

# Arrays: 2D Matrices

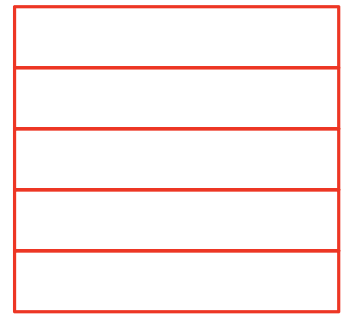
2-D Matrix : Array of arrays



Array



Arrays



2D-Matrix

all arrays are  
of same size

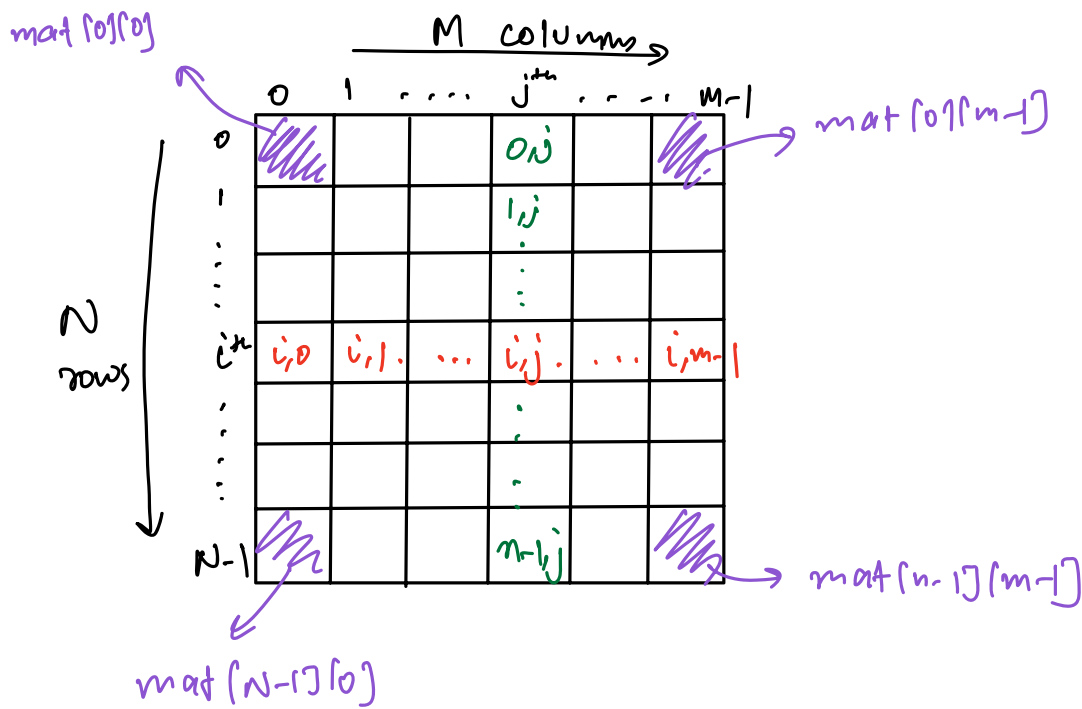
Say, size of each array  
in a matrix  $\rightarrow M$  (no. of columns)

Total no. of arrays  $\rightarrow N$  (no. of rows)

Declare: `int mat[N][M]` (TODO  $\rightarrow$  learn in your own language)

$\swarrow$   $\searrow$

no. of rows      no. of columns



### Observation

- If we move in  $i^{th}$  row, column index will change from  $[0, m-1]$ .
- If we move in  $j^{th}$  column, row index will change from  $[0, n-1]$ .

### Question 1

Given  $mat[N][M]$ , print row-wise sum.

eg

	0	1	2	
0	1	5	9	→ 15
1	2	8	2	→ 12
2	7	6	2	→ 15

Code

```

for (i=0; i<n; ++i) {
    // ith row
    sum = 0
    for (j=0; j<m; ++j)
        sum += mat[i][j]
    print(sum)
}

```

TC:  $O(N \times m)$

SC:  $O(1)$

Question 2

Given square matrix,  $mat[N][N]$ , print diagonals.

Square matrix: (# of rows) = (# of columns)

	0	1	2	3
0	0,0			0,3
1		1,1	1,2	
2		2,1	2,2	
3	3,0			3,3

left  $\rightarrow$  right diagonals

right  $\rightarrow$  left

```

for (i=0; i<n; ++i) {

```

```

    for (j=0; j<n; ++j) {

```

TC:  $O(N^2)$

```

        if (i==j)

```

```

            print(mat[i][j])
        }
    }
}

```



$i=0, j=0$   
 while ( $i < n$  <sup>optional</sup> &  $j < n$ ) {  
     print(mat[i][j])  
      $i++$ ,  $j++$   
 }  
 OR  
 for ( $i=0; i < n; i++$ )  
     print(mat[i][i])  
 }  
 TC:  $O(N)$   
 SC:  $O(1)$

for right  $\rightarrow$  left diagonal,  $i+j = n-1$

$i=0, j=n-1$  <sup>optional</sup>  
 while ( $i < n$  &  $j \geq 0$ ) {  
     print(mat[i][j])  
      $i++$ ,  $j--$   
 }  
 }  
 right  $\rightarrow$  left  
 TC:  $O(N)$   
 SC:  $O(1)$

### Question 3

Given mat  $[N][M]$ , print all diagonals going from  $R \rightarrow L$ .

Note: Diagonals will start from 0th row OR  $m-1^{th}$  column.

	0	1	2	3	4	5	6
0	0,0	0,1	0,2	0,3	0,4	0,5	0,6
1	1,0	1,1					1,6
2	2,0					2,5	2,6
3					3,4		3,6

mat[4][7]

Diagonal starting point:

(0,0) (0,1) (0,2) . . . (0,6)  
 (1,6) (2,6) (3,6)

1. Print all diagonals from 0th row

```
for(k=0; k<m; ++k) {
```

```
    // starting: (0,k)
```

```
    i=0, j=k
```

```
    while(i<n && j<=0)
```

```
        print(mat[i][j])
```

```
        i++, j--
```

```
    }
    print(newline)
```

```
}
```

k=0-6

k=0	i=0, j=0	(0,0)
1	i=0, j=1	(0,1) (1,0)
2	i=0, j=2	
3		
4		
5		
6		

2. Print all diagonals from  $m-1^{\text{th}}$  column

```
for ( k=1; k < n; ++k ) {
```

```
    i = k, j = m-1
```

```
    while ( i < n & j >= 0 ) {
```

```
        print(mat[i][j])
```

```
        i++, j--
```

```
    }  
    print(newline)
```

```
}
```

k=1    i=1, j=6    (1,6) (2,5) (3,4)

2    :

3    :

total TC :  $O(N \times M)$

total SC :  $O(1)$

BREAK: 8:14 - 8:24

## Question 4

Given a  $\text{mat}[N][N]$ , calculate transpose of a matrix without extra space.

Transpose is:

0<sup>th</sup> row  $\rightarrow$  0<sup>th</sup> column

1<sup>st</sup> row  $\rightarrow$  1<sup>st</sup> column

$\vdots$

$n-1$ <sup>th</sup> row  $\rightarrow$   $n-1$ <sup>th</sup> column

	0	1	2	3	4
0	1	2	3	4	5
1	6	7	8	9	10
2	11	12	13	14	15
3	16	17	18	19	20
4	21	22	23	24	25

transpose  $\rightarrow$

	0	1	2	3	4
0	1	6	11	16	21
1	2	7	12	17	22
2	3	8	13	18	23
3	4	9	14	19	24
4	5	10	15	20	25

$\text{mat}[5][5]$

$[i, j] \rightarrow [j, i]$

Code

```
for (i=0; i<n; ++i) {
```

```
    for (j=0; j<n; ++j) {
```

```
        swap(mat[i][j], mat[j][i])
```

```
    }  
}
```

~~X~~  
Not work

$i=1, j=3$

$\text{swap}(\text{mat}[1][3], \text{mat}[3][1])$

$\vdots$

$i=3, j=1$

$\text{swap}(\text{mat}[3][1], \text{mat}[1][3])$

double swapping

↓ solution

either swap when  $i < j$  OR  $i > j$

for ( $i=0; i < n; ++i$ ) {

for ( $j=0; j < n; ++j$ ) {

if ( $i < j$ ) {

swap( $\text{mat}[i][j], \text{mat}[j][i]$ )

}

}

↓

for ( $i=0; i < n; ++i$ ) {

for ( $j=i+1; j < n; ++j$ ) {

swap( $\text{mat}[i][j], \text{mat}[j][i]$ )

}

}

✓ WORK

TC:  $O(N^2)$

SC:  $O(1)$



# Question 5

Given square matrix  $mat(N)(N)$ , rotate  $90^\circ$  clockwise from top left. SC:  $O(1)$

	0	1	2	3
0	1	2	3	4
1	5	6	7	8
2	9	10	11	12
3	13	14	15	16

$90^\circ$   
clockwise

	0	1	2	3
0	13	9	5	1
1	14	10	6	2
2	15	11	7	3
3	16	12	8	4

same

transpose

	0	1	2	3
0	1	5	9	13
1	2	6	10	14
2	3	7	11	15
3	4	8	12	16

reverse  
each row

	0	1	2	3
0	13	9	5	1
1	14	10	6	2
2	15	11	7	3
3	16	12	8	4

$90^\circ$  clockwise  
rotation

= transpose + reverse

$\downarrow$   
 $O(N^2)$   
 $O(1)$

$\downarrow$   
 $O(N^2)$   
 $O(1)$

total TC:  $O(N^2)$   
SC:  $O(1)$



mat



mat X

Doubt

$$10^5 \times 10^5$$

$10^5$  times

times

$$10^5 \times 10^5 = 10^{5+5} = 10^{10}$$

$$10^{5 \times 10^5}$$

$$\% 10^9 + 7$$