

# Assignment:-06

Ans 1)

## MINIMUM SPANNING TREE:-

It is a subset of the edges of a connected edge-weighted undirected graph that connects all the vertices together, without any cycle and with the minimum possible total edge weight.

### Applications:-

- Consider  $n$  stations are to be linked using a communication network, and laying of communication link b/w any 2 stations involves a cost; so we use MST for a better output.
- Same goes with roadways & highways & airlines.
- Design LAN
- Laying Pipeline connecting offshore drilling sites, refineries & markets.

Ans 2)

Algorithm

Time Complexity

Space Complexity

Prim's Algorithm

$O(V+E)$

$O(V)$

Dijkstra's Algorithm

$O(V^2)$

$O(V^2)$

Kruskal's Algorithm

$O(E \log V)$

$O(V \log V)$

Bellman Ford

$O(VE)$

$O(V)$

Ans 3)

## Graph:-



8

0				
1				
4				
3				

[37]

Prim's

Algo:-

3	4	5	6	7
∞	∞	∞	∞	∞

4

8

∞	∞	∞	1
7	∞	1	8

4

14

1

10

2

1

5

4

7

10

2

4

7

1

9

2

1

8

8  
∞  
∞  
7  
2  
6  
6  
6

brant:-

0	1	2	3	4	5	6	7	8
-1	<del>1</del>	<del>-1</del>	-1	-1	-1	<del>1</del>	<del>1</del>	-1
	6	1				1	1	



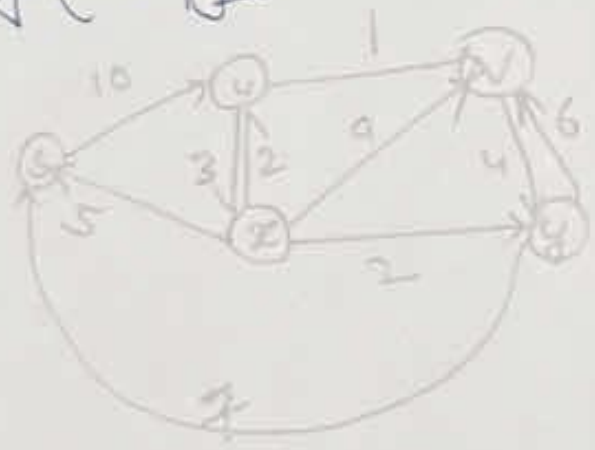
Wgt. = 37

Ans 4)

- i) Shortest path may change. The reason is that there may be different path from 's' to 't'. For example:-  
 let shortest path be of weight 15 & edge 5. Let there be another path with 2 edges and total weight 25. Hence, the shortest path increases. More weighted of other paths are also increase.
- ii) If we multiply all edges wgt by 10, shortest path won't change. Only the weight will be increased by 10 or otherwise it will follow the same path.

Ans 5)

Dijkstra's Algo:-



Node  
u  
x  
z  
w

Shortest distance from source node  
8  
5  
9  
7

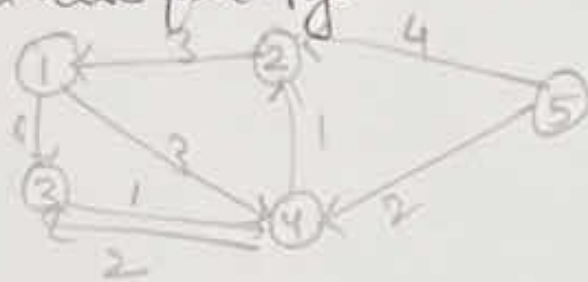
column 1000 -

1st	→	5	10	20	5	20
2nd	→	5	10	10	5	20
3rd	→	5	5	5	5	20
4th	→	5	5	5	5	20

no  
cycle  
exists

Question 5

Floyd Warshall Algo:-



TC =  $O(V^3)$   
 SC =  $O(V^2)$