

→ Numericals:

1. Calculate the conductivity of silicon doped with 10^{21} atoms m^{-3} of boron if the mobility of holes is $0.048 m^2 V^{-1} s^{-1}$

$$\begin{aligned}\sigma &= ne\mu_h \\ &= 10^{21} \times 1.6 \times 10^{-19} \times 0.048 \\ &= 0.768 \times 10^2 = \underline{\underline{7.68 \text{ ohm}^{-1} \text{m}^{-1}}}\end{aligned}$$

2. Calculate the resistivity of intrinsic germanium if the intrinsic carrier density is $2.5 \times 10^{19} m^{-3}$ assuming electron and hole mobilities of 0.38 and $0.18 m^2 V^{-1} s^{-1}$ respectively.

$$\begin{aligned}\rho &= \frac{1}{\sigma} = \frac{1}{ne(\mu_e + \mu_h)} \\ &= \frac{1}{2.5 \times 10^{19} \times 1.6 \times 10^{-19} (0.38 + 0.18)} \\ &= \frac{1}{4 \times 10^{-19} \times 10^{+19} (0.56)} \\ &= \frac{1}{2.24} = \underline{\underline{0.446 \text{ ohm m}}}\end{aligned}$$

3. Calculate the conductivity of germanium with the given data. What is the effect of doping germanium with donor-type impurity to the extent of one atom per 10^8 germanium atoms?

$$\text{Given} : n_i = 2.4 \times 10^{19} \text{ m}^{-3}$$

$$\mu_e = 0.38 \text{ m}^2 \text{V}^{-1} \text{s}^{-1}, \mu_h = 0.19 \text{ m}^2 \text{V}^{-1} \text{s}^{-1}$$

$$\text{no of atoms: } 4.4 \times 10^{28}$$

$$e = 1.6 \times 10^{-19} \text{ C}$$

$$\sigma_i = n_i e (\mu_e + \mu_h)$$

$$= 2.4 \times 10^{19} \times 1.6 \times 10^{-19} (0.38 + 0.19)$$

$$= 3.84 (0.57)$$

$$= 2.227 = \underline{\underline{2.23 \text{ ohm}^{-1} \text{m}^{-1}}}$$

4. The electrical conductivity of an intrinsic semiconductor increases from $19.96 \text{ ohm}^{-1} \text{m}^{-1}$ to $79.44 \text{ ohm}^{-1} \text{m}^{-1}$ when the temp is increased from 60 to 100°C . Find the band gap energy of Semiconductor.

$$\sigma = k \cdot \exp(E_g / 2kT)$$

$$\Delta(\ln \sigma) = -E_g$$

$$\Delta(1/T) = -1/k$$

$$E_g = \frac{-(\ln \sigma_2 - \ln \sigma_1) \times 2 \times k}{(1/T_2 - 1/T_1)}$$

$$\begin{aligned}
 &= -\frac{(-4.3750 + 2.9937) \times d \times 1.38 \times 10^{-23}}{(3.003 - 2.681) \times 10^{-3}} \\
 &= \frac{1.3813}{0.322 \times 10^{-3}} \times 2.76 \times 10^{-23} \\
 &= 11.839 \times 10^{-20} \\
 &= 1.1839 \times 10^{-19} \\
 &= \frac{1.1839 \times 10^{-19}}{1.6 \times 10^{-19}} = 0.739 \\
 &\approx 0.74 \text{ eV}
 \end{aligned}$$

(silicon)

5. Intrinsic semiconductor has a carrier concentration of $1.1 \times 10^{16} \text{ m}^{-3}$. If the mobilities of electrons and holes are 0.17 and $0.035 \text{ m}^2 \text{ V}^{-1} \text{ s}^{-1}$ respectively at room temperature, compute the resistivity of silicon.

$$\sigma_i = n_i e (\mu_e + \mu_h)$$

$$= 1.1 \times 10^{16} \times 1.6 \times 10^{-19} (0.17 + 0.035)$$

$$= 1.76 \times 10^{-3} (0.205)$$

$$= 0.3608 \times 10^{-3}$$

$$= 3.608 \times 10^{-4} \text{ Ohm}^{-1} \text{ m}^{-1}$$

$$\text{Resistivity} = \frac{1}{\sigma} = \rho = \frac{1}{3.608 \times 10^{-4}} = 2.77 \times 10^4 \text{ Ohm}$$

6. The compound gallium arsenide has an intrinsic conductivity of $10^{-6} \text{ ohm}^{-1}\text{m}^{-1}$ at 20°C . How many electrons have jumped the forbidden energy gap?

[Given : $\mu_e = 0.88 \text{ m}^2 \text{ V}^{-1}\text{s}^{-1}$ and $\mu_h = 0.04 \text{ m}^2 \text{ V}^{-1}\text{s}^{-1}$]

$$n_i = \frac{\sigma}{e(\mu_e + \mu_h)}$$

$$= \frac{1 \times 10^{-6}}{1.6 \times 10^{-19}} \cdot (0.88 + 0.04)$$

$$= 0.825 \times 10^{12} (0.92)$$

$$= \frac{1 \times 10^{-6}}{1.6 \times 10^{-19} (0.92)} = \frac{6.79 \times 10^{12} \text{ m}^{-3}}{1}$$

7. The resistivity of Ge at 20°C is 0.5 ohm m . What will be its resistivity at 40°C if band gap of Ge is 0.7 eV ?

$$\frac{\Delta(\ln \rho)}{\Delta(1/T)} = \frac{Eg}{2K}$$

$$Eg = \frac{\Delta(\ln \rho) \times 2K}{\Delta(1/T)}$$

$$\Delta(\ln \rho) = \frac{Eg}{2K} \times \Delta(1/T)$$

$$= \frac{0.7 \times 1.6 \times 10^{-19} \times (1/313 - 1/1293)}{2 \times 1.38 \times 10^{-23}}$$

$$\neq 1/12 (3.19 - 3.41) \times 10^{-3}$$

$$\begin{aligned}\ln f_{40} &= \ln f_{20} = -0.885 \\ &= -0.693 - 0.885 \\ &= -1.578\end{aligned}$$

$$f_{40} = 0.206 \text{ ohm m}$$

8. An intrinsic Semiconductor has an energy gap of 0.7 eV. Calculate probability of occupation of the lowest level in conduction band at 0°, 50°, 100°

- Lowest level in Conduction Band

$$(E - E_f) = 0.35 \text{ eV}$$

probability

$$F(ut) = \frac{1}{1 + \exp((E - E_f)/kT)}$$

1) The critical temperature and critical magnetic field for superconducting lead are 7.2 K and 800 gauss respectively. What will be the temperature upto which lead will be in superconducting state in a magnetic field of 400 gauss

$$\Rightarrow T_c = 7.2$$

$$H_c(0) = 800 \text{ K}$$

$$H_c(T) = 400 \text{ K}$$

$$H_c(T) = H_c(0) \left[1 - \left(\frac{T}{T_c} \right)^2 \right]$$

$$400 = 800 \left[1 - \frac{T^2}{51.84} \right]$$

$$\frac{1-1}{2} = -\frac{T^2}{51.84}$$

$$0.8 =$$

$$-0.5$$

$$25.9 = T^2$$

$$T = 5.09 \text{ K}$$

2) Superconducting dme tin has a critical magnetic field of 217 gauss at 2 K. If the critical temperature for superconducting transition for tin is 3.7 K, find the critical magnetic field at 3 K.

$$H_c(T) = H_c(0) \left[1 - \left(\frac{T}{T_c} \right)^2 \right]$$

$$H_c(T_1) = H_c(0) \left[1 - \left(\frac{T_1}{T_c} \right)^2 \right] \quad \text{--- (1)}$$

$$H_c(T_2) = H_c(0) \left[1 - \left(\frac{T_2}{T_c} \right)^2 \right] \quad \text{--- (2)}$$

$$\frac{H_c(T_1)}{H_c(T_2)} = \frac{T_c^2 - T_1^2}{T_c^2 - T_2^2}$$

$$= \frac{(3.7)^2 - (2)^2}{(3.7)^2 - (3)^2}$$

$$= \frac{13.69 - 4}{13.69 - 9} = \frac{9.69}{4.69}$$

$$\frac{217}{H_c(T_2)} = \underline{\underline{2.066}}$$

$$H_c(T_2) = 105.02 \text{ Gauss}$$

- 3) The transition temperature for Pb is 7.2 K. However at 5 K it loses the superconducting property if subjected a magnetic field of $3.3 \times 10^4 \text{ A/m}$. Find the maximum value of H which will allow the

metal to retain its superconductivity at 0K

$$\rightarrow T_c = 7.2 \text{ K} \quad H_c(T) = 3.3 \times 10^4$$

$$T_g = 5 \text{ K}$$

$$H_c(T) = H_c(0) \left[1 - \left(\frac{T}{T_c} \right)^2 \right]$$

$$3.3 \times 10^4 = H_c(0) \left[1 - \left(\frac{5}{7.2} \right)^2 \right]$$

$$= H_c(0) \left[1 - \frac{25}{51.84} \right]$$

$$3.3 \times 10^4 = H_c(0) [1 - 0.48]$$

$$3.3 \times 10^4 = H_c(0) [0.52]$$

$$H_c(0) = 6.34 \times 10^4 \text{ A/m}$$

- 4) The critical field of N6 is $1 \times 10^5 \text{ A/m}$ at 8K, and $2 \times 10^5 \text{ A/m}$ at 0K. Calculate the transition temperature of the element.

$$\rightarrow H_c(T) = 1 \times 10^5 \text{ A/m}$$

$$H_c(0) = 2 \times 10^5 \text{ A/m}$$

$$T = 8 \text{ K}$$

$$T_c = ?$$

$$H_c(T) = H_c(0) \left[1 - \left(\frac{T}{T_c} \right)^2 \right]$$

$$1 \times 10^5 = 2 \times 10^5 \left[1 - \left(\frac{8}{T_c} \right)^2 \right]$$

$$\frac{1 \times 10^5}{2 \times 10^5} = 1 - \frac{64}{(T_c)^2}$$

$$0.5 = 1 - \frac{64}{T_c^2}$$

$$(T_c)^2 = \frac{1 - 64}{0.5}$$

$$T_c = \frac{11.31}{-}$$

1. The Hall co-efficient of a specimen of a doped silicon is found to be $3.66 \times 10^{-4} \text{ m}^3/\text{C}$. The resistivity of the specimen is $8.93 \times 10^{-3} \Omega \text{ m}$. Find the mobility and density of the charge carriers.

Given : $R_H = 3.66 \times 10^{-4} \text{ m}^3/\text{C}$

$$\rho = 8.93 \times 10^{-3} \Omega \text{ m}$$

n = density of charge carriers.

$$n = \frac{1}{R_H e} = \frac{1}{3.66 \times 10^{-4} \times 1.6 \times 10^{-19}}$$

$$= 0.1707 \times 10^{23}$$

$$= 1.707 \times 10^{22}$$

$$\mu_e = \frac{\sigma}{ne} = R_H \frac{1}{\rho} = \frac{3.66 \times 10^{-4}}{8.93 \times 10^{-3}}$$

$$\underline{\mu_e = 0.041 \text{ m}^2/\text{Vs}}$$

2. A semiconductor sample of thickness $1.2 \times 10^{-4} \text{ m}$ is placed in a magnetic field of 0.2 T acting perpendicular to its thickness. Find the hall voltage generated when a current of 100 mA passes through it. Assume the charge carrier concentration is 10^{23} m^{-3}

Given: $t = 1.2 \times 10^{-4} \text{ m}$ $I = 100 \text{ mA}$
 $B = 0.2 \text{ T}$ $e = 1.6 \times 10^{-19}$

$$V_H = ?$$

$$n = 10^{23} \text{ m}^{-3}$$

$$V_H = \frac{3\pi B I}{8 \text{ net}} = \frac{3 \times 3.14}{8} \cdot \frac{0.2 \times 100 \times 10^{-3}}{10^{23} \times 1.6 \times 10^{-19} \times 1.2 \times 10^{-4}}$$

$$= \frac{9.42 \times 20 \times 10^{-3}}{8 \times 1.92 \times 10^{23} \times 10^{-23}} = \frac{188.4 \times 10^{-3}}{15.36}$$

$$= \underline{\underline{12.26 \times 10^{-3}}}$$

3. The Hall Coefficient of a semiconductor is $3.22 \times 10^{-4} \text{ m}^3/\text{C}$. Its resistivity is $9 \times 10^{-3} \Omega \text{ m}$. Calculate mobility and carrier concentration

$$n = \frac{1}{R_H e} = \frac{1}{3.22 \times 10^{-4} \times 1.6 \times 10^{-19}}$$

$$= \frac{1}{5.152 \times 10^{-23}} = \frac{0.1940 \times 10^{23}}{1.94 \times 10^{22}}$$

$$\mu_e = R_H \cdot \frac{1}{\rho} = 1.94 \times 10^{22} \cdot \frac{1}{9 \times 10^{-3}} \\ = 0.02156 \times 10^{-3} m^2/Vs$$

4. A Si plate of thickness 1 mm, breadth 1 cm, and length 10 cm is placed in a magnetic field of 0.5 T, acting perpendicular to axis. If 1 A current flows along its length, calculate the Hall Voltage developed, if Hall co-efficient is $3.66 \times 10^{-4} m^3 C^{-1}$

$$V_H = R_H \cdot \frac{BI}{t} = 3.66 \times 10^{-4} \times 0.5 \times 1 \\ = 3.66 \times 10^{-4} \times 0.5 \times 10^3 \\ = 1.83 \times 10^{-1}$$

$$V_H = 0.183 V$$

5. Calculate the Hall Voltage across a semiconductor with following data

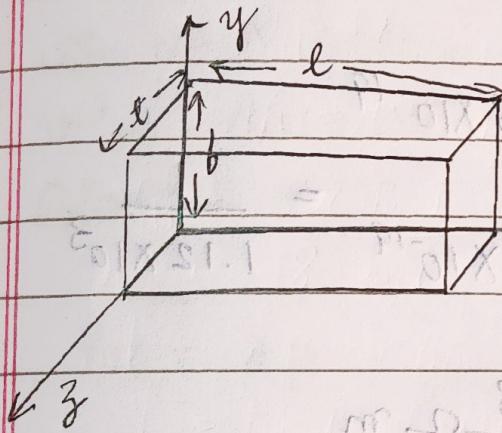
- Width = 0.11 m
- Thickness = 0.01 m
- Magnetic field = 0.6 T

Current, I = 10 mA Hall coefficient $R_H = 3.84 \times 10^{-4} m^3$

$$V_H = R_H \cdot \frac{BI}{t} = 3.84 \times 10^{-4} \times \frac{0.6 \times 10 \times 10^{-3}}{0.01}$$

$$= 2304 \times 10^{-7} = 2.304 \times 10^{-4} V$$

6. A rectangular plane sheet of a semiconductor material of dimensions 2 cm along γ direction, and 1 mm along α direction. Hall probes are attached on its surfaces parallel to $\alpha\gamma$ plane and a magnetic field of flux density of 1 Weber/m² is applied along γ direction. A current of 3 mA is flowing in it in the α -direction. Calculate the Hall voltage measured by the probes if the Hall coefficient of the material is 3.66×10^{-4} m²/C. Also calculate the charge carrier.



$$a) V_H = R_H \cdot \frac{BI}{t}$$

$$V_H = \frac{3.66 \times 10^{-4} \times 1 \times 3 \times 10^{-3}}{1 \times 10^{-3}} = \frac{10.98 \times 10^{-7}}{1 \times 10^{-3}}$$

$$V_H = \frac{10.98 \times 10^{-4}}{1} V$$

$$\approx 1.1 \text{ mV}$$

$$b) \Rightarrow R_H = \frac{1}{ne}$$

$$n = \frac{1}{R_H e} = \frac{1}{3.66 \times 10^{-4} \times 1.6 \times 10^{-19}} = \frac{1.71 \times 10^{23}}{\text{cm}^3}$$

$$V = 1.1 \text{ mV}$$

7. A sample of Si is doped with 10^{22} Phosphorous atom/m³. What is its resistivity? What shall voltage would you expect in the sample of $100\mu\text{m}$ thick when the current of 1mA is passed perpendicular to a magnetic field of 0.1T

Given: $\mu_e = 0.7 \text{ m}^2/\text{Vs}$

$$\rho = ? \quad \mu_e = \frac{e}{ne} = \frac{1}{Pne} \quad P = \frac{1}{\rho ne}$$

$$0.7 = \frac{1}{1.6 \times 10^{22} \times 1.6 \times 10^{-19}}$$

$$\rho = \frac{1}{0.7 \times 10^{22} \times 1.6 \times 10^{-19}} = \frac{1}{1.12 \times 10^3}$$

$$\rho = 0.892 \times 10^{-3} \Omega \text{ m}$$

$$V_H = R_H \cdot \frac{BI}{t} = \frac{1}{ne} \cdot \frac{BI}{t}$$

$$= \frac{1}{10^{22} \times 1.6 \times 10^{-19}} \times \frac{0.1 \times 1 \times 10^{-3}}{160 \times 10^{-6}}$$

$$= \frac{0.1 \times 10^{-3}}{160 \times 10^{-3}} = 6.25 \times 10^{-4}$$

$$= 0.625 \times 10^{-3} \text{ V}$$

Q2

$$V_H = \frac{3\pi}{8} \frac{1}{ne}$$

$$= \frac{3 \times 3.14 \times 1}{8 \times 10^{22} \times 1.6 \times 10^{-19}}$$

$$= \frac{9.42}{12.8 \times 10^3} = \underline{\underline{0.73 \times 10^{-3} V}}$$

8. A current of 3 mA is flowing in a semiconducting material of length 2 cm and width 1 mm . Calculate the Hall voltage, if the Hall coefficient is $3.66 \times 10^{-4}\text{ m}^3/\text{C}$. Also calculate charge concentration

Given : $B = 1\text{ T}$

$$V_H = RH \cdot \frac{BI}{t} = \frac{3.66 \times 10^{-4} \times 1 \times 3 \times 10^{-3}}{1 \times 10^{-3}}$$

$$= \frac{10.98 \times 10^{-7}}{10^{-3}}$$

$$= \underline{\underline{10.98 \times 10^{-4}}}$$

$$V_H = \underline{\underline{1.098 \times 10^{-3} V}}$$

$$n = \frac{1}{R_{He}} = \frac{1}{3.66 \times 10^{-4} \times 1.6 \times 10^{-19}} = \underline{\underline{5.856}}$$

$$\underline{\underline{0.1707 \times 10^{23}}}$$