## Probability Assignment-2

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Question—In answering a question on a multiple choice test, a student either knows the answer or guesses. Let  $\frac{3}{4}$ be the probability that he knows the answer and  $\frac{1}{4}$  be the probability that he guesses. Assuming that a student who guesses at the answer will be correct with probability  $\frac{1}{4}$ . What is the probability that the student knows the answer given that he answered it correctly?

## SOLUTION -:

Given,

Let  $X \in \{0,1\}$  where 0 denotes a guess and 1 denotes that he knows the answer. Let  $Y \in \{0, 1\}$ where 0 being the case when the answer is incorrect and 1 being the case that the answer is correct.

From the given information,

| Random Variable | Description                |
|-----------------|----------------------------|
| X = 0           | Student guesses the answer |
| X = 1           | Student knows the answer   |
| Y = 0           | Answer is incorrect        |
| Y = 1           | Answer is correct          |
|                 | TABLE 0                    |

RANDOM VARIABLE AND THEIR DESCRIPTION

| Pr(Event)                      | Value |
|--------------------------------|-------|
| Pr( <i>Y</i> =1   <i>X</i> =0) | 0.25  |
| $Pr(Y=1 \mid X=1)$             | 1     |
| Pr(X=0)                        | 0.25  |
| Pr(X=1)                        | 0.75  |

TABLE 0 PROBABILITY OF EVENTS

The probability that the student knows the answer and he answered it correctly is

$$\Pr\left(X=1|Y=1\right) \tag{1}$$

$$= \frac{\Pr(Y=1|X=1)\Pr(X=1)}{\sum_{i=0}^{i=1} \Pr(Y=1|X=i) \Pr(X=i)}$$
(2)  
$$= \frac{0.75}{0.25 \times 0.25 + 1 \times 0.75}$$
(3)

$$=\frac{0.75}{0.25\times0.25+1\times0.75}\tag{3}$$

$$= 0.92308$$
 (4)