



Power Systems Laboratory
(EE3P006)

EXPERIMENT-2

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FORMATION OF BUS ADMITTANCE AND IMPEDANCE MATRICES AND SOLUTION OF NETWORKS

AIM:

To develop a program to obtain Ybus matrix for the given networks by the method of inspection.

FORMATION OF Y-BUS MATRIX

Each admittance Y_{ii} ($i = 1, 2, \dots, n$) is called the self admittance or driving point admittance of bus i and equals the sum of all admittances terminating on the particular bus. Each off-diagonal term Y_{ij} ($i, j = 1, 2, \dots, n; j \neq i$) is the transfer admittance between buses i and j , $n = \text{total number of buses}$. Further, $Y_{ij} = Y_{ji}$

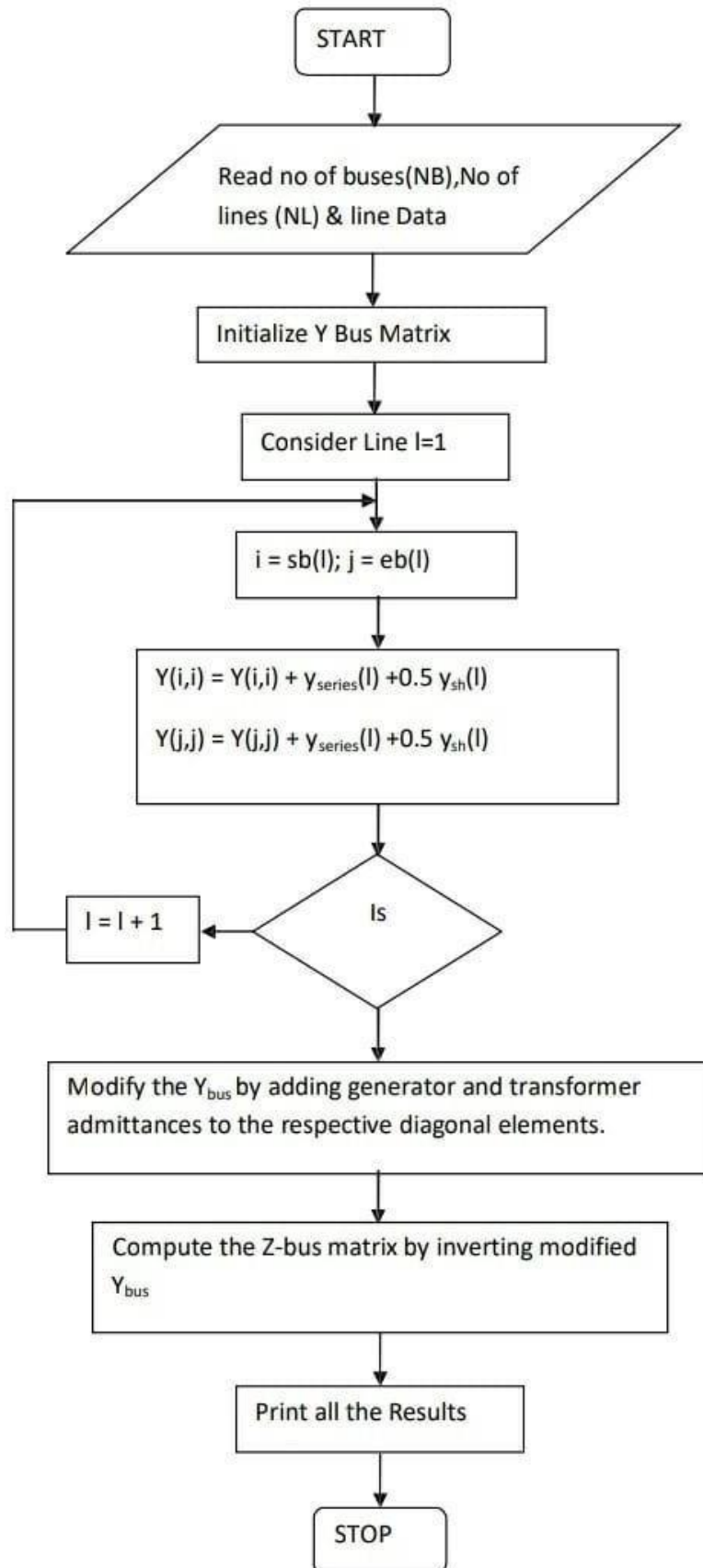
ALGORITHM

Step (1): Initialize [Y-Bus] matrix that is replace all entries by zero. $Y_{ij} = Y_{ij} - y_{ij} = Y_{ji}$
= off diagonal element n

Step (2): Compute $Y_{ii} = \sum y_{ij} = \text{diagonal element. } j = 1$

Step (3) : Modify the Ybus matrix by adding the transformer and the generator admittances to the respective diagonal elements of Y- bus matrix.

Step (4) : Compute the Z-Bus matrix by inverting the modified Ybus matrix.



1. The [Y-Bus] matrix is formed by inspection method for a four bus system. The line data and is given below.

LINE DATA

Line Number	SB	EB	Series Impedance (p.u)	Line charging Admittance (p.u)
1	1	2	$0.10 + j0.40$	$j0.015$
2	2	3	$0.15 + j0.60$	$j0.020$
3	3	4	$0.18 + j0.55$	$j0.018$
4	4	1	$0.10 + j0.35$	$j0.012$
5	4	2	$0.25 + j0.20$	$j0.030$

FORMATION OF Y-BUS BY THE METHOD OF INSPECTION

PROGRAM:

```
clc; clear all;
%      lineno. Frombus Tobus series Impeadence Admittance
linedata = [ 1  1  2  0.1+1i*0.4  1i*0.015;
2  2  3  0.15+1i*0.6  1i*0.2;
3  3  4  0.18+1i*0.55  1i*0.018;
4  4  1  0.1+1i*0.35  1i*0.012;
5  4  2  0.25+1i*0.2  1i*0.3];

gfb = linedata(:,2); %going from bus
ctb = linedata(:,3); %coming to bus

y= 1./linedata(:,4);
a = linedata(:,5);

nbus = max(max(gfb),max(ctb)); %no of buses in the system
nbranch = length(gfb); %no of branches in the system

Y = zeros(nbus,nbus);

% non diagonal elements for i=1:nbranch
Y(gfb(i),ctb(i)) = -y(i);
Y(ctb(i),gfb(i)) = -y(i);
end
```

```

% diagonal elemnets for i=1:nbus
for j= 1:nbranch
if(gfb(i)==j || ctb(j) == i) Y(i,i) = Y(i,i)+y(j)+a(j)./2;

end

end

end

disp("Admittance bus matrix: "); disp(Y);
Z = Y';
disp("Impeadence bus from inverse of admittance bus:") disp(Z);

```

OUTPUT:

Admittance bus matrix:

1.3430 - 4.9810i	-0.5882 + 2.3529i	0.0000 + 0.0000i	-0.7547 + 2.6415i
-0.5882 + 2.3529i	3.4194 - 5.6153i	-0.3922 + 1.5686i	-2.4390 + 1.9512i
0.0000 + 0.0000i	-0.3922 + 1.5686i	0.9296 - 3.1019i	-0.5375 + 1.6423i
-0.7547 + 2.6415i	-2.4390 + 1.9512i	-0.5375 + 1.6423i	1.2922 - 4.2688i

Impedance bus from inverse of admittance bus:

1.3430 + 4.9810i	-0.5882 - 2.3529i	0.0000 + 0.0000i	-0.7547 - 2.6415i
-0.5882 - 2.3529i	3.4194 + 5.6153i	-0.3922 - 1.5686i	-2.4390 - 1.9512i
0.0000 + 0.0000i	-0.3922 - 1.5686i	0.9296 + 3.1019i	-0.5375 - 1.6423i
-0.7547 - 2.6415i	-2.4390 - 1.9512i	-0.5375 - 1.6423i	1.2922 + 4.2688i

FORMATION OF Z-BUS MATRIX

Z-Bus matrix is an important matrix used in different kinds of power system studies such as short circuit study, load flow study, etc.

- In short circuit analysis, the generator and transformer impedances must be taken into account. In contingency analysis, the shunt elements are neglected while forming the Z-Bus matrix, which is used to compute the outage distribution factors.
- This can be easily obtained by inverting the Ybus formed by inspection method or by analytical method. Taking inverse of the Ybus for large systems is time consuming; moreover, modification in the system requires the whole process to be repeated to reflect the changes in the system. In such cases, the Z-Bus is computed by Z-Bus building algorithm

ALGORITHM:

Step1: Start the program.

Step2: Read the number of buses, starting bus and ending bus.

Step3: Initialize the ZBus matrix.

Step4: Form the Z-Bus matrix as follows:

Case1: When a new bus of impedance Z_b is connected to reference bus Z_{bus} ,
 $new = [Z_b]$

Case2: Adding new bus p to existing bus q

$$Z_{bus, new} = \begin{bmatrix} Z_{orig} & Z_{1q} \\ & Z_{2q} \\ & \vdots \\ Z_{q1} & Z_{q2} & \dots & Z_{qq} + Z_b \end{bmatrix}$$

Case3: Adding impedance from an existing bus to reference bus.

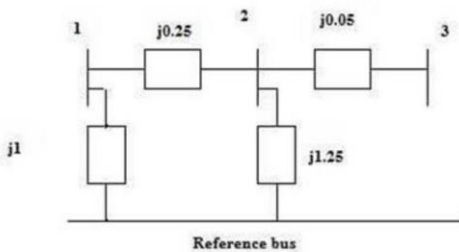
$$Z_{jk, act} = Z_{jk} - \frac{Z_{j(n+1)} * Z_{(n+1)k}}{Z_{(n+1)(n+1)}}$$

Case4: Adding Z_b between two existing buses h and q

$$Z_{bus,new} = \begin{bmatrix} Z_{orig} & & \\ & Z_{1h} - Z_{1q} & \\ & Z_{2h} - Z_{2q} & \\ Z_{h1} - Z_{q1} & Z_{h2} - Z_{q2} & \dots Z_{(n+1)(n+1)} \end{bmatrix}$$

Case5: Print the Z-bus matrix.

2. Z bus



```
%      from to Z   type
linedata1= [2    1    1    1;
            3    1    1.25  1;
            4    3    0.05  2;
            3    2    0.25  4];
```

PROGRAM:

```
%   from   to   Z   type
linedata1= [2  1   1   1;
            3  1  1.25   1;
            4  3  0.05   2;
            3  2  0.25   4];

zbus = (0); zline = linedata1(:,3); type = linedata1(:,4); n =
length(zline);

for i = 1:n
[r,c]=size(zbus);
frbus = linedata1(i,1); tobus = linedata1(i,2);

if (type(i)==1 || type(i)==2) w= min(frbus,tobus);
zbus = [[zbus zbus(:,w)]; [zbus(w,:) zline(i)+zbus(w,w)]];
end

if (type(i)==3 || type(i)==4)
s = zbus(:,frbus)-zbus(:,tobus); s1 = s';
zbus = zbus-(s*s1)/(zline(i)+zbus(frbus,frbus)+zbus(tobus,tobus)-
2*zbus(frbus,tobus));
end
end
n1 = size(zbus);
zbus = zbus(2:n1,2:n1); disp("Impeadence matrix bus: ") disp(zbus);
```

OUTPUT:

Impendence matrix bus:

0.6000	0.5000	0.5000
0.5000	0.6250	0.6250
0.5000	0.6250	0.6750