## Probability Assignment-1

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*(i)* 

(ii)

Question—An urn contains 25 balls of which 10 balls bear a mark 'X' and the remaining 15 bear a mark 'Y'. A ball is drawn at random from the urn, its mark is noted down and it is replaced. If 6 balls are drawn in this way, find the probability that

- (i) all will bear 'X' mark.
- (ii) not more than 2 will bear 'Y' mark.(iii) at least one ball will bear 'Y' mark.
- (iv) the number of balls with 'X' mark and 'Y' mark will be equal.

SOLUTION -:

Given,

Balls in the urn (N) = 25,

Balls marked with  $X(N_X) = 10$ 

Balls marked with  $Y(N_Y) = 15$ 

Probability of an event E, Pr(E) is defined as

VariablesDefinitionnNo. Of trialszNo. Of balls marked X in n trialspPr(()X)qPr(()Y) = 1 - Pr(X)

 $\Pr(Z=6) = \binom{6}{0} (\frac{2}{5})^6 (\frac{3}{5})^0 \tag{1}$ 

$$= (\frac{2}{5})^6 \tag{2}$$

$$=\frac{64}{15625}$$
 (3)

 $Pr(E) = \frac{\text{Number of outcomes favourable to event } E}{\text{Total number of outcomes}}$ 

$$\Pr(X) = \frac{N_X}{N} = \frac{10}{25} = \frac{2}{5}$$

$$\Pr(Y) = \frac{N_Y}{N} = \frac{15}{25} = \frac{3}{5}$$

Here, in this problem we are drawing 6 balls with replacement having only two outputs either ball marked with X or Ball marked with Y So this trials can be thought of as Binomial trials.

Let, Z be the Random variable that represents the number of balls marked as X in 6 trials.

$$\Pr\left(Z=z\right) = \binom{n}{z} p^z \, q^{n-z}$$

Where,In all the following Subquestion value of n is 6

$$Pr(Z >= 4) = Pr(Z = 4) + Pr(Z = 5) + Pr(Z = 6)$$

$$= \binom{6}{0} (\frac{2}{5})^6 (\frac{3}{5})^0 \tag{5}$$

$$=\left(\frac{2}{5}\right)^6\tag{6}$$

$$=\frac{64}{15625}\tag{7}$$

(iii)

$$Pr(Z \le 6) = 1 - Pr(Z = 4)$$
 (8)

$$=1-\binom{6}{6}(\frac{2}{5})^6(\frac{3}{5})^0\tag{9}$$

$$=\frac{15561}{15625}\tag{10}$$

(iv)

$$Pr(Z = 3) = {6 \choose 3} (\frac{2}{5})^3 (\frac{3}{5})^3$$

$$= \frac{4320}{15625}$$

$$= \frac{864}{3125}$$
(11)

$$=\frac{4320}{15625}\tag{12}$$

$$=\frac{864}{3125}\tag{13}$$