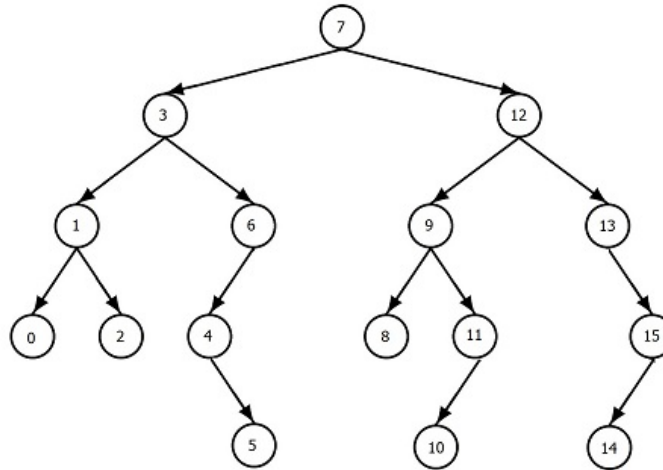


## Assignment 2

### CS 213: Data Structures and Algorithms

1. Given a BST  $T$  and an element  $a$ , the task is to delete all elements  $b < a$  from  $T$ . Write a function `del_less(T, a)` in pseudo-code to perform this. What is the time complexity of your algorithm? Execute your algorithm for  $a = 11$  on the following tree and show function calls with their input arguments.



2. We say that an AVL tree is deeply imbalanced if, at every internal node  $x$ , the left subtree  $T_L$  and the right subtree  $T_R$  are of different heights. Combining this with the AVL condition, the following holds at every internal node having subtrees  $T_L$  and  $T_R$ :

$$|ht(T_L) - ht(T_R)| = 1$$

- (a) List all deeply imbalanced AVL tree structures of heights 1, 2, and 3.
- (b) Is there a recurrence relation on the number of deeply imbalanced AVL trees having height  $h$ ? If so, state and prove this relation. See if  $h = 1, 2, 3$  satisfy it, and compute this number for  $h = 4$ .