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Division - 11

MSC Assignment - 1

Q.1. A person is standing at the top of a hill. He throws a ball upwards with an initial velocity of 10 m/s. The ball reaches a maximum height of 5 m and then falls back to the ground. Calculate the time taken by the ball to reach the ground.

Solution:

Given: Initial velocity $u = 10 \text{ m/s}$, Maximum height $h = 5 \text{ m}$.

At the maximum height, the final velocity $v = 0 \text{ m/s}$.

Using the equation of motion:

$$v^2 = u^2 - 2gh$$

$$0 = 10^2 - 2 \times 10 \times h$$

$$0 = 100 - 20h$$

$$20h = 100$$

$$h = 5 \text{ m}$$

Now, to find the time taken to reach the ground, we use the equation:

$$h = ut - \frac{1}{2}gt^2$$

$$5 = 10t - \frac{1}{2} \times 10 \times t^2$$

$$5 = 10t - 5t^2$$

$$5t^2 - 10t + 5 = 0$$

$$t^2 - 2t + 1 = 0$$

$$(t - 1)^2 = 0$$

$$t = 1 \text{ s}$$

Therefore, the time taken by the ball to reach the ground is 1 second.

Q.2. A person is standing at the top of a hill. He throws a ball upwards with an initial velocity of 10 m/s. The ball reaches a maximum height of 5 m and then falls back to the ground. Calculate the time taken by the ball to reach the ground.

Solution:

Given: Initial velocity $u = 10 \text{ m/s}$, Maximum height $h = 5 \text{ m}$.

At the maximum height, the final velocity $v = 0 \text{ m/s}$.

Using the equation of motion:

$$v^2 = u^2 - 2gh$$

$$0 = 10^2 - 2 \times 10 \times h$$

$$0 = 100 - 20h$$

$$20h = 100$$

$$h = 5 \text{ m}$$

Now, to find the time taken to reach the ground, we use the equation:

$$h = ut - \frac{1}{2}gt^2$$

$$5 = 10t - \frac{1}{2} \times 10 \times t^2$$

$$5 = 10t - 5t^2$$

$$5t^2 - 10t + 5 = 0$$

$$t^2 - 2t + 1 = 0$$

$$(t - 1)^2 = 0$$

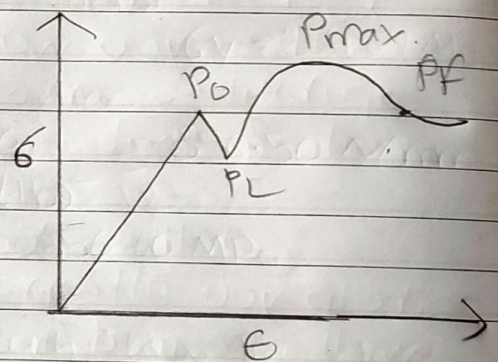
$$t = 1 \text{ s}$$

Therefore, the time taken by the ball to reach the ground is 1 second.

Q1) Tensile test conducted on steel specimen of diameter 12.5mm & gauge length 50mm. loads at upper & lower yield points were 4600 & 4500 respectively. Max & fracture loads were 7500 kg & 5000 kg. Gauge length after fracture was 62.5mm, diameter of fracture place was 8mm.

- Find-
- ① lower yield stress
 - ② upper yield stress
 - ③ ultimate tensile stress
 - ④ fracture stress
 - ⑤ True fracture stress
 - ⑥ percent elongation
 - ⑦ Percent reduction in cross section area.

Ans → $P_L = 4500 \text{ kg}$
 $P_U = 4600 \text{ kg}$
 $P_{\text{max}} = 7500 \text{ kg}$
 $P_F = 5000 \text{ kg}$
 $d_o = 12.5 \text{ mm}$



Given: $A_o = \frac{\pi}{4} d_o^2$

$A_f = \frac{\pi}{4} d_f^2$

① ∴ Lower yield strength (σ_{yL}) = $\frac{P_L}{A_o} = \frac{4500}{\frac{\pi (12.5)^2}{4}}$

$$= 36.66 \text{ kg/mm}^2$$

$$= 366.69 \text{ N/mm}^2$$

$$= \underline{366.69 \text{ MPa}}$$

$$\textcircled{11} \text{ upper yield stress } (\sigma_{yu}) = \frac{P_u}{A_0} = \frac{4600}{\pi/4 (12.5)^2} = 37.48 \text{ kg/mm}^2 = 374.8 \text{ N/mm}^2 = 374.8 \text{ N/10}^6 \text{ m}^2 = 374.8 \times 10^6 \text{ N/m}^2$$

$$\boxed{\sigma_{yu} = 374.8 \text{ MPa}}$$

$$\textcircled{3} \text{ Ultimate tensile stress } (\sigma_{UTS}) = \frac{P_{max}}{A_0} = \frac{7500}{\pi/4 (12.5)^2} = 61.11 \text{ kg/mm}^2$$

$$\underline{\sigma_{UTS} = 611.1 \text{ MPa}}$$

$$\textcircled{4} \text{ Fracture stress } (\sigma_{fT}) = \frac{P_{max}}{A_0} = \frac{75000}{\pi/4 (12.5)^2} = 61.4074 \text{ kg/mm}^2$$

$$\underline{\sigma_{fT} = 617.4 \text{ MPa}}$$

$$\textcircled{5} \text{ True fracture stress } (\sigma_{true}) = \frac{P_t}{A_f} = \frac{6000}{\pi/4 (8)^2} = 99.47 \text{ kg/mm}^2$$

$$\underline{\sigma_{true} = 994.7 \text{ MPa}}$$

$$\textcircled{6} \text{ Percent elongation} = \frac{(62.5 - 50)}{50} \times 100 = 25\%$$

$$\textcircled{7} \text{ Percent reduction in cross section area} = \frac{(A_0 - A_f)}{A_0} \times 100 = 59.04\%$$

Q2) A test rod of 15mm diameter failed at 50kN during tensile test but reached max load of 63kN. The specimen had 75mm gauge length and yielding at 45kN and was elongated to 80mm. Calculate a. Yield stress. b. Ultimate tensile stress c. % Elongation.

Ans → Given - $P_f = 50\text{ kN}$

$$P_{\max} = 63\text{ kN}$$

$$L_0 = 75\text{ mm}; L_f = 80\text{ mm}$$

$$P_y = 45\text{ kN}, d_0 = 15\text{ mm}$$

$$a) \sigma_{\text{yield}} = \frac{P_y}{A_0} = \frac{P_y}{\frac{\pi}{4} d_0^2} = \frac{45 \times 10^3}{\frac{\pi}{4} (15)^2} = 254.64 \text{ N/mm}^2$$

$$\sigma_y = 254.64 \text{ MPa}$$

$$b) \sigma_{\text{UTS}} = \frac{P_{\max}}{A_0} = \frac{63 \times 10^3}{\frac{\pi}{4} (15)^2} = 356.50 \text{ N/mm}^2$$

$$\sigma_{\text{UTS}} = 356.60 \text{ MPa}$$

$$c) \text{Percentage elongation} = \frac{L_f - L_0}{L_0} \times 100$$

$$= \frac{80 - 75}{75} \times 100$$

$$= 6.67\%$$

- (Q3) A 20 cm long rod w/c diameter of 0.3 cm is loaded with 4000 N. If diameter reduces to 0.27 cm. Find - ① Engineering stress ② True stress

Ans \rightarrow $L_0 = 20 \text{ cm}$
 $d_0 = 0.3 \text{ cm} = 3 \text{ mm}$, $d_f = 0.27 \text{ cm} = 2.7 \text{ mm}$
 $L = 4000 \text{ N}$

① Engineering stress = $\frac{\text{load}}{\text{original area}} = \frac{4000}{\pi/4 (d_0)^2}$
 $= 565.884 \text{ N/mm}^2$
 $\sigma_{\text{eng}} = 565.88 \text{ MPa}$

② True stress = $\frac{\text{load}}{\text{new area}} = \frac{4000}{\pi/4 (d_f)^2}$
 $= 698.622 \text{ N/mm}^2$
 $= 698.622 \times 10^6 \text{ N/m}^2$
 $\sigma_{\text{true}} = 698.622 \text{ MPa}$

- (Q4) The tensile test specimen of mild steel of 8 mm diameter & 40 mm gauge length was tested with following result.

$L_{\text{max}} = 3212 \text{ kg}$, $L_y = 1756 \text{ kg}$, $\Delta L = 50 \text{ mm}$, $d_f = 5.4 \text{ mm}$.

- Find - ① σ_{TS} in kg/mm^2
 ② ϵ in kg/mm^2
 ③ % elongation.
 ④ % reduction in area.

Ans) $d_o = 8 \text{ mm}$, $d_f = 5.4 \text{ mm}$

$L_o = 40 \text{ mm}$, $\Delta l = 50 \text{ mm}$

$L_{\max} = 3212 \text{ kg}$, $L_y = 1750 \text{ kg}$

$$\textcircled{1} \text{ UTS} = \frac{L_{\max}}{A_o} = \frac{3212}{\pi/4 (d_o)^2}$$

$$\text{UTS} = \underline{63.90 \text{ kg/mm}^2}$$

$$\textcircled{2} \text{ Y.S} = \frac{L_y}{A_o} = \frac{1750}{\pi/4 (d_o)^2} = 34.815$$

$$\text{YS} = \underline{34.815 \text{ kg/mm}^2}$$

$$\textcircled{3} \% \text{ elongation} = \frac{\Delta l}{l_o} \times 100$$

$$= \frac{50}{40} \times 100$$

$$\underline{\% \text{ elongation} = 125\%}$$

$$\textcircled{4} \% \text{ reduction in area} = \left(\frac{A_o - A_f}{A_o} \right) \times 100$$

$$= \frac{\pi/4 (d_o^2 - d_f^2)}{\pi/4 d_o^2} \times 100$$

$$\underline{\% \text{ reduction in area} = 54.43\%}$$

Q35) Following data was obtained during tensile test conducted on mild steel specimen 42mm in diameter & 210mm long.

ΔL with 45 kN = 0.404 mm

$L_y = 163 \text{ kN}$, $L_{\max} = 245 \text{ kN}$, $L_f = 250 \text{ mm}$

Find - ① Young's modulus

② Yield point

③ Ultimate stress

④ Percentage elongation.

Ans $\rightarrow L_0 = 210 \text{ mm}$, $L_f = 250 \text{ mm}$, ΔL at 45 kN = 0.404 mm
 $L_y = 163 \text{ kN}$, $L_{\max} = 245 \text{ kN}$, $d_0 = 42 \text{ mm}$.

① Young's modulus

$$\text{stress } \sigma = \frac{P}{A} = \frac{40}{\pi d_0^2} = 0.0289 \text{ kN/mm}^2$$

$$= 0.0289 \times 10^6 \text{ kN/m}^2$$

$$= 289 \times 10^4 \text{ kN/m}^2$$

$$\text{strain} = \frac{\Delta L}{L_0} = \frac{0.404}{210} = 1.92 \times 10^{-3}$$

$$\text{Young's modulus } E = \frac{\text{stress}}{\text{strain}} = \frac{2.89 \times 10^4}{1.92 \times 10^{-3}}$$

$$\text{Young's modulus} = 1.505 \times 10^7 \text{ kN/m}^2$$

$$\textcircled{2} \sigma_{yp} = \frac{L_y}{A_0} = \frac{163}{\pi d_0^2}$$

$$= 0.11765 \text{ kN/mm}^2$$

$$= 1.1765 \times 10^5 \text{ kN/m}^2$$

$$= 1.1765 \times 10^6 \text{ N/m}^2$$

$$\sigma_{yp} = 1.1765 \times 10^2 \text{ MPa}$$

$$= 117.65 \text{ MPa}$$

$$\textcircled{3} \sigma_{UTS} = \frac{L_{max}}{A_0} = \frac{245}{\pi d_0^2}$$

$$= 0.17683 \text{ kN/mm}^2$$

$$= 1.7683 \times 10^5 \text{ kN/m}^2$$

$$= 1.7683 \times 10^8 \text{ N/m}^2$$

$$= 176.83 \times 10^6 \text{ N/m}^2$$

$$\sigma_{UTS} = 176.83 \text{ MPa}$$

$$\textcircled{4} \% \text{ elongation} = \frac{L_f - L_0}{L_0} \times 100$$

$$= \frac{40}{210} \times 100$$

$$\approx \% \text{ elongation} = 19.04\%$$