

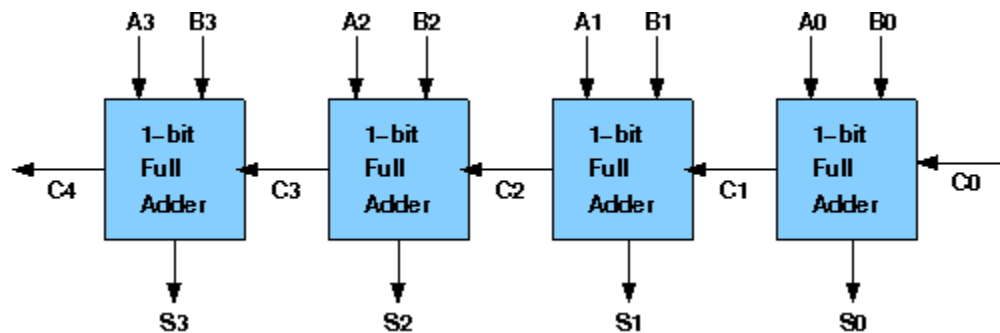
Experiment No. : 02

Aim: To Design of Ripple Carry Adders

Theory:

Arithmetic operations like addition, subtraction, multiplication, division are basic operations to be implemented in digital computers using basic gates like AND, OR, NOR, NAND etc. Among all the arithmetic operations if we can implement addition then it is easy to perform multiplication (by repeated addition), subtraction (by negating one operand) or division (repeated subtraction).

Half Adders can be used to add two one bit binary numbers. It is also possible to create a logical circuit using multiple full adders to add N-bit binary numbers. Each full adder inputs a C_{in} , which is the C_{out} of the previous adder. This kind of adder is a Ripple Carry Adder, since each carry bit "ripples" to the next full adder. The first (and only the first) full adder may be replaced by a half adder. The block diagram of 4-bit Ripple Carry Adder is shown here below –



The layout of ripple carry adder is simple, which allows for fast design time; however, the ripple carry adder is relatively slow, since each full adder must wait for the carry bit to be calculated from the previous full adder. The gate delay can easily be calculated by inspection of the full adder circuit. Each full adder requires three levels of logic. In a 32-bit [ripple carry] adder, there are 32 full adders, so the critical path (worst case) delay is $31 * 2(\text{for carry propagation}) + 3(\text{for sum}) = 65$ gate delays.

Design Issues :

The corresponding Boolean expressions are given here to construct a ripple carry adder. In the half adder circuit the sum and carry bits are defined as

$$\text{sum} = A \oplus B$$

$$\text{carry} = AB$$

In the full adder circuit the the Sum and Carry output is defined by inputs A, B and Carryin as

$$\text{Sum} = ABC + ABC + ABC + ABC$$

$$\text{Carry} = ABC + ABC + ABC + ABC$$

Having these we could design the circuit. But, we first check to see if there are any logically equivalent statements that would lead to a more structured equivalent circuit.

With a little algebraic manipulation, one can see that

$$\text{Sum} = ABC + ABC + ABC + ABC$$

$$= (AB + AB) C + (AB + AB) C$$

$$= (A \oplus B) C + (A \oplus B) C$$

$$= A \oplus B \oplus C$$

$$\text{Carry} = ABC + ABC + ABC + ABC$$

$$= AB + (AB + AB) C$$

$$= AB + (A \oplus B) C$$

Procedure:

Design of Ripple Carry Adders:

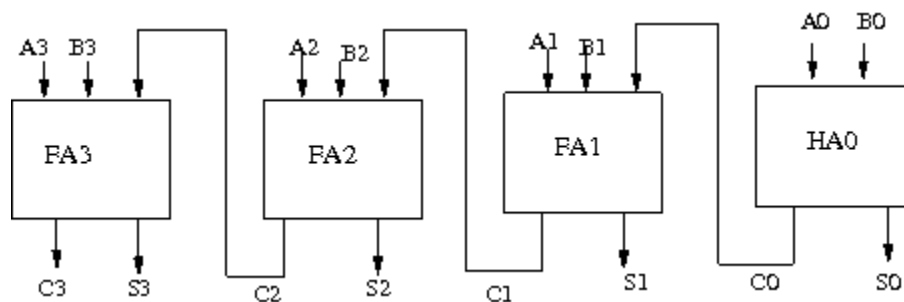
Procedure to perform the experiment: Design of Ripple Carry Adders

1. Start the simulator as directed. This simulator supports 5-valued logic.
2. To design the circuit we need 3 full adder, 1 half adder, 8 Bit switch(to give input), 3 Digital display(2 for seeing input and 1 for seeing output sum), 1 Bit display(to see the carry output), wires.
3. The pin configuration of a component is shown whenever the mouse is hovered on any canned component of the palette or presses the 'show pin config' button. Pin numbering

starts from 1 and from the bottom left corner (indicating with the circle) and increases anticlockwise.

4. For half adder input is in pin-5,8 output sum is in pin-4 and carry is pin-1, For full adder input is in pin-5,6,8 output sum is in pin-4 and carry is pin-1
5. Click on the half adder component(in the Adder drawer in the pallet) and then click on the position of the editor window where you want to add the component(no drag and drop, simple click will serve the purpose), likewise add 3 full adders(from the Adder drawer in the pallet), 8 Bit switches, 3 digital display and 1 bit Displays(from Display and Input drawer of the pallet, if it is not seen scroll down in the drawer)
6. To connect any two components select the Connection menu of Palette, and then click on the Source terminal and click on the target terminal. According to the circuit diagram connect all the components; connect 4 bit switches to the 4 terminals of a digital display and another set of 4 bit switches to the 4 terminals of another digital display. Connect the pin-1 of the full adder which will give the final carry output. Connect the sum (pin-4) of all the adders to the terminals of the third digital display(according to the circuit diagram shown in screenshot). After the connection is over click the selection tool in the palette.
7. To see the circuit working, click on the Selection tool in the pallet then give input by double clicking on the bit switch, (let it be 0011(3) and 0111(7)) you will see the output on the output(10) digital display as sum and 0 as carry in bit display.

Circuit diagram of Ripple Carry Adder:



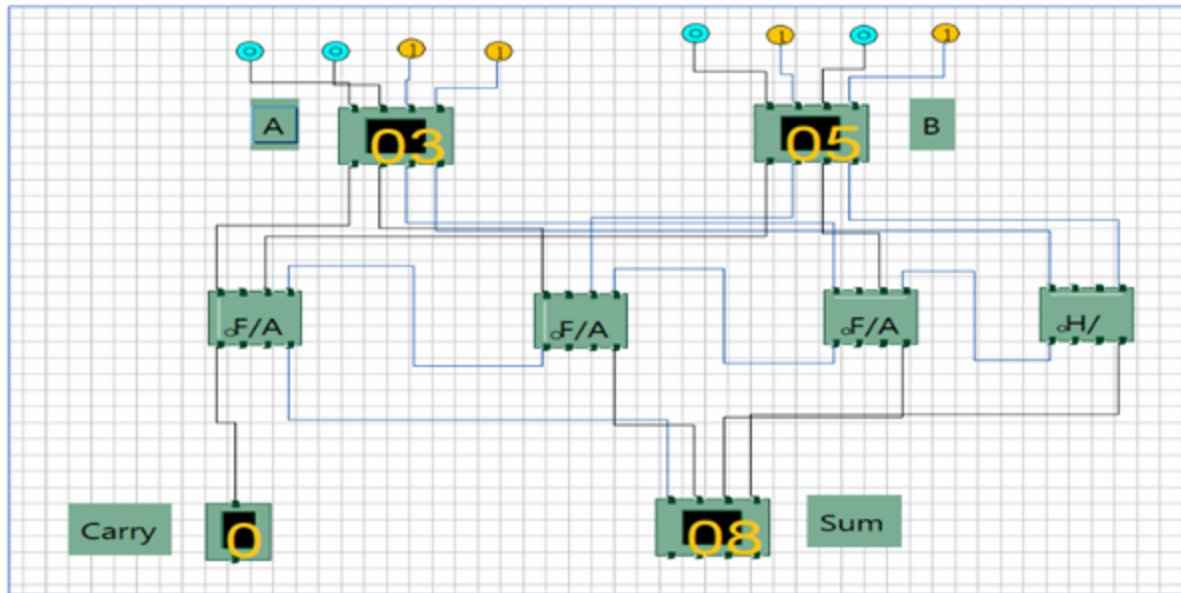
Screenshot of Ripple Carry Adder:

Components:

The components needed to create 4 bit ripple carry adder is listed here -

- 4 full-adders
- wires to connect

- LED display to obtain the output



Here, the two inputs A and B are 4-bit inputs. Three Full Adders and One Half Adder is used since first carry is to be 0, to construct the 4-bit Ripple Carry Adder.

For the test case, A = 3 and B = 5 and the Sum is $3+5 = 8$ and Carry is 0, which is as expected.

Conclusion: Thus, we have successfully designed the Ripple Carry Adder. and full-adders.