

Hashing-1

Content

- Hashmap intro
- freq. of each element
- first non-repeating element
- # of distinct elements
- exist a subarray with sum 20

Scenario-1 : 1000 rooms labelled as: $[1, 1000]$
↳ occupied / not occupied

array \rightarrow `bool room[1001]`
↓
since rooms are
labelled as $[1, 1000]$
not $[0, 999]$

\Rightarrow `room[i] = true`
[if the room is occupied]
 \Rightarrow `room[i] = false`
[not occupied]

Scenario 2 : 1000 rooms labelled between $[1, 10^9]$

`bool room[10^9+1]`

↳ Issue: Huge space wastage

↳ Advantage: TC: $O(1)$ to find any room's occupancy

Hashmap

It stores $\langle \text{key}, \text{value} \rangle$ pairs

$\langle 10015, \text{occupied} \rangle$

$\langle 123, \text{unoccupied} \rangle$

\vdots

N entries
 $= 1000$

\Rightarrow check in 10015?

\rightarrow occupied in TC: $O(1)$

TC: $O(1)$ to search

SC: $O(N)$ to store for N rooms.

Note: Keys are unique. Value can be anything.

Q1 Store population of every country.

Key: country name \rightarrow string

value: population \rightarrow int/long

Hashmap \langle ^{key}string, ^{value}long \rangle $\underset{\substack{\uparrow \\ \text{variable name}}}{hm}; \quad \Rightarrow$ pseudo syntax

eg India, US, UK

$hm =$

- $\langle \text{"India"}, 1.5 \times 10^9 \rangle$
- $\langle \text{"US"}, 10^8 \rangle$
- $\langle \text{"UK"}, 10^7 \rangle$

Q₂ for every country, we want to know all states.

Key: country name \rightarrow string

Value: all states names \rightarrow array<string>

\hookrightarrow C++: vector

\hookrightarrow py: list

\hookrightarrow java: arraylist

HashMap<string, array<string>> hm

Q₃ for every country, store population of each state.

Key: country name \rightarrow string

Value: population of each state \rightarrow HashMap<string, long>

\uparrow
state
name

\uparrow
population

HashMap<string, HashMap<string, long>> hm

Observation 1: value can be anything

Observation 2: Key can only be primitive datatype

\downarrow
int / long / float / double / string / char

HashSet <Key>

- we only store keys
- Keys have to be unique
- only primitive datatype

HashMap functions

Size: {# of keys}

insert (Key, value)

search (Key) → value
↳ NOT FOUND

delete (Key) → delete key & value

update (Key, new Value)

↳ HashMap

~~<India, 800>~~

<US, 200>

<India, 900>

HashSet functions

Size: {# of keys}

insert (Key)

search (Key) → true
↳ false

delete (Key)

All operations above are $O(1)$

→ Hashing libraries name in diff languages.

Pseudocode	Java	C++	Python	JS	C#
HashMap	HashMap	unordered-map	dict	map	dictionary
HashSet	HashSet	unordered-set	set	set	HashSet

Question 1

Given N array elements & Q queries.

for each query, find freq. of given element in array.

eg $a[10] = \{ 2, 6, 3, 8, 2, 8, 2, 3, 8, 10, 6 \}$

Q = 4 freq

2 3

8 3

3 2

5 0

Constraints:

$1 \leq N \leq 10^5$ $1 \leq Q \leq 10^5$

$1 \leq a[i] \leq 10^9$

Idea 1: for each query, iterate & get count

TC: $O(Q*N)$ SC: $O(1)$

Can't create a count array since $a[i] \leq 10^9$.

Idea 2: Store data in hashmap

key \rightarrow array element \rightarrow int

value \rightarrow freq. of element \rightarrow int

{ 2 6 3 8 2 8 2 3 8 10 6 }

$\langle 2, 3 \rangle$	$\langle 8, 3 \rangle$
$\langle 6, 2 \rangle$	$\langle 10, 1 \rangle$
$\langle 3, 2 \rangle$	

Code

HashMap \langle int, int \rangle hm

for ($i=0$; $i<n$; $++i$) { $\rightarrow O(N)$

 // key = $a[i]$

 if (hm.containsKey($a[i]$) == true) {

 hm.put($a[i]$, hm.get($a[i]$) + 1) // update

 } else {

 hm.put($a[i]$, 1) // insert

 }

freq

```
for (i=0; i<Q.size; ++i) {  $\rightarrow O(1)$ 
```

```
    // key = Q[i]
```

```
    if (hm.search(Q[i]) == true) {
```

```
        print(hm[Q[i]])  $\rightarrow$  access value of key
```

```
    }
```

```
    else {
```

```
        print(i)
```

TC: $O(N+Q)$

SC: $O(N)$

Question 2: find the first non-repeating element.

\rightarrow first element from start

eg a[] = { 1, 2, 3, 1, 2, 5 }

freq = 2, freq = 2, freq = 1

ans = 3

a[] = { 4, 3, 2, 2, 5, 4 }

Idea 1: 1. Insert all elements in hashmap

2. Iterate hashmap to get first key with value = 1.

Note: Order of insertion of keys is not maintained in hashmap/unordered.

Idea 2: 1. Insert all elements in hashmap $\rightarrow O(N)$
2. Iterate over array & get first element with $hm[ai] = 1 \rightarrow O(N)$

TC: $O(N)$ SC: $O(N)$

Code \rightarrow TODO

Question 3:

Given a $[N]$ elements, find no. of distinct elements? ^{count}

eg $a[5] = \{ 3, 5, 6, 5, 4 \}$

ans = 4

$a[5] = \{ 1, 1, 1, 2, 2 \}$

ans = 2

Idea 1: 1. insert all elements in hashmap
2. count keys with value = 1

Idea 2: Insert all elements in hashset

$a[7] = \{ 6, 3, 7, 3, 8, 6, 9 \}$

HashSet<int> hs

hs = $\{ 6, 3, 7, 8, 9 \}$

hs.size = 5

Note: In HashSet, if same key is inserted multiple times, it will only store 1 occurrence.

Code

```
HashSet<int> hs
for (i=0; i<n; i++) {
    hs.insert(a[i])
}
print (hs.size)
```

TC: $O(N)$

SC: $O(N)$

Question 4

Given N elements, check if all elements are unique or not?

1. insert all elements in HashSet

2. check if $hs.size() == n \Rightarrow$ unique

else
Not unique

Question 5

Given $a(N)$ elements, check if there exists a subarray with $\text{sum} = 0$.

eg $a[10] =$

0	2	2	1	-3	4	3	1	-2	-3	2
		1	2	3	4	5	6	7	8	9

$2+1+3=0$ (points to indices 2, 3, 4)
 $-3+4+2+1+-2+-3=0$ (points to indices 4, 5, 6, 7, 8, 9)

ans = true

Idea: for every subarray, calculate sum

↙
nested loops
 $O(N^3)$

↓
prefix sum
 $O(N^2), O(N)$

↘
carry forward
 $O(N^2), O(1)$

TC: $O(N^2)$ SC: $O(1)$

	0	1	2	3	4	5	6	7	8	9
$a[10] =$	2	2	1	-3	4	3	1	-2	-3	2
$pf[10] =$	2	4	5	2	6	9	10	8	5	7

observation: In $pf[10]$, numbers are repeating

$$pf[0] = 2 = \text{sum}[0,0]$$

$$pf[3] = 2 = \text{sum}[0,3] = \text{sum}[0,0] + \text{sum}[1,3]$$

$$\cancel{2} = \cancel{2} + \text{sum}[1,3]$$

$$\boxed{\text{sum}[1,3] = 0}$$

$$a[4] = \{ 2 \ -5 \ 3 \ 6 \}$$

$$pf[1] = \{ 2 \ -3 \ 0 \ 6 \}$$

↳ in $pf[1]$, there is no repetition but subarray with $\text{sum} = 0$ exist?

$$pf[2] = 0 = \text{sum}[0,2]$$

Note: In $pf[1]$, even if single 0 is present, there exists a subarray with $\text{sum} = 0$

final Idea:

If ele repeat in $pf[1]$

OR

If 0 is present in $pf[1]$

→ there exist a subarray with $\text{sum} = 0$

Code

```
bool subarrayZero (a[] ) {
```

```
    n = a.length
```

```
    pf[n] // create pf[] → TODO
```

```
    HashSet<int> hs
```

```
    for (i=0; i<n; ++i) {
```

```
        if (pf[i] == 0) { return true; }
```

```
        hs.insert (pf[i])
```

```
    }
```

```
    if ( hs.size() < N ) { // repetition in pf[]
```

```
        return true
```

```
    }
```

```
    return false
```

```
}
```

TC: $O(N)$

SC: $O(N)$