

Sequential Circuits

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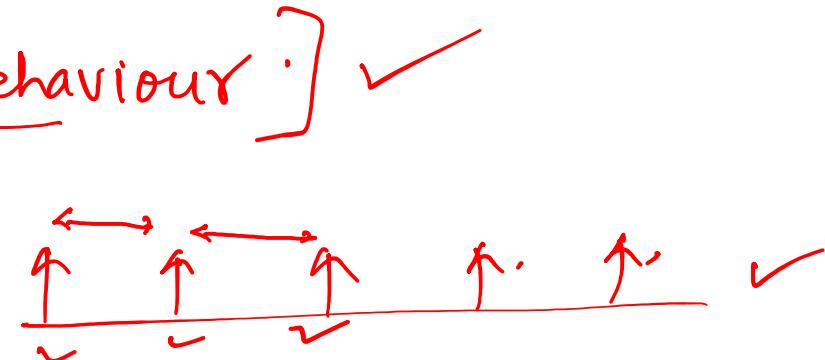
CS-230: Digital Logic Design & Computer Architecture



Lecture 17 (14 February 2022)

CADSL

Sequential Circuit

- temporal behaviour ✓
- ↑
Clock.
- 

Synchronous Sequential Circuit

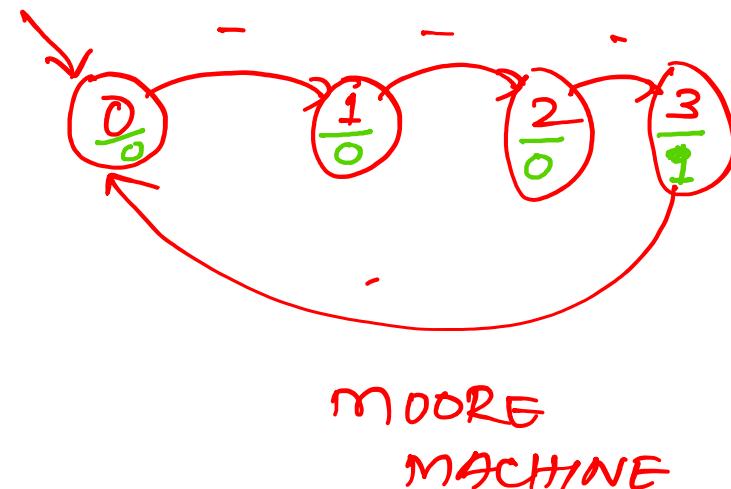
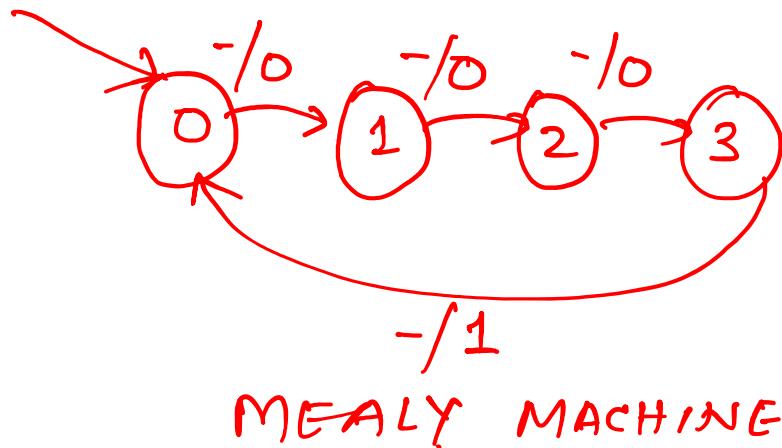
⇒ Asynchronous Sequential Circuits
(no clock).
Order · the event · (handshaking)



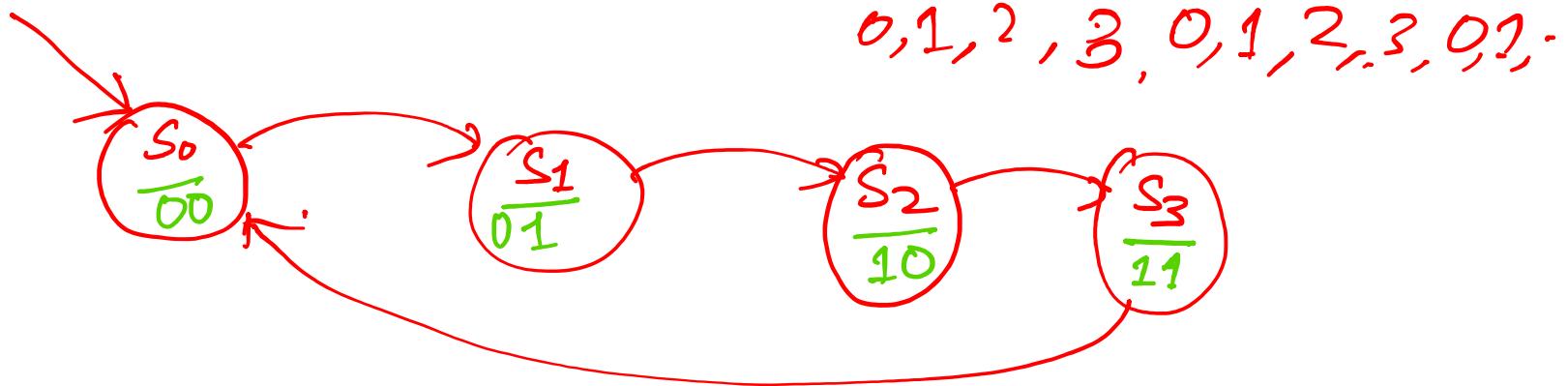
State Machine

$$M \underbrace{(I, O, S, S_0, \delta, \lambda)}$$
$$\lambda: S \rightarrow O$$
 MEALY
$$\lambda: S \times I \rightarrow O$$
 MOORE
MEALY

0,0,0,1,0,0,0,1 .

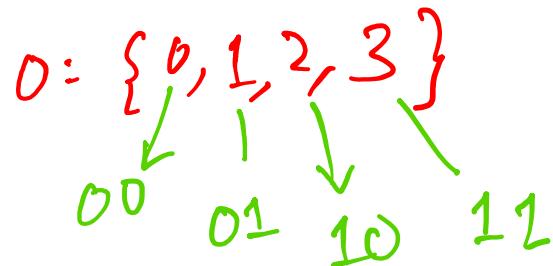


State Machine

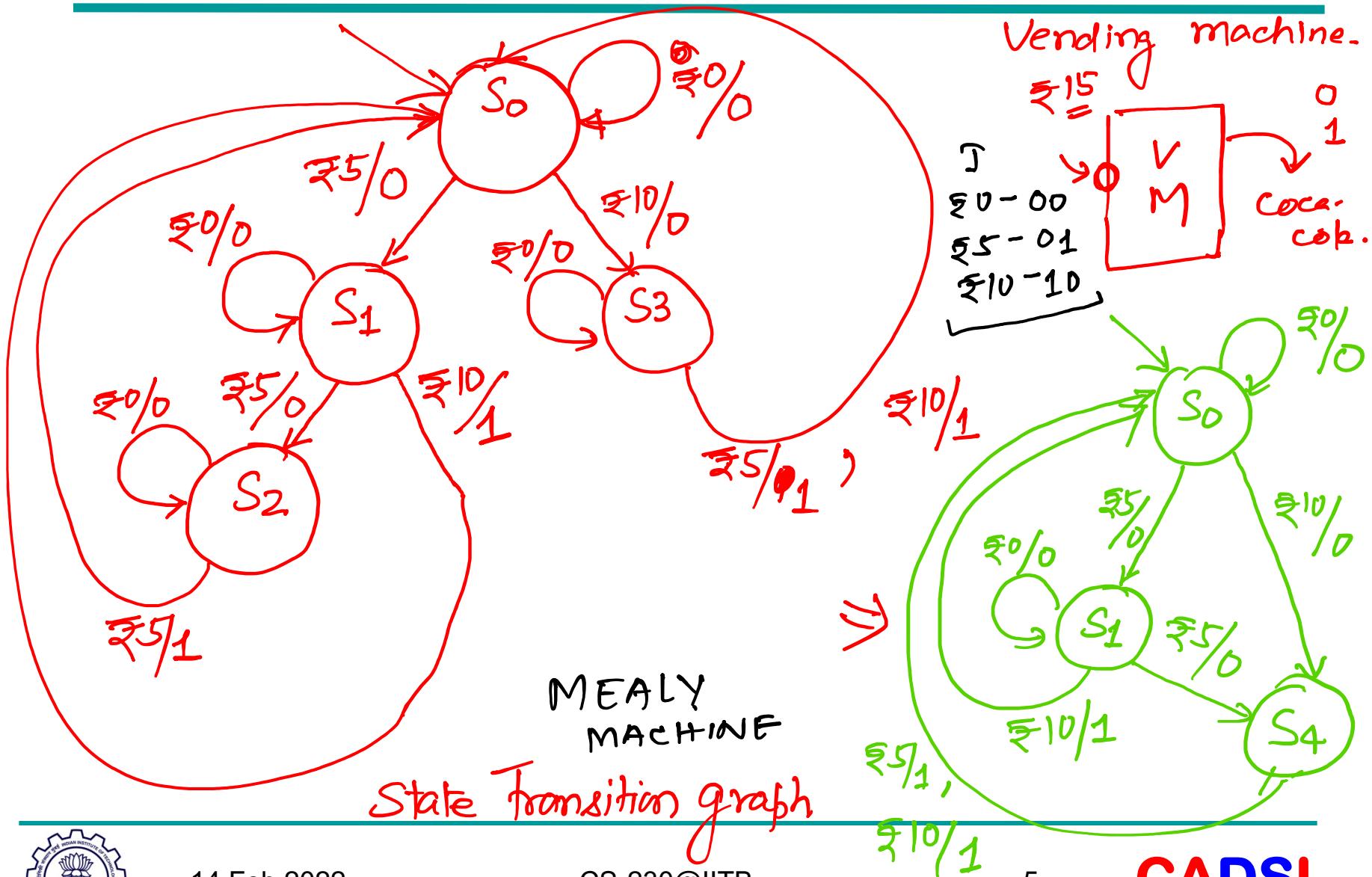


Free running Counter

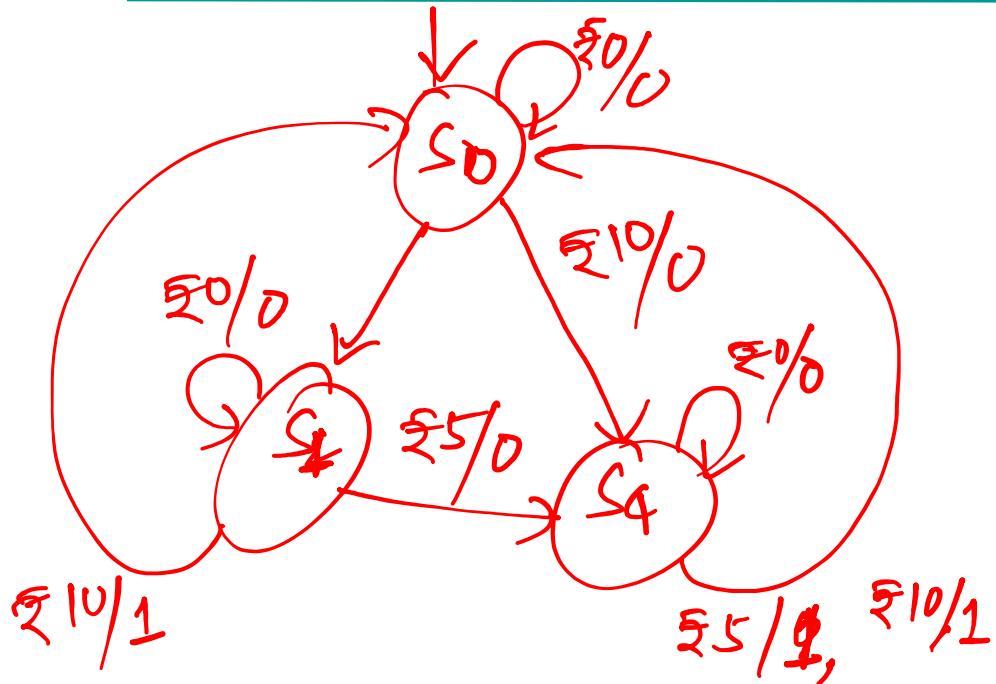
0, 1, 2, 3, 0, 1, 2, 3, - - -



Finite State Machine



Finite State Machine



3 States,
 $t_1 \underline{t_0}$

$S_0 -$	$\underline{00}$
$S_1 -$	01
$S_4 -$	10

I	a_1	a_0
00	00	
01	01	
10		10

PS	NS, Output		
	00/00	01 (2)	10 (2)
S_0 00	$S_0, 0$	$S_1, 0$	$S_4, 0$
S_1 01	$S_1, 0$	$S_4, 0$	$S_0, 1$
S_4 10	$S_4, 0$	$S_0, 1$	$S_0, 1$

$$M(I, O, S, S_0, \delta, \lambda)$$

$$I = \{00, 01, 10\} \quad O = \{0, 1\}$$

$$S = \{S_0, S_1, S_4\} \quad S_0 = \{S_0\}$$

$$\delta' \quad \delta, \lambda$$



Finite State Machine

$$S^{t_1}(t_1, t_0, a_1, q_0)$$

$$S^o(t_1, t_0, a_1, q_0)$$

$$\lambda(t_1, t_0, a_1, q_0)$$

$\lambda = t_0 q_1 + t_1 q_1 + t_1 q_0$

		a_1	a_0
		00	01
t_1	t_0	00	01
	00	0	0
	01	0	0
	11	X	X
	10	1	1

Annotations:

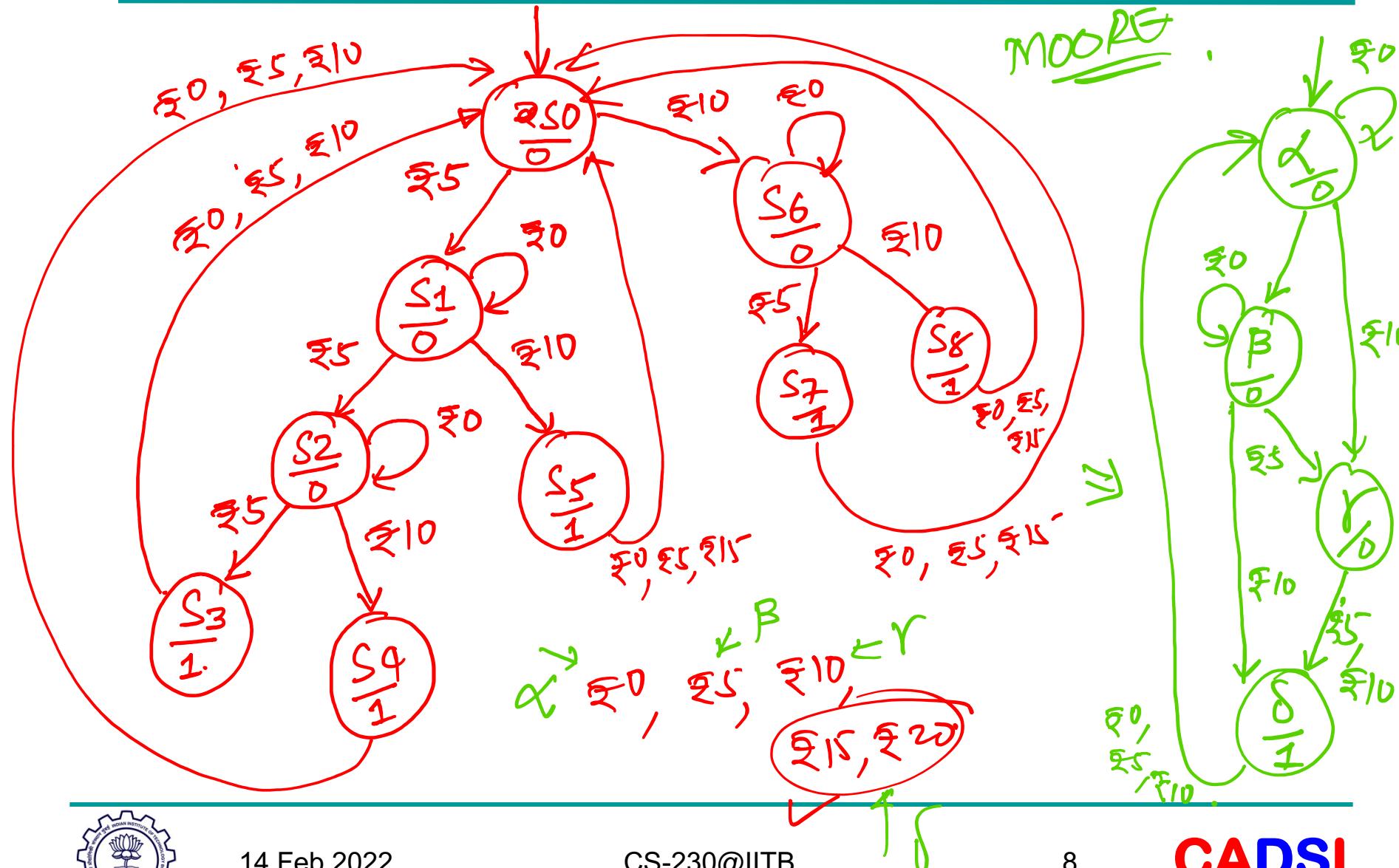
- A green arrow points from t_1, t_0 to the top-left cell (00).
- Blue arrows point from a_1, a_0 to the columns and rows respectively.
- Black ovals highlight specific states:
 - Top row: 00, 01
 - Left column: 00, 01
 - Bottom-right quadrant: 11, 10, 11, 10

$$\lambda = t_0 q_1 + t_1 q_1 + t_1 q_0$$

$$\begin{aligned} S^{t_1} &= \\ S^{t_0} &= \end{aligned}$$



Finite State Machine



Finite State machine

MOORE MACHINE

$$\xrightarrow{\quad \alpha, \beta, f, \delta \quad}$$
$$\stackrel{00}{\leftarrow} = \stackrel{01}{-} \stackrel{10}{-} \stackrel{11}{-}$$

t_1, t_0

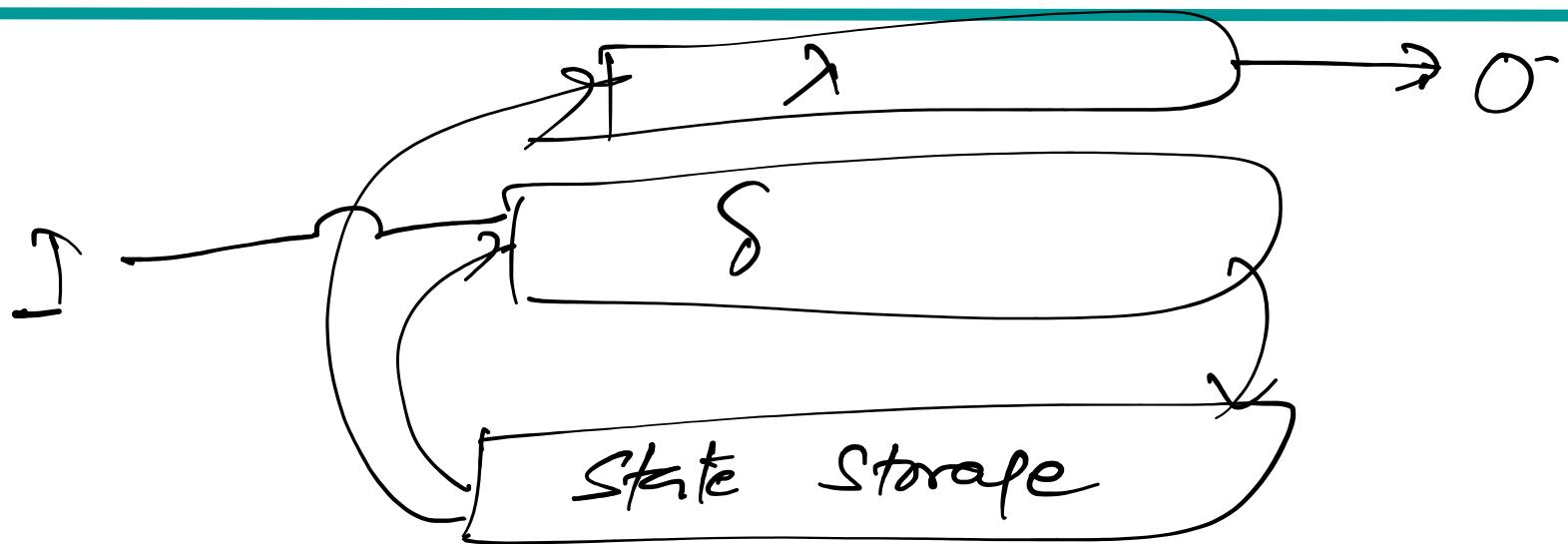
$$\left. \begin{array}{l} \delta^t(t_1, t_0, q_1, q_0) \\ \delta^t(t_1, t_0, q, q_0) \\ \gamma(t_1, t_0) \end{array} \right\}$$

a, a_0

$$I = \{ \begin{matrix} 00 & 01 \\ 01 & 01 \\ 10 & 10 \end{matrix} \}$$



Finite State machine



Thank You

