

eg ① Find max & min value of
 $x^3 + 3xy^2 - 3x^2 - 3y^2 + 4$

② If $u^3 + v^3 + w^3 = x + y + z$
 $u^2 + v^2 + w^2 = x^3 + y^3 + z^3$
 $u + v + w = x^2 + y^2 + z^2$

Show that

$$\frac{\partial(u, v, w)}{\partial(x, y, z)} = \frac{(x-y)(y-z)(z-x)}{(u-v)(v-w)(w-u)}$$

③ Find point on the surface $z^2 = xy + 1$ nearest to the origin by using Lagrange's method.

Q2] Fill in the blanks

① The critical points of $x^2 + y^2 + 6x + 12$ are

② The focal length of mirror is found from the formula $\frac{1}{v} - \frac{1}{u} = \frac{2}{f}$. Find

% error in f if u & v both have 2% error.

③ If u, v & w are functionally dependent then find relatⁿ betⁿ them if

$$u = \frac{x+y}{z} \quad v = \frac{y+z}{x} \quad w = \frac{y(x+y+z)}{xz}$$

④ Find $\frac{\partial(u, v)}{\partial(x, y)}$ if $x = u \cos v$
 $y = u \sin v$