal.firwin(filt order, cutoff, fs=fs, pass zero=stop)
                 f stft, t stft, stft = signal.stft(lfp short,fs, nperseg=nperseg, noverlap=
                 # compute the magnitude and phase response of the filter
                 freq resp = np.fft.fft(filt coefs, n=int(fs))
                 mag resp = abs(freq resp)**2
                 ph resp = np.angle(freq resp)
                 freqs = np.fft.fftfreq(int(fs),1/fs)
                 plt.figure(figsize=(15,5))
                 plt.subplot(1,3,1)
                 # plot impulse response
                 t filt = np.arange(0,len(filt coefs))/fs
                 plt.plot(t filt,filt coefs)
                 plt.xlabel('Time(s)'); plt.ylabel('Amplitude');
                 plt.subplot(1,3,2)
                 plt.plot(freqs, mag_resp, '.')
                 plt.xlabel('Frequency(Hz)'); plt.ylabel('Power');
                 plt.xlim([0,100])
                 plt.subplot(1,3,3)
                 plt.plot(freqs, ph_resp, '.')
                 plt.xlabel('Frequency(Hz)'); plt.ylabel('Phase');
                 plt.xlim([0,100])
                 plt.figure(figsize=(15,4))
                 lfp filt = np.convolve(lfp short, filt coefs, mode='same')
                 plt.plot(t_short, lfp_short, alpha=0.8, label='Original')
                 plt.plot(t short, lfp filt, alpha=0.8, label='Filtered')
                 plt.xlim([0,5])
                 plt.legend()
                 plt.xlabel('Time(s)');plt.vlabel('Voltage (V)')
                 filt f stft, filt t stft, filt stft = signal.stft(lfp filt,fs, nperseg=nper
                 plt.figure(figsize= (5,5))
                 plt.plot(f stft,np.array([(x.real**2 +x.imag**2).mean() for x in stft]),labe
                 plt.plot(filt f stft,np.array([(x.real**2 +x.imag**2).mean() for x in filt 
                 plt.legend()
                 plt.xlim([0,100])
```

In [20]: filtering(lfp_short,fs,(4,12),nperseg,noverlap,False) filtering(lfp_short,fs,(4,12),nperseg,noverlap,True) filtering(lfp_short,fs,0.1,nperseg,noverlap,False) 0.0125 0.0100 0.8 0.0075 0.0050 0.6 0.0025 0.4 0.0000 -0.0025 0.2 -2 -0.0050 0.0 -0.0075 Frequency(Hz) Original -3 -4 Time(s) Original 0.08 Filtered 0.06 0.04 0.02

0.00

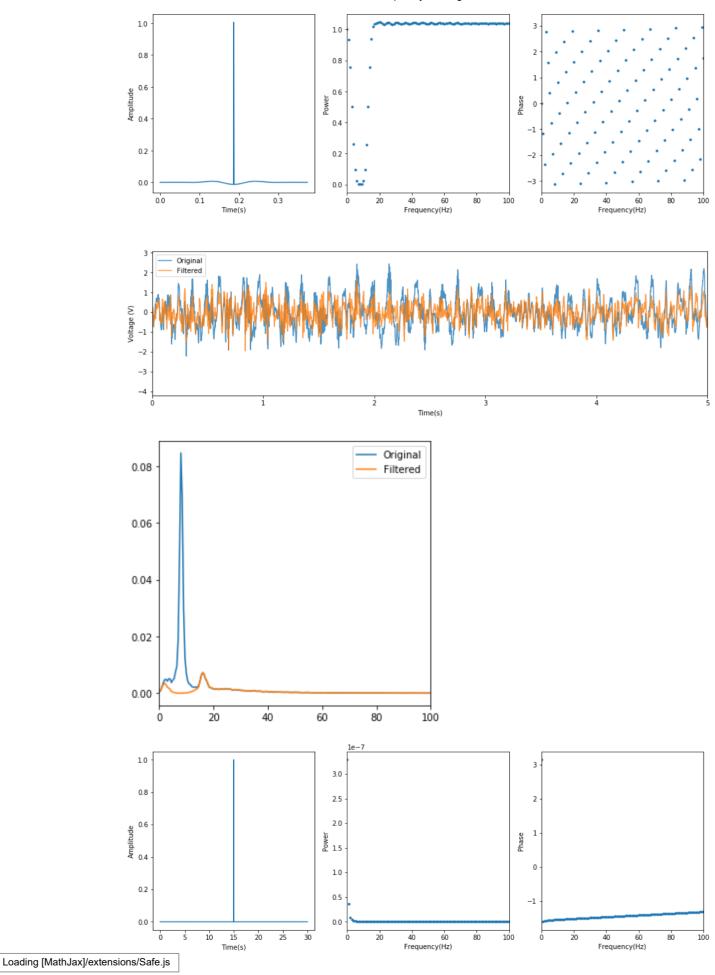
20

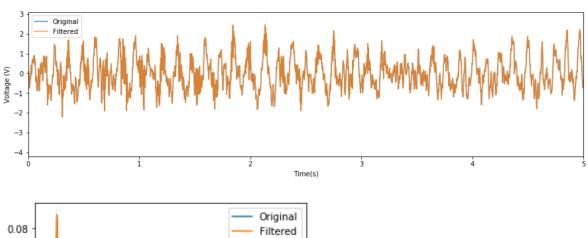
40

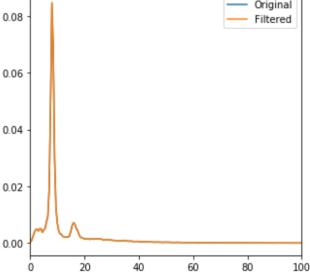
60

80

100







Congratulations!

You have just performed your first time-frequency analysis on neural data! While Fourier analysis from the last lab is the basis of signal analysis (and of the methods today), the set of tools presented here are the ones practicing neuroscientists actually use on a daily basis, including computing PSD and coherence. In addition, filtering has broad applications across domains, especially in sound engineering. Almost every lab in Cognitive Science and Neuroscience that record electrophysiological data here at UCSD will employ these tools for their analysis, so understanding these well will certainly position you to become an effective research assistant, or even graduate student researcher.

End Survery

Please take a few minutes to fill out the following as it will help us to improve the following assignments & lectures.



What was one thing you learned from this lab & associated lectures?

ANSWER: Wave filtering

What was one thing that you still found confusing after the lab, and need clarification?

ANSWER: The usage for coherence

Style:

What was one thing you enjoyed about the formatting of this assignment (e.g., clarity, structure, guidance, etc.)?

ANSWER: Able to check answers

What was one thing that you thought could use improvements on?

ANSWER: Confusing Questions

Thank you!