

Solved Examples

Solid State Physics

- Ex. 1**
- (i) Calculate the energy gap of Si, given that it is transparent to radiation of wavelength greater than 11000 \AA
 - (ii) Calculate the energy band gap in germanium. Given that it is transparent radiation of wavelength greater than 17760 \AA

Soln :

The energy gap E_g is the minimum energy required to shift the electron from V.B. to C.

- (i) Energy of the incident photon should at least be

$$\begin{aligned} \text{For silicon } h\nu &= E_g \\ E_g &= h\nu = \\ E_g &= \text{J.} \\ E_g &= \\ \mathbf{E_g = 1.129 \text{ eV.}} \end{aligned}$$

- (ii) For Germanium $\lambda = 17760 \times 10^{-10} \text{ m}$.

$$\begin{aligned} \text{So, energy gap of germanium} \\ &= \text{J.} \\ &= \end{aligned}$$

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- Ex. 2** Find the drift velocity for an electron in silver wire for radius 1 mm and carrying a current of 2 A. Density of silver is 10.5 gm/cc.
Avogadro number = $6.025 \times 10^{23}/\text{gm mole}$.

Soln :

Given :

$$\text{Density of silver} = 10.5 \text{ gm/cc.}$$

$$\text{At.wt. of silver} = 108$$

Formula required :

$$I = q \cdot n \cdot v \cdot A$$

Therefore number of electrons per unit volume = $n = \frac{\text{Density}}{\text{At.wt.}} \times \text{Avogadro number}$

$$n = \frac{10.5}{108} \times 6.025 \times 10^{23} \text{ per cm}^3$$

$$\text{or } n = 6 \times 10^{28} \text{ per m}^3$$

$$\text{Cross section area } A = \pi r^2 = \pi \times (10^{-3})^2 = 3 \times 10^{-6} \text{ m}^2$$

$$\text{Now current } I = q \cdot n \cdot v \cdot A$$

$$v = \frac{I}{q \cdot n \cdot A}$$

$$= 7 \times 10^{-4} \text{ m/s.}$$

Ex. 3 An n-type semi-conductor is to have a resistivity $10\Omega \text{ cm}$. Calculate the number of donor atoms which must be added to achieve this.
Given that $\mu_d = 500 \text{ cm}^2/\text{V.S}$

Soln :

Given :

Resistivity $\rho = 10\Omega \text{ cm}$, $\mu_d = 500 \text{ cm}^2/\text{V.S}$

Formula required :

Conductivity σ and $\sigma = n_d \cdot e \cdot \mu_d$

$$n_d = \frac{\sigma}{e \cdot \mu_d}$$

$$= 1.25$$

Ex. 4 Calculate the conductivity of specimen if a donor impurity is added to an extent of one part in 10^8 Ge atoms at room temperature?

Soln :

Given :

Avogadro number = 6.02×10^{23} atoms/gm.mole.

At.wt. of Ge = 72.6,

Density of Ge = 5.32 gm/c.c,

Mobility $\mu = 3800 \text{ cm}^2/\text{v.s}$.

Formula required :

$$\sigma = n \cdot e \cdot \mu_e$$

Concentration of Ge atoms =

As there is one donor atom per 10^8 atoms of Ge

n_d

Conductivity $\sigma = n_d \cdot \mu_e \cdot e$

$$0.268 \text{ mho/cm}$$

Ex. 5 A silver wire is in the form of ribbon 0.50 cm. wide and 0.10 mm thick. When a current of 2 amp passes through the ribbon, perpendicular to 0.80 Tesla magnetic field calculate the Hall voltage produced. The density of silver = 10.5 gm/cc

Soln :

Given :

$B = 0.8$ Tesla, Density = 10.5 gm/cc

Formula required :

$$V_H = B \cdot v \cdot d$$

The number of electrons in 1cc of silver are :

As each silver atom contributes one electron, the number of electrons per m³ = 6

$$\text{Area } A = 0.5$$

Hall voltage $V_H = B.v.d.$

The drift vel

$$V_H =$$

$$= 0.333 \text{ volts}$$

Ex. 6 A copper specimen having length 1 meter, width 1 cm and thickness 1 mm is conducting 1 amp. Current along its length and is applied with a magnetic field of 1 Tesla along its thickness. It experiences Hall effect and a hall voltage of 0.074 microvolts appears along its width. Calculate the Hall coefficient and the mobility of electrons in copper. (Conductivity of copper is $\sigma = 5.8 \times 10^7 \text{ } (\Omega\text{m}^{-1})$)

Soln :

Given :

$$l = 1 \text{ m,}$$

$$d = 1 \text{ cm} = 10^{-2} \text{ m}$$

$$W = 1 \text{ mm} = 10^{-3} \text{ m,}$$

$$I = 1 \text{ Amp}$$

$$B = 1 \text{ Tesla,}$$

$$V_H = 0.074 \times 10^{-6} \text{ Volts}$$

$$\sigma = 5.8 \times 10^7 \text{ mho/m}$$

Formula required :

$$V_H$$

The Hall voltage is

$$V_H = R_H \times$$

$$R_H =$$

$$R_H$$

Mobility

$$\mu = \sigma \times R_H =$$

$$\mu = 4.3 \times 10^{-3} \text{ m}^2/\text{volt.sec}$$

Ex. 7 A slab of copper 2.0 mm in length and 1.5 cm wide is placed in a uniform magnetic field with magnitude 0.40 T. When a current of 75 amp flows along the length, the voltage measured across the width is 0.81 μV , determine the concentration of mobile electrons in copper.

Soln :

$$V_H \quad R_H$$

$$R_H =$$

=

$$n =$$

$$= 11.79 \text{ /cu.m}$$

Ex. 8 A silver wire is in form of a ribbon 0.50cm Wide and 0.10 mm thick. When a current of 2 amp passes through the ribbon, perpendicular to 0.80 Tesla magnetic field, Calculate the Hall voltage produced. The density of silver 10.5 gm/cc. And atomic weight of Ag = 108.

Soln :

Given :

$$\begin{aligned} \text{Numbers of electrons } n &= 6.025 \times 10^{23} \times \approx 5.857 \times 10^{22} \text{ per c.c.} \\ &= 5.857 \times 10^{28} \text{ per m}^3. \end{aligned}$$

Formula :

$$V_H$$

$$V_H = 1.70 \times 10^{-6} \text{ V} = 1.7 \mu\text{V}$$

Ex. 9 Calculate the mobility of charge carriers in a doped silicon of which conductivity is 100 mho/m and the Hall coefficient is $3.6 \times 10^{-4} \text{ m}^3/\text{C}$

Soln :

Hall Co-efficient R_H

Conductivity $\sigma = 100 \text{ mho/m}$

Formulae : $\sigma = ne\mu$

$$\mu =$$

$$= 0.036 \text{ m}^2/\text{V.s}$$