

## CONTENTS

1	Stability	1
2	Routh Hurwitz Criterion	1
3	Compensators	1
4	Nyquist Plot	1
5	State space model	1

*Abstract*—This manual is an introduction to control systems based on GATE problems. Links to sample Python codes are available in the text.

## 1 STABILITY

## 2 ROUTH HURWITZ CRITERION

## 3 COMPENSATORS

## 4 NYQUIST PLOT

## 5 STATE SPACE MODEL

5.0.1. The transfer function of the system  $Y(s)/U(s)$  whose state-space equations are given below:

$$\dot{\mathbf{x}} = \begin{pmatrix} 1 & 2 \\ 2 & 0 \end{pmatrix} \mathbf{x} + \begin{pmatrix} 1 \\ 2 \end{pmatrix} u(t) \quad (5.0.1.1)$$

$$\mathbf{y} = \begin{pmatrix} 1 & 0 \end{pmatrix} \mathbf{x} \quad (5.0.1.2)$$

(A)  $\frac{s+2}{s^2-2s-2}$  (B)  $\frac{s-2}{s^2+s-4}$  (C)  $\frac{s-4}{s^2+s-4}$  (D)  $\frac{s+4}{s^2-s-4}$

**Solution:** By comparing the above equations to to (5.1.1) and (5.1.2) we get

$$\mathbf{D} = 0 \quad (5.0.1.3)$$

$$\mathbf{C} = \begin{pmatrix} 1 & 0 \end{pmatrix} \quad (5.0.1.4)$$

$$\mathbf{B} = \begin{pmatrix} 1 \\ 2 \end{pmatrix} \quad (5.0.1.5)$$

$$\mathbf{A} = \begin{pmatrix} 1 & 2 \\ 2 & 0 \end{pmatrix} \quad (5.0.1.6)$$

From equation (5.3.1) the transfer function

$$H(s) = \frac{Y(s)}{U(s)} = \mathbf{C}(s\mathbf{I} - \mathbf{A})^{-1}\mathbf{B} + \mathbf{D} \quad (5.0.1.7)$$

$$H(s) = \begin{pmatrix} 1 & 0 \end{pmatrix} \begin{pmatrix} s-1 & -2 \\ -2 & s \end{pmatrix}^{-1} \begin{pmatrix} 1 \\ 2 \end{pmatrix} \quad (5.0.1.8)$$

$$H(s) = \begin{pmatrix} 1 & 0 \end{pmatrix} \frac{1}{s^2 - s - 4} \begin{pmatrix} s & 2 \\ 2 & s-1 \end{pmatrix} \begin{pmatrix} 1 \\ 2 \end{pmatrix} \quad (5.0.1.9)$$

$$H(s) = \frac{1}{s^2 - s - 4} \begin{pmatrix} 1 & 0 \end{pmatrix} \begin{pmatrix} s+4 \\ 2+2s-2 \end{pmatrix} \quad (5.0.1.10)$$

$$H(s) = \frac{s+4}{s^2 - s - 4} \quad (5.0.1.11)$$

The following code computes the transfer function performing all calculations.

codes / ee18btech11040 . py