

# Assignment:- 05

Ans 1)

BFS

- uses queue data structure.
- Stands for Breadth First Search.
- can be used to find single source shortest path in an unweighted graph and we reach a vertex with min. no. of edges from a source vertex.
- Siblings are visited before children.

Applications:-

- Shortest path & minimum spanning tree in unweighted graph.
- Peer to peer networks.
- Social Networking websites.
- GPS Navigation Systems.

DFS

- uses stack data structure.
- stands for Depth First Search.
- we might traverse through more edges to reach a destination vertex from source.
- children are visited before siblings.

Applications:-

- Detecting cycle in graph.
- Path finding.
- Topographical Sorting.
- Solving puzzles with only 1 solution.

Ans 2)

In BFS; we use queue data structure as queue is used when things don't have to be processed immediately, but have to be processed immediately, but have to be processed in FIFO order like BFS.

In DFS; stack data structure is used as it is beneficial for backtracking. For DFS, we retrieve it from root to the furthest node as much as possible; giving it a LIFO like approach.

Ans 3)

Dense Graph is a graph in which no. of edges is close to the maximal no. of edges.

Sparse Graph is a graph in which the no. of edges is close to the minimal no. of edges. It can be a disconnected graph.

Adjacency lists are preferred for sparse graphs & Adjacency Matrix for Dense Graphs.

Ans 4.)

### Cycle detection in directed graph (BFS)



-1 - unvisited,  
0 - into queue,  
1 - traversed.

Queue: 

|   |   |   |   |   |
|---|---|---|---|---|
| A | B | C | D | E |
|---|---|---|---|---|

Visited set: 

|   |   |   |   |
|---|---|---|---|
| A | B | C | D |
|---|---|---|---|

When D checks its adjacent vertices it finds E with 0.

If any vertex finds the adjacent vertex with flag 0, then it contains cycle.

### Cycle detection in directed graph (DFS)



-1 - unvisited,  
0 - visited & stack push,  
1 - visited & popped.

Stack: 

|   |
|---|
| B |
| C |
| A |

visited: A, B, C, D, E

→ D → D → E → B

Here, E find B with 0.  
→ It's a cycle.

| Parent Vertex | Map Forest |
|---------------|------------|
| A             | —          |
| B             | A          |
| C             | B          |
| D             | B          |
| E             | D          |

Ans 5 The DISJOINT SETS data structure is also known as Union-find data structure and merge-find set. It is a data structure that contains a collection of disjoint or non-overlapping sets.

The DISJOINT SETS means when the set is partitioned into the disjoint subsets, various operations are performed on it.

In this case, we can add new set, merge them & also find the representative member of a set. It also allows to find out whether the two elements are at same set or not effectively.

### Operations on Disjoint sets:

(1) Union:-

Q If sets  $S_1$  &  $S_2$  are 2 disjoint sets, then union  $S_1 \cup S_2$  is a set of all elements of such that  $x$  is in either  $S_1$  or  $S_2$ .

- (b) As the sets should be disjoint S1 & S2 replace S1 & S2 which no longer exists  
 (c) It is achieved by simply making one of the trees as a subtree of other, that is, let parent field of one of the roots of the trees to other root.



Change into 1

(2) Find:-

Given an element  $x$ , to find the set containing it.

Eg:-  $\text{find}(3) \rightarrow S1$   
 $\text{find}(4) \rightarrow S2$

(3) Make Set  $G$ :-

create a set containing  $G$   
 $\text{makeSet}(1) = \{1\}$

Ques 6)



DFS:-

|        |   |   |   |   |   |   |   |   |
|--------|---|---|---|---|---|---|---|---|
| child  | G | D | F | H | C | E | A | B |
| Parent | - | G | G | G | H | C | E | A |

Path:-

$G \rightarrow H \rightarrow C \rightarrow E \rightarrow A \rightarrow B$

DFS:- Node visited

~~G~~  
~~D~~  
~~H~~  
~~F~~  
~~C~~  
~~E~~  
~~A~~  
~~B~~

Stack

~~G~~  
~~F~~  
~~C~~  
~~E~~  
~~A~~  
~~B~~

Path

$G \rightarrow F \rightarrow C \rightarrow E \rightarrow A \rightarrow B$



Ans 7



$$V = \{a, b, c, d, e, f, g, h, i, j\}$$

$$E = \{(a, b), (b, c), (c, d), (d, a), (e, f), (f, g), (h, i), (i, j)\}$$

| Vertex<br>Edge → | {a}          | {b} | {c} | {d} | {e}    | <del>{f}</del> | {g}    | {h}    | {i}    | {j} |
|------------------|--------------|-----|-----|-----|--------|----------------|--------|--------|--------|-----|
| (a, b)           | {a, b}       | {c} | {d} | {e} | —      |                | {g}    | {h}    | {i}    | {j} |
| (b, c)           | {a, b, c}    |     | {d} | {e} |        |                | {g}    | {h}    | {i}    | {j} |
| (c, d)           | {a, b, c}    |     | {d} | {e} |        |                | {g}    | {h}    | {i}    | {j} |
| (d, a)           | {a, b, c, d} |     | {e} | {f} |        |                | {g}    | {h}    | {i}    | {j} |
| (e, f)           |              |     |     |     | {e, f} |                |        |        |        |     |
| (f, g)           |              |     |     |     |        | {g}            |        |        |        |     |
| (h, i)           |              |     |     |     |        |                | {h, i} |        |        |     |
| (i, j)           |              |     |     |     |        |                |        | {i, j} |        |     |
| (j, a)           |              |     |     |     |        |                |        |        | {j, a} |     |

Finally - {a, b, c, d}, {e, f, g}, {h, i} & {j}

Ans 8



Algo:-

- Go to node 0, it has no outgoing edges so push node 0 into the stack & mark as visited.
- Go to node 1, again it has no outgoing edges so push it in stack & mark as visited.
- Go to node 2, process all adjacent and mark it visited.
- Node 3 is visited, so continue with next node.
- Go to node 4, all its adjacent nodes are already visited, so push it in stack & mark as visited.
- Go to node 5, push it in stack & stop.

Output:-

5 4 2 3 1 0

Ans 9.)

Heap is generally preferred for priority queue implementation because heap provides better performance compared to array & linked list.

Algorithms when priority queue is used:-

(1) Dijkstra's Algo:-

Shortest path algorithm; when the graph is stored in the form of adjacency list or matrix; priority queue can be used to extract minimum effectively when implementing it.

(2) Prim's Algo:-

To store keys of Nodes & extract minimum key node at every step.

Ans 10.)

Min Heap

- For every pair of parent & child nodes, parent node always has <sup>lower</sup> value than descendant child node.
- Value of nodes increases as we traverse from root to leaf node.
- Root node has the lowest value.

Max Heap

- For every pair of parent and descendant child nodes, the parent has higher value than child node.
- Value of nodes decreases as we traverse from root to leaf node.
- Root node has the largest value.