Agenda:-

- 1) Logistic Regression
- 2) Performance Matrix
 - a) Confusion Matrix
 - 6) Accordacy
 - C) Precision
 - d> Recall
 - e) F-Beta Score.

1) Logistic Regression: -

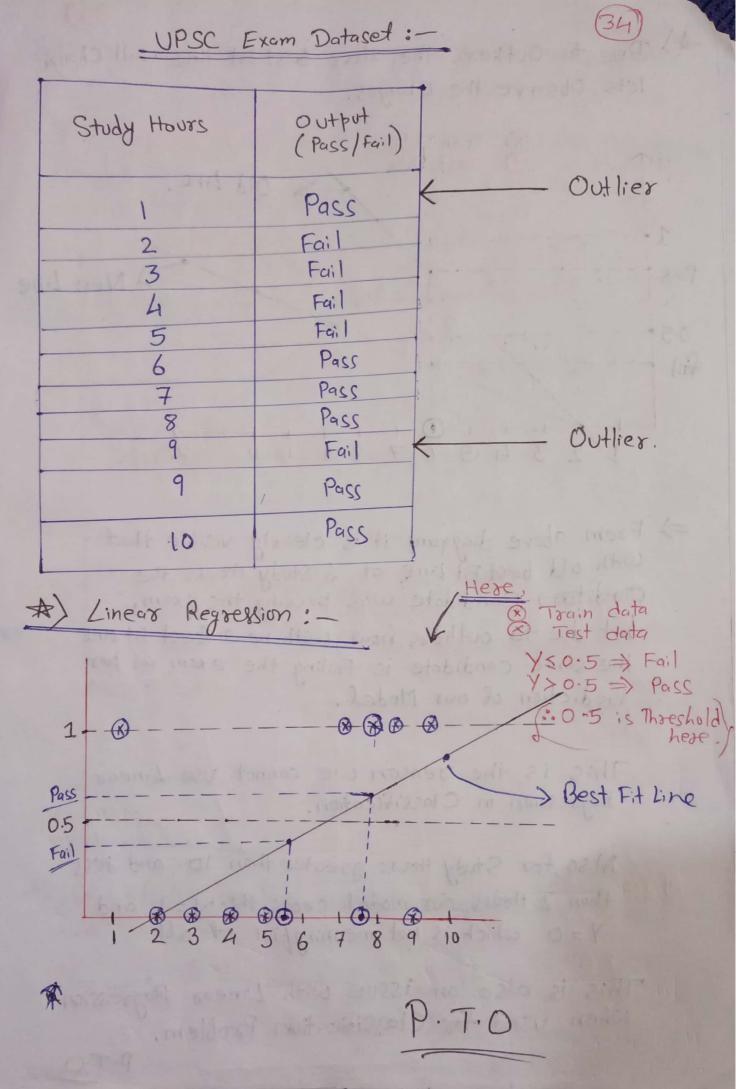
=> The logistic Regression technique involves the dependent Variable, which can be represented in the binary (o or 1, true or false, Yes or No) Values, Which means that the outcome could only be in either one form of two. For Example, it can be utilized when we need to find the probality of

Note: - Logistic Regression is used when the dependent Variable (Target)
Logistic Regression Model . - is categoricals. a Successful or Fail Event.

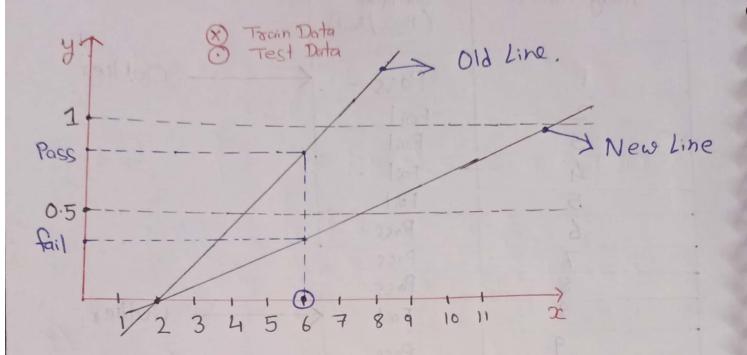
Logistic Regression Model:-

Pass Logistic Study Regression HOUTS 1-qi Kola HOURS

Inputs: Study Hours, Play Hours | Weights: O1, 02 11
... Logistic Regression is used when the dependent variable is Toroto.



Due to Outliers the above best fit line will Change lets Observe the Changes.



From above diagram it is clearly visible that with old best Fit Line at 6 Study Hours the conditions Candidate was passing the exam, but due to outliers now with new best Fit Line the same candidate is Failing the exam as per Prediction of our Model.

This is the reason we cannot use Linear Regression in Classification.

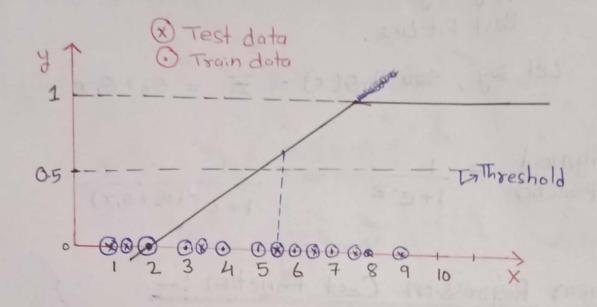
Also, for Study Hours greater than 10 and less than 2 Hours our model cross the Y=1 and Y=0 which is not meaningful at all.

This is also an issue with Linear Regression when used for Claysification Problem.

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So, to Avoid this what we can do is make Best Fit Line Parallel to X-axis when it tries to cross. Y=1 or Y=0 Lines. This is the Logistic Regression Model.



Test data	Model Prediction
1.5	Fail
3.6	Fail
5.4	Pass
6.7	Pass
7.9	Pass
Manager A	, 53

To get this type of output that ranges from 0 to 1 we use Sigmoid Activation function. This Function will squash the Line Parallel to X-axis when it tries to cross y=1 and y=0 Line.

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Step 1: Best Fit Line
$$ho(x) = 0_0 + 0.00$$

Step 2: - Apply Sigmoid Activation function to Best Fit Line.

Let say, som
$$ho(x) = Z = 0.0 + 0.0$$

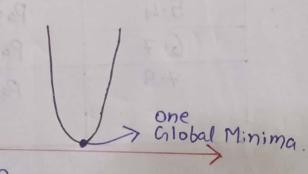
:. Sigmoid =
$$\frac{1}{1+e^{-z}}$$
 = $\frac{1}{1+e^{-(\theta_0+\theta_1x)}}$

1) Linear Regression Cost Function:

$$\frac{MSE}{J(\theta_0,\theta_i)} = \frac{1}{m} \underset{i=1}{\overset{m}{\geq}} \left(h\theta(x)^{(i)} - y^{(i)}\right)^2$$

:. $ho(x) = O_0 + O_1 x$

.. This Cost Function has Caradient Descend as Convex Function.

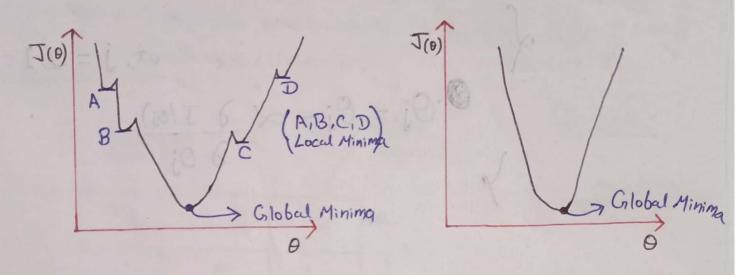


.: Now Lets create Logistic Regression Cost Function using above Cost Function.

$$ho(x) = Z = 0.40100$$

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But there is one very big issue with this is that it creates a non-convex gradient descent function. Which has lot of Local Minima. Where our gradient-descent algorithm is stuck on the first Local Minima and never reaches global Minima.



We use Log - Loss Cost Functions:

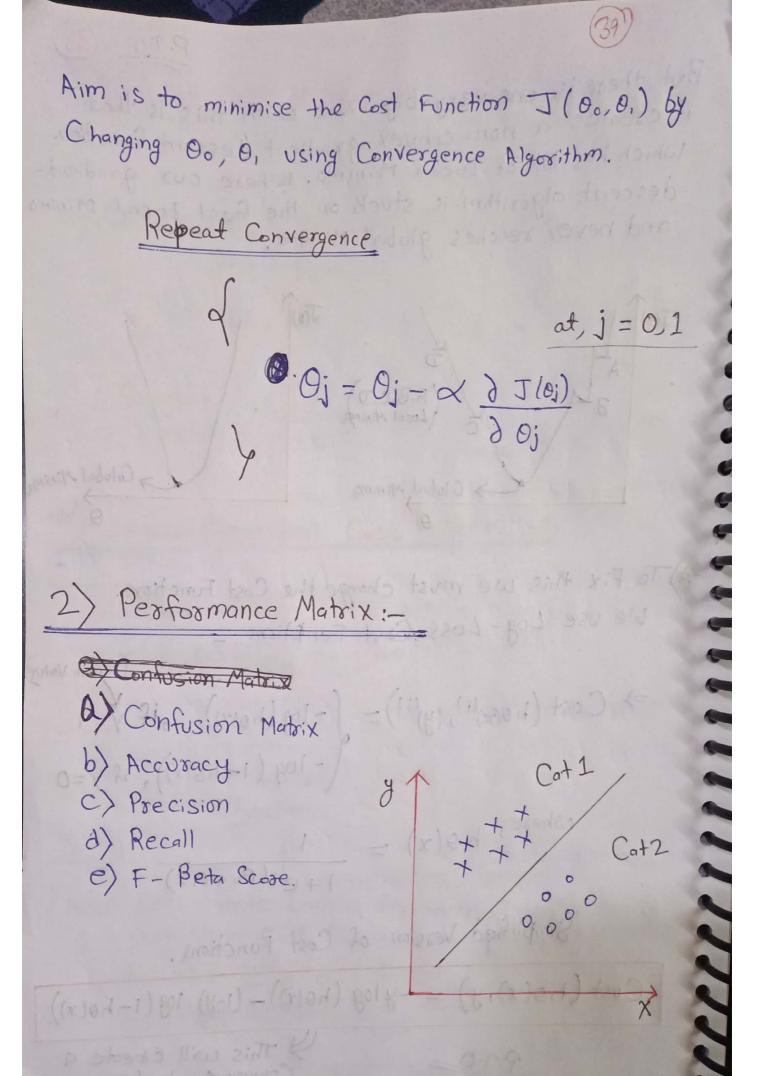
$$\Rightarrow \operatorname{Cost}(h \circ Gc)^{(i)}, (y)^{(i)}) = \begin{cases} -\log(h \circ (x)), & \text{if } y = 1 \\ -\log(1 - h \circ (x)), & \text{if } y = 0 \end{cases}$$

where,
$$h \Theta(x) = \frac{1}{1 + e^{-(\theta_0 + \theta_1 x)}}$$

Simplified Version of Cost Functions.

P.T.0

Y This will cheate a Convex Gradient Descent.



a) Confusion Matrix:

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A confusion Matrix is an extremely useful tools to Observe in which way the model is wrong (or Right!). It is a matrix that compades the number of Predictions for each class that are correct and those that are incorrect.

Dataset: - Pr	del rediction	
F ₁ F ₂ 0/P ŷ	Jo	
	ist til	
00	(y) Actual Values	
- 0 1	1 TP FP TO FN TN	
	Predicted Valve (y)	
* For Binary Classification:		
Truly (1 0 (Actual (y) Value (y)		
1 2 2	Positive	
Predicted Truly	Negative	

In a Confusion Matrix, there are 4 Numbers to

TP FP

OFN TN

Predicted
Values(g)

- True-Positives (TP): The Number of Positive observations the model correctly Predicted as Positive.
- ii) False-Positive (FP): The Number of Negative

 Observations the model incorrectly

 Predicted as Positive.
- iii) True Negative (TN): The Number of Negative

 Observations the model corretly

 Predicted as Negative.
- iv) False-Negative (FN): The Number of Positive Observations the model incorrectly Predicted as Negative.

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1) Impostant Note: -

C	Prediction
TP-Truly Positive	Correct
raisely Positive	Incorrect
- Falsely Negative	Incorrect
TN - Truly Negative	Correct

b) Accuracy: - Accuracy is defined as the ratio of correct Predictions to total Number of Observations | Predictions.

Accuracy = Correct Predictions

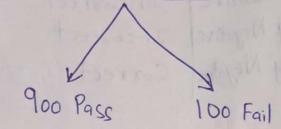
Total Predictions

$$Accoracy = \frac{TP + TN}{TP + TN + FP + FN}$$

.. That is, our Model is 70% Accuracy

Limitation of Accuracy:

Consider a Binary Classification Data Set with 1000 Observations



Imbalance Dataset

The create a dump Model which Predicts
Only Pass. So for our data set it will predict.
Correctly for 900 Observations.

So, Accuracy = 900 = 0.9 08 90%

Conclusion: - We cannot decide whether a model is good or Bad by just considering Accuracy.

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C) Precision: - Precision is defined for Pass or fail.

i.e Precision of Pass or Precision of Fail.

The main aim in Precision is to reduce wrong Predictions. (i.e. False Positive and False Negative).

Example:-

i) Spam Prediction: _ If our Mail is ham but our model Predicts it as Spam, we may Miss out on important mails, we must reduce this,

ii) Diabetes Prediction: If we have Diabetes, but our Model Predicts that we don't have Diabetes, we will be in quite Danger of getting Seriously ill. We must reduce this, False Negatives. Scanned with CamScanner

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d) Recall: - Recall is also defined for Pass or Fail.

Recall = Correctly Predicted Pass or Fail

Total Prediction of Pass or Fail

$$\frac{\left(\text{Recall}\right)_{\text{Pass}} = \frac{\text{TP}}{\text{TP+FN}}}{\left(\text{Recall}\right)_{\text{Fail}} = \frac{\text{TN}}{\text{TN+FO}}$$

Example

$$(\text{Recall})_{\text{F}} = \frac{5}{5+1} = \frac{5}{6}$$

 $(\text{Recall})_{\text{F}} = \frac{2}{2+2} = \frac{2}{4} = \frac{1}{2}$

* Example:-

=> Preditt if Tommorrows Stock is going to Crash.

Aim: Aim will be to reduce

False Negative, So that
People can Remove money
in Time: FNW

Aim: - Aim is to reduce
False Positive,
Soll their stock to reduce

The is weighted Harmonic Mean of Precision and Recall. B-Parameter Determines the weight of Recall in the combined Score.

 $\beta < 1 \Rightarrow$ More Weight to Precision $\beta > 1 \Rightarrow$ More Weight to Recall $\beta = 0 \Rightarrow$ Only Precision $\beta = 0 \Rightarrow$ Only Recall.

$$F-B$$
 score = $(1+B)^2$ (Precision × Recall)
$$B^2$$
 (Precision) + Recall.

i) If we need to give equal important to FP and FN reduction. (B=1)

11) If FP is more Important than FN. (B=0.5)

F-0.5 Score = 1.25 PAR

O.25 PAR

O.25 PAR

(III) If FN is more Important than FP. (B=2)

F-2 Score = 5 PXR
4P+R