

## Arrays: Carry forward

### Question 1

Given a char array  $s$ , calculate # of pairs  $(i, j)$  such that  $i < j$  &  $s[i] = 'a'$  &  $s[j] = 'g'$ .

All chars are lower case  $[a, z]$

eg ~~a~~    b    a    a    g    d    c    a    g  
0    1    2    3    4    5    6    7

ans = 5

$(2, 3)$  ,  $(6, 7)$  ,  $(1, 3)$  ,  $(1, 7)$  ,  $(2, 7)$

b    c    a    g    g    a    a    g  
0    1    2    3    4    5    6    7

ans = 5

$(2, 3)$     $(2, 4)$     $(5, 7)$     $(6, 7)$  ,  $(2, 7)$

a    c    g    d    g    a    g  
0    1    2    3    4    5    6

ans = 4

$(0, 2)$      $(0, 4)$      $(0, 6)$      $(5, 6)$

Iterate over every pair and check whether its valid or not.

ans = 0

```
for (i = 0; i < n; ++i) {  
    for (j = i + 1; j < n; ++j) {  
        if (s[i] == 'a' & s[j] == 'g')  
            ++ans  
    }  
}
```

TC:  $O(N^2)$

SC:  $O(1)$

Observation 1: Break loop if  $s[i] \neq 'a'$

ans = 0

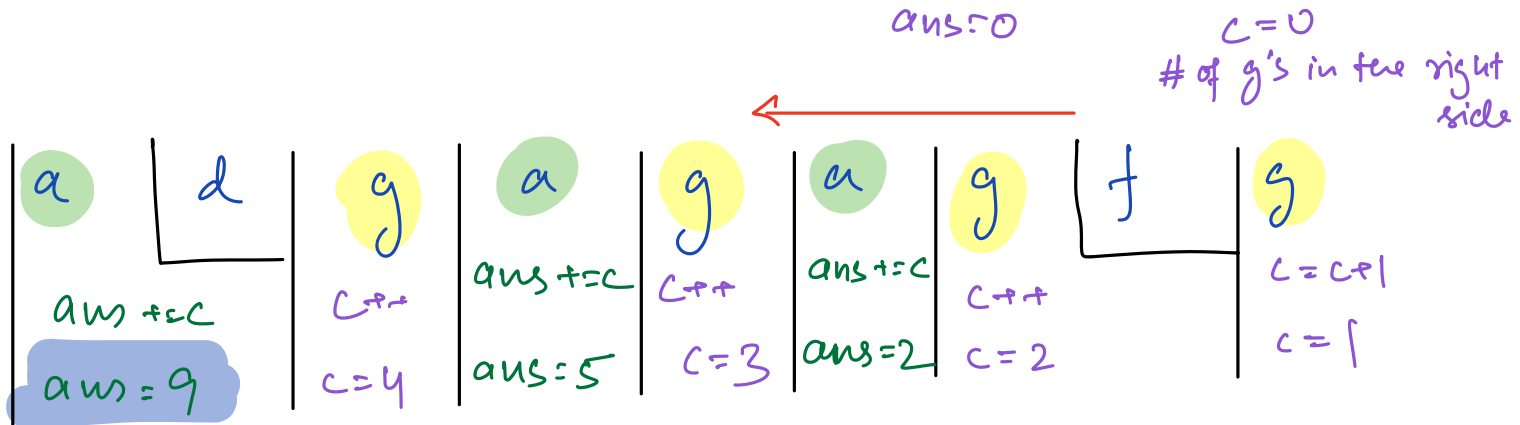
```
for (i = 0; i < n; ++i) {  
    if (s[i] == 'a') {  
        for (j = i + 1; j < n; ++j) {  
            if (s[j] == 'g')  
                ++ans  
        }  
    }  
}
```

TC:  $O(N^2)$

SC:  $O(1)$

HW: try using suffix array

Observation 2: We need count of g's in the right side of every 'a'. finally sum all of them.



$ans = 0, c = 0$

for ( $i = n - 1; i \geq 0; --i$ ) {

if ( $s[i] == 'g'$ )

$c++$

else if ( $s[i] == 'a'$ )

$ans += c$

}

print(ans)

TC:  $O(N)$

SC:  $O(1)$


HW: Can you traverse from left to right?

## Question 2 leaders in an Array

Given an array  $a[N]$ , you have to find count of leaders in array.

An element is a leader if it is strictly greater than entire right side.

Note:  $a[n-1]$  is always a leader.

eg  count = 5

 ans = 3

 ans = 5

Code

```
mx = a[n-1]
```

```
ans = 1
```

```
for (i = n-2; i >= 0; --i) {
```

```
    if (a[i] > mx) {
```

```
        ans++
```

```
        mx = a[i]
```

```
    }
```

```
print(ans)
```

TC:  $O(N)$

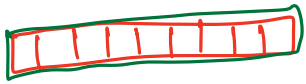
SC:  $O(1)$

# Subarray

Continuous part of an array is called subarray.



→ single element is a subarray



→ full array is a subarray

→ empty array is **not** subarray

eg indices:

[2, 3, 4, 5] ⇒ subarray ✓

[3, 4, 6, 7, 8] ⇒ subarray ✗

[1, 2, 3] ⇒ subarray ✓

[5] ⇒ subarray ✓

4 5 1 9 0 2 3 5

[5] ✓

[4, 5, 1, 0] ✗

[9, 0, 2, 3] ✓

[4, 5, 1] ✓

If I have a subarray from index  $i$  to index  $j$

Can I write subarray as  $\rightarrow [i, j]$  ✓

because all indices  
are included in  $[i, j]$

length of a subarray  $[i, j] \Rightarrow j - i + 1$

$$[1, 4] \Rightarrow 4 - 1 + 1 = 4$$

$\Downarrow$

1, 2, 3, 4

You can use these pre-defined functions

$\rightarrow \min(a, b)$

TC:  $O(1)$  SC:  $O(1)$

$\rightarrow \max(a, b)$

TC:  $O(1)$  SC:  $O(1)$

$\rightarrow \text{sort}()$  array

TC:  $O(N \log N)$  SC:  $O(1)$

BREAK: 8:05 - 8:15

### Question 3 Closest Min Max

Given an array, find the length of the smallest subarray which contains both Min and Max of array.

eg

1	2	3	1	3	4	6	4	6	3
0	1	2	3	4	5	6	7	8	9

$[3, 6] \rightarrow$  smallest subarray

$$\text{length} = 6 - 3 + 1 = 4$$

min = 1  
max = 6

2 2 6 4 5 1 5 2 6 4 1

min = 1  
max = 6

length = 3

8 8 8 8

min = 8  
max = 8

length = 1

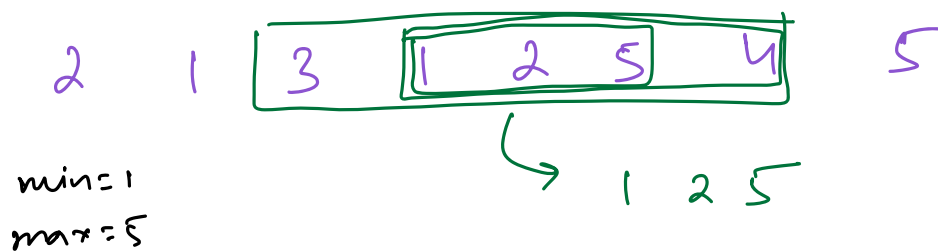
### Observation

1. we only need to have 1 min and 1 max.

..... Min ... [Max ... <sup>Min</sup>Min] ... Max .....

If you have more than 1 Min or 1 Max value in the answer, then you can always shrink the subarray.

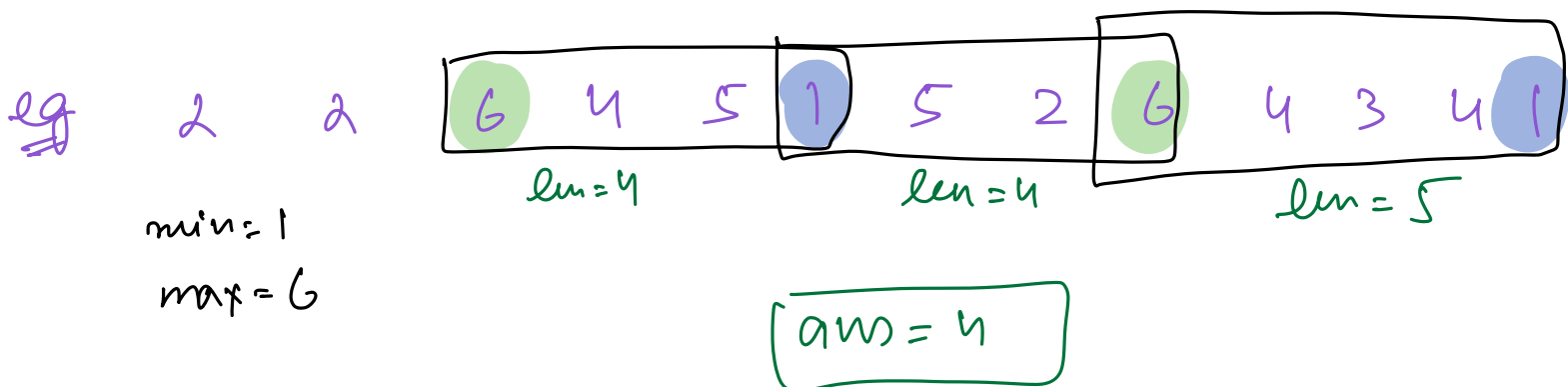
2. Min & Max are always present at corners.



You can shrink your subarray until max & min are not at corners.

3. 2 cases:

→ [min ..... Max] → for every min value, find the closest max value in the right.  
→ [Max ..... Min]





Bruteforce

ans = N

// iterate & get min & max → TODO

if ( min == max )

return 1

for ( i = 0; i < n; ++i ) {

if ( a[i] == min ) {

for ( j = i + 1; j < n; ++j ) {

if ( a[j] == max ) {

ans = min ( ans, j - i + 1 )

break

}

}

}

else if ( a[i] == max ) {

for ( j = i + 1; j < n; ++j ) {

if ( a[j] == min ) {

ans = min ( ans, j - i + 1 )

break

}

}

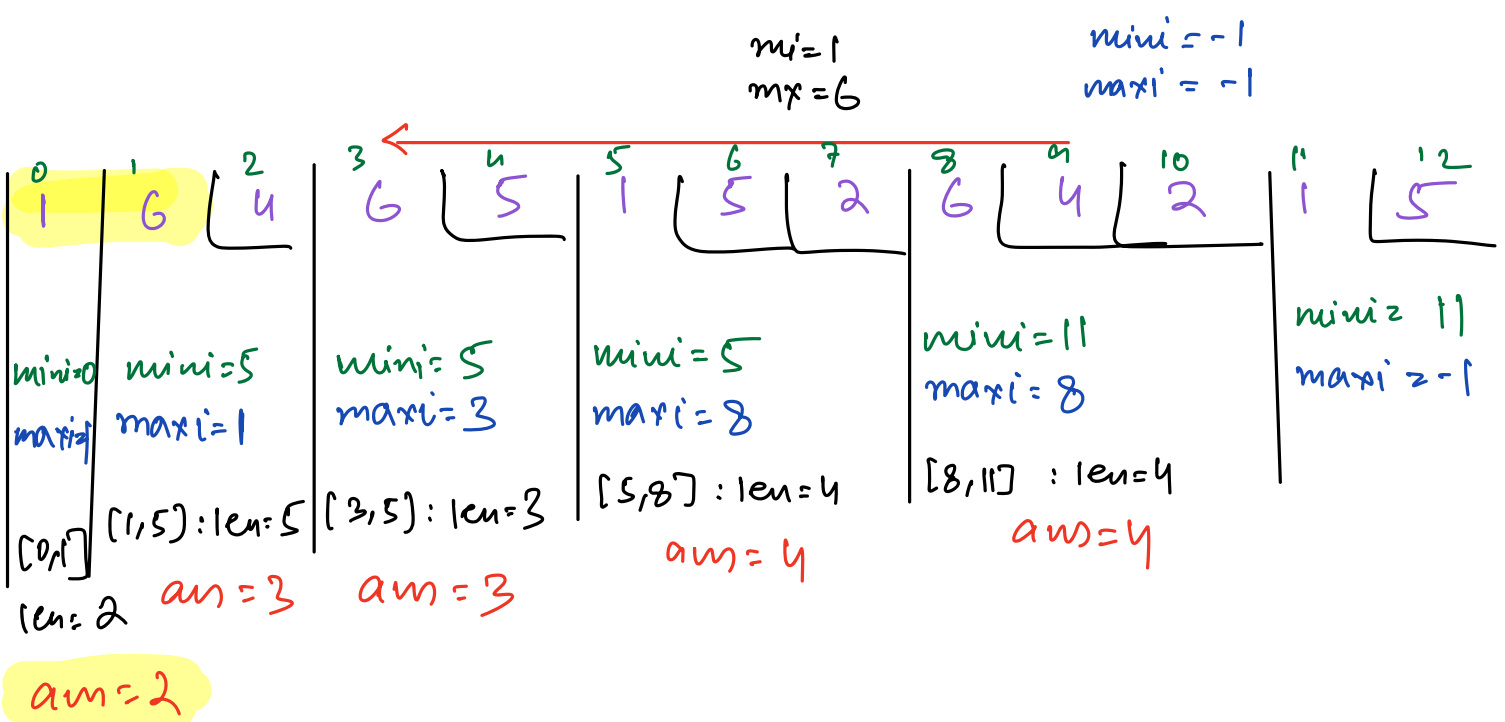
}

}

return ans

TC:  $O(N^2)$

SC:  $O(1)$



Code

// iterate & find min & max value  $\rightarrow$  TC:  $O(N)$  SC:  $O(1)$

if ( $mi == mx$ )

return 1

$mini=-1$ ,  $maxi=-1$ ,  $ans=N$

for ( $i=n-1$ ;  $i \geq 0$ ;  $--i$ ) {

if ( $a[i] == mi$ ) {

$mini=i$

if ( $maxi \neq -1$ )

$ans = \min(ans, \overset{\substack{\text{abs}(maxi-mini)+1 \\ \uparrow}}{maxi - mini + 1})$

}

else if ( $a[i] == mx$ ) {

$maxi=i$

if ( $mini \neq -1$ )

$ans = \min(ans, \overset{\substack{\text{abs}(maxi-mini)+1 \\ \uparrow}}{mini - maxi + 1})$

}

TC:  $O(N)$

SC:  $O(1)$

3

return am