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- 4 Nyquist Plot
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Abstract—This manual is an introduction to control systems based on GATE problems.Links to sample Python codes are available in the text.

1 STABILITY

2 ROUTH HURWITZ CRITERION

- 3 Compensators
- 4 NYQUIST PLOT
- 5 STATE SPACE MODEL

6 oscillator

6.1. Fig. shows a Hartley oscillator.

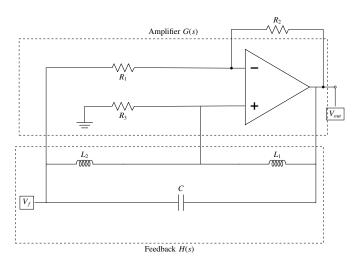


Fig. 6.1: Hartley oscillator

6.2. Draw the equivalent block diagram of an oscillator.

Solution: Fig. shows the block diagram of the an Oscillator in Fig. 6.2.

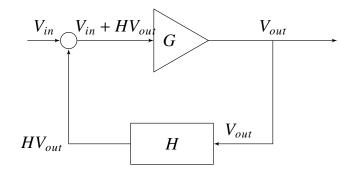


Fig. 6.2: block diagram for oscillator

6.3. Show that the gain of the oscillator is

$$Gain = \frac{V_{out}}{V_{in}} = \frac{G}{1 - GH}$$
 (6.3.1)

Solution: From figure 6.2 Oscillators gain can be given as follows:

$$G(V_{in} + HV_{out}) = V_{out} \tag{6.3.2}$$

$$G(V_{in} = (1 - GH)V_{out}$$
 (6.3.3)

$$\frac{V_{out}}{V_{in}} = \frac{G}{1 - GH} \tag{6.3.4}$$

resulting in (6.3.1).

6.4. State the condition for sustained oscillations. Justify.

Solution: Condition for sustained oscillation is given by

$$GH = 1$$
 (6.4.1)

Along with, total phase gain o the circuit should be 0 or 2π

Justification: as, when GH = 1, gain becomes infinity, and theoretically we can get output, without actually providing input

Total phase gain should be so, as we want our signal to be in phase after every loop traversal.

6.5. Find *G* and *H*.

Solution: Consider the below circuit fig 6.5,its basic form of a LC oscillator.

The above figure 6.5 can also be drawn as fig. 6.5, when feedback is considered as load:

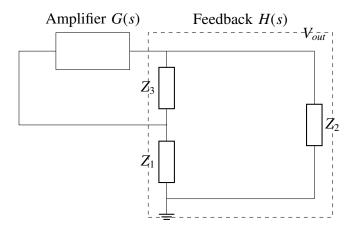


Fig. 6.5: Basic Circuit representation of LC circuit

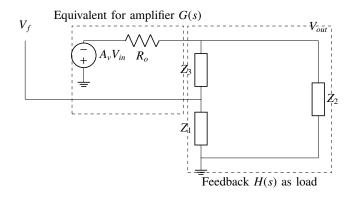


Fig. 6.5: Amplifier written in equivalent circuit form

We know that feedback gain is H, i.e, $\frac{V_0}{V_f} = H$

Fig. 6.5 is equivalent amplifier circuit representation of figure above. 6.5

Applying voltage divider rule we get From figure 6.5

$$H = \frac{Z_1}{Z_1 + Z_3} \tag{6.5.1}$$

From fig. (6.5)

$$G = \frac{V_o}{V_{in}} = \frac{A_v Z_L}{R_o + Z_L}$$
 (6.5.2)

(6.5.3)

where.

 R_o is the equivalent resistance in amplifier A_v is the amplification factor of the opamp v_{in} is the internal voltage in amplifier Z_L is equivalent load across output

$$Z_L = \frac{(Z_1 + Z_3)Z_2}{Z_1 + Z_2 + Z_3}$$
 (6.5.4)

6.6. Find the frequency of oscillation using the condition that AB = 1.

Solution: For any LC oscillator, Now,we know that GH = 1 for sustained oscillations, putting the the above terms in the equation on solving,

Hartley oscillator:

The Hartley oscillator is one of the classical LC feedback circuits,i.e feedback is made of LC components.Below here

$$Z_1 = SL_1(inductor) (6.6.1)$$

$$Z_2 = SL_2(inductor) (6.6.2)$$

$$Z_3 = \frac{1}{SC}(capacitor) (6.6.3)$$

 \therefore H(s) can be given by,

$$H(s) = \frac{SL_1}{SL_2 + \frac{1}{SC}}$$
 (6.6.4)

$$=\frac{S^2L_1C}{S^2L_2C+1}\tag{6.6.5}$$

$$G(s) = \frac{A_{\nu}(SL_1 + \frac{1}{SC})Sl_2}{R_o(SL_1 + SL_2 + \frac{1}{SC} + S^2L_1L_2\frac{L_2}{C})}$$
(6.6.6)

$$= \frac{A_{\nu}(S^{2}L_{1}C+1)SL_{2}}{R_{o}(S^{2}(L_{1}+L_{2})C+1)+S^{3}L_{1}L_{2}C+SL_{2}}$$
(6.6.7)

putting that in and equating GH = 1 we get,

$$1 = \frac{S^2 L_1 L_2 A_{\nu}}{(S L_1 + S L_2 + \frac{1}{SC}) R_o + S L_2 (S L_1 + \frac{1}{SC})}$$
(6.6.8)

$$S^{2}L_{1}L_{2}A_{v} = (SL_{1} + SL_{2} + \frac{1}{SC})R_{o} + SL_{2}(SL_{1} + \frac{1}{SC})$$
(6.6.9)

As we need, to find frequency, put S = iw

$$\omega^{2} L_{1} L_{2} A_{\nu} = j(\omega L_{1} + \omega L_{2} - \frac{1}{\omega C}) R_{o} - \omega L_{2} (\omega L_{1} + \frac{1}{\omega C})$$
(6.6.10)

To satisfy the above equation, equating imaginary term to Zero.

$$\omega L_1 + \omega L_2 = \frac{1}{\omega C} \tag{6.6.11}$$

$$\omega = \frac{1}{\sqrt{(L_1 + L_2)(C)}} \tag{6.6.12}$$

$$f = \frac{1}{2\pi\sqrt{(L_1 + L_2)(C)}} \tag{6.6.13}$$

$$H = \frac{Z_1}{Z_1 + Z_3} = \frac{Z_1}{Z_2}$$

$$= \frac{L_1}{L_2}$$
(6.6.14)

$$G = \frac{L_2}{L_1} \tag{6.6.16}$$

6.7. For Hartley oscillator frequency generated can be given as

$$f = \frac{1}{2\pi\sqrt{(L_1 + L_2)C}} \tag{6.7.1}$$

We know that for an opamp gain is given by:

$$G = \frac{R_2}{R_1} \tag{6.7.2}$$

Here,

$$G(S) = \frac{R_2}{R_1} = \frac{L_2}{L_1}$$
 (6.7.3)

referring to 6.6.16 And,

$$H(s) = \frac{V_o}{V_f} = \frac{L_1}{L_2}$$
 (6.7.4)

referring to 6.6.15

6.8. Simulation:

Taking the following values, and applying in 6.7.1

Component	Value
R_1	10ΚΩ
R_2	100ΚΩ
R_3	~
L_1	$1\mu H$
L_2	$1\mu H$
С	120 pF

We get f = 103 MHz

Feedback factor for Hartley given by:

$$B = \frac{L_1}{L_2} = 1 \tag{6.8.1}$$

W.K.T, AB = 1

 \therefore Minimum amplification Gain,A = 1