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2 Routh Hurwitz Criterion 1

Abstract—This manual is an introduction to control systems based on GATE problems.Links to sample Python codes are available in the text.

## 1 STABILITY

- 2 ROUTH HURWITZ CRITERION
  - 3 Compensators
  - 4 Nyquist Plot
  - 5 STATE SPACE MODEL
- 5.0.1. The transfer function of the system Y(s)/U(s) whose state-space equations are given below:

$$\begin{pmatrix} x_1'(t) \\ x_2'(t) \end{pmatrix} = \begin{pmatrix} 1 & 2 \\ 2 & 0 \end{pmatrix} \begin{pmatrix} x_1(t) \\ x_2(t) \end{pmatrix} + \begin{pmatrix} 1 \\ 2 \end{pmatrix} u(t)$$
 (5.0.1.1)

$$y(t) = \begin{pmatrix} 1 & 0 \end{pmatrix} \begin{pmatrix} x_1(t) \\ x_2(t) \end{pmatrix}$$
 (5.0.1.2)

(A)  $\frac{s+2}{s^2-2s-2}$  (B)  $\frac{s-2}{s^2+s-4}$  (C)  $\frac{s-4}{s^2+s-4}$ (D)  $\frac{s+4}{s^2-s-4}$  **Solution:** By comparing the above equations to to (5.1.1) and (5.1.2) we get

$$D = 0 (5.0.1.3)$$

$$C = \begin{pmatrix} 1 & 0 \end{pmatrix} \tag{5.0.1.4}$$

$$B = \begin{pmatrix} 1\\2 \end{pmatrix} \tag{5.0.1.5}$$

$$A = \begin{pmatrix} 1 & 2 \\ 2 & 0 \end{pmatrix} \tag{5.0.1.6}$$

From equation (5.3.1) the transfer function

$$H(s) = \frac{Y(s)}{U(s)} = C(sI - A)^{-1}B + DI \quad (5.0.1.7)$$

$$H(s) = \begin{pmatrix} 1 & 0 \end{pmatrix} \begin{pmatrix} s - 1 & -2 \\ -2 & s \end{pmatrix}^{-1} \begin{pmatrix} 1 \\ 2 \end{pmatrix}$$
 (5.0.1.8)

$$H(s) = \begin{pmatrix} 1 & 0 \end{pmatrix} \frac{\begin{pmatrix} s & 2 \\ 2 & s - 1 \end{pmatrix}}{s^2 - s - 4} \begin{pmatrix} 1 \\ 2 \end{pmatrix}$$
 (5.0.1.9)

$$H(s) = \begin{pmatrix} 1 & 0 \end{pmatrix} \frac{\begin{pmatrix} s+4\\ 2+2s-2 \end{pmatrix}}{s^2-s-4}$$
 (5.0.1.10)

$$H(s) = \frac{s+4}{s^2 - s - 4} \tag{5.0.1.11}$$