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1 import numpy as np
2 from scipy.optimize import fsolve
3 from scipy.integrate import odeint
4
5 def theta_beta_mach(beta, M1, gamma, theta):
6     left = 2 * np.tan(beta) * (M1**2 * np.sin(beta)**
7     2 - 1)
8     right = M1**2 * (gamma + np.cos(2*beta)) + 2
9     return np.arctan(left / right) - theta
10
11 def normal_shock_M2(M1n, gamma):
12     numerator = 1 + ((gamma-1)/2)*M1n**2
13     denominator = gamma*M1n**2 - (gamma-1)/2
14     return np.sqrt(numerator / denominator)
15
16 def taylor_maccoll(y, theta, gamma=1.4):
17     v_r, v_theta = y
18     denom = (gamma - 1) / 2 * (1 - v_r ** 2 - v_theta
19     ** 2) - v_theta ** 2
20     if np.abs(denom) < 1e-8: denom = 1e-8
21     deriv_vr = v_theta
22     deriv_vtheta = (
23         v_theta ** 2 * v_r
24         - (gamma - 1) / 2 * (1 - v_r ** 2 - v_theta
25         ** 2)
26         * (2 * v_r + v_theta / np.tan(theta))
27     ) / denom
28     return [deriv_vr, deriv_vtheta]
29
30 def cone_shock(cone_angle_deg, M1, gamma=1.4, N=1000
31 ):
32     theta = np.deg2rad(cone_angle_deg)
33     beta_guess = [theta + np.deg2rad(1), np.deg2rad(
34     80)]
35     beta_sol = fsolve(theta_beta_mach, np.mean(
36     beta_guess), args=(M1, gamma, theta))[0]
37     M1n = M1 * np.sin(beta_sol)

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36     M2n = normal_shock_M2(M1n, gamma)
37     # Flow behind the shock
38     VR0 = M2n / M1      # Nondimensional radial
    velocity
39     Vtheta0 = 0         # At the shock, all velocity
    change is normal
40     y0 = [VR0, Vtheta0]
41     thetas = np.linspace(beta_sol, theta, N)
42     sol = odeint(taylor_maccoll, y0, thetas, args=(
    gamma,))
43
44     vtheta_surface = sol[-1, 1]
45     return {
46         "shock_angle_deg": np.rad2deg(beta_sol),
47         "beta_rad": beta_sol,
48         "M1n": M1n,
49         "M2n": M2n,
50         "cone_surface_vtheta": vtheta_surface,
51         "thetas": thetas,
52         "Vr": sol[:,0],
53         "Vtheta": sol[:,1],
54     }
55
56 # inputs here
57 #####
58 cone_angle_deg = 35
59 M1 = 2
60 results = cone_shock(cone_angle_deg, M1)
61 #####
62
63
64 print(f"Shock angle: {results['shock_angle_deg']:.2f}
    deg")
65 print(f"Normal Mach behind shock: {results['M2n']:.4f
    }")
66 print(f"Vtheta at cone surface (should be 0): {
    results['cone_surface_vtheta']:.4e}")
67
68 import matplotlib.pyplot as plt
69 plt.plot(np.rad2deg(results['thetas']), results['Vr'
    ], label="Vr")

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70 plt.plot(np.rad2deg(results['thetas']), results['  
    Vtheta'], label="Vtheta")  
71 plt.xlabel("theta (deg)")  
72 plt.ylabel("Velocity (nondimensional)")  
73 plt.legend()  
74 plt.title("Taylor-Maccoll velocities from shock to  
    cone surface")  
75 plt.show()  
76  
77
```