## **CONTENTS**

1 Stability

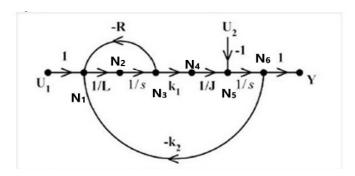
Abstract—This manual is an introduction to control systems based on GATE problems.Links to sample Python codes are available in the text.

Download python codes using

## 1 STABILITY

## 2 ROUTH HURWITZ CRITERION

2.1. In a system whose signal flow graph is shown in the figure,  $U_1(s)$  and  $U_2(s)$  are inputs. The transfer function  $\frac{Y(s)}{U_1(s)}$  is



## **Solution:**

$$\frac{Y(s)}{U_1(s)}\Big|_{U_2(s)=0}$$
 (2.1.1)

Using Matrix Formula:

The transition equations are

$$N_1 = U_1 - RN_3 - k_2N_6 (2.1.2)$$

$$N_2 = \frac{N_1}{L} {(2.1.3)}$$

$$N_3 = \frac{N_2}{s} \tag{2.1.4}$$

$$N_4 = k_1 N_3 \tag{2.1.5}$$

$$N_5 = \frac{N_4}{J} \tag{2.1.6}$$

$$N_6 = \frac{N_5}{s} \tag{2.1.7}$$

State Transition Matrix:

1

$$\mathbf{T} = \begin{pmatrix} 0 & 0 & -R & 0 & 0 & -k_2 \\ \frac{1}{L} & 0 & 0 & 0 & 0 & 0 \\ 0 & \frac{1}{s} & 0 & 0 & 0 & 0 \\ 0 & 0 & k_1 & 0 & 0 & 0 \\ 0 & 0 & 0 & \frac{1}{J} & 0 & 0 \\ 0 & 0 & 0 & 0 & \frac{1}{L} & 0 \end{pmatrix}$$
 (2.1.8)

$$\mathbf{U} = (\mathbf{I} - \mathbf{T})^{-1} \tag{2.1.9}$$

$$(\mathbf{I} - \mathbf{T}) = \begin{pmatrix} 1 & 0 & R & 0 & 0 & k_2 \\ \frac{-1}{L} & 1 & 0 & 0 & 0 & 0 \\ 0 & \frac{-1}{s} & 1 & 0 & 0 & 0 \\ 0 & 0 & -k_2 & 1 & 0 & 0 \\ 0 & 0 & 0 & \frac{-1}{J} & 1 & 0 \\ 0 & 0 & 0 & 0 & \frac{-1}{s} & 1 \end{pmatrix}$$
(2.1.10)

 $U_{50}$  will be the gain of the system

$$\mathbf{U_{50}} = \frac{\begin{vmatrix} \frac{-1}{L} & 1 & 0 & 0 & 0 \\ 0 & \frac{-1}{s} & 1 & 0 & 0 \\ 0 & 0 & -k_2 & 1 & 0 \\ 0 & 0 & 0 & \frac{-1}{J} & 1 \\ 0 & 0 & 0 & 0 & \frac{-1}{s} \end{vmatrix}}{\begin{pmatrix} 1 & 0 & R & 0 & 0 & k_2 \\ \frac{-1}{L} & 1 & 0 & 0 & 0 & 0 \\ 0 & \frac{-1}{s} & 1 & 0 & 0 & 0 \\ 0 & 0 & -k_2 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & \frac{-1}{J} & 1 & 0 \\ 0 & 0 & 0 & 0 & \frac{-1}{J} & 1 \end{pmatrix}}$$
(2.1.11)

Gain can be found by cofactor expansion or else by running the code in (1.2.5). Gain obtained is

$$\frac{Y(s)}{U_1(s)} = \frac{k_1}{s^2 L J + sRJ + k_1 k_2}$$
 (2.1.12)

3 Compensators

4 NYOUIST PLOT