



Routh's Method

Examine the **absolute stability** of the system having following **characteristic equation**, using Routh's method and **verify** using extraction of **poles**.

$$s^3 + 4s^2 + 6s + 4 = 0$$

1	6
4	4
5	0
4	0

No Sign change, system stable.

-2.0000
-1.0000 - 1.0000i
-1.0000 + 1.0000i



Routh's Method

Construct **Routh's** array for the following **characteristic** equations and **determine** the number of **poles** either on **imaginary** axis or in the **right** half of s-plane.

$$s^5 + 4s^4 + 6s^3 + 24s^2 + 25s + 100 = 0$$

1	6	25
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4	24	100
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0(16)	0(48)	0
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12	100	0
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-85.3	0
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100	Zero Row → poles symmetric
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Two sign changes → 2 poles in RH

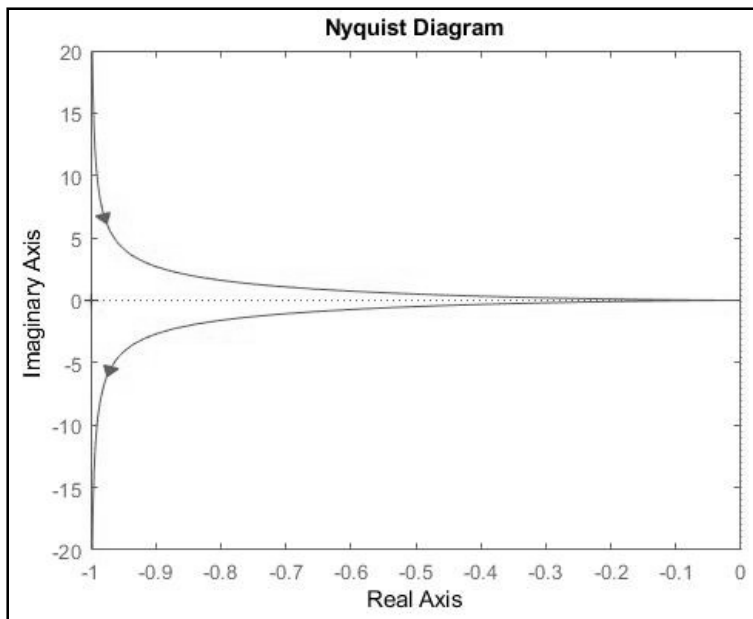
-4.0000
-1.0000 - 2.0000i
-1.0000 + 2.0000i
1.0000 - 2.0000i
1.0000 + 2.0000i



Nyquist Stability Analysis

Examine **closed loop** absolute stability of following **plant** using **Nyquist** stability criterion and **verify** the same using the actual **closed loop pole locations**.

$$G(s) = \frac{1}{s(s-1)}$$



1 Clockwise encirclement
i.e. $N = 1$, $P = 1$, So, $Z = 2$
Closed loop unstable.

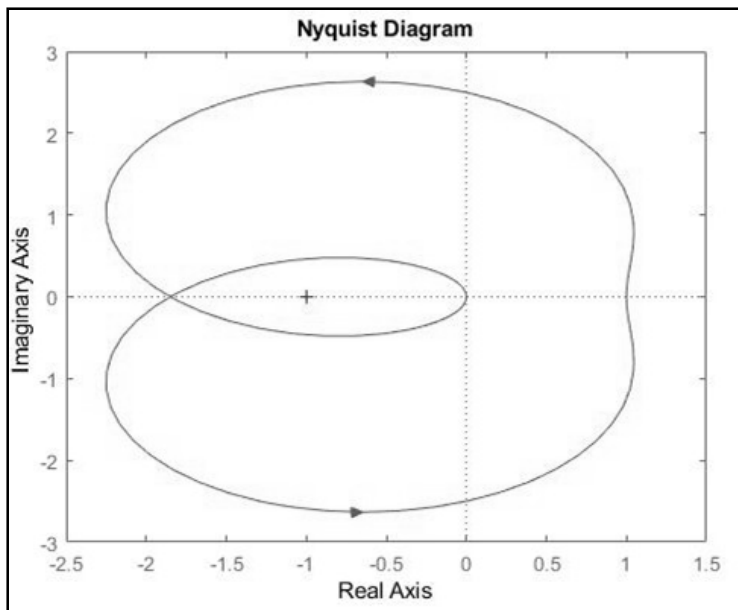
$$0.5000 + 0.8660i$$
$$0.5000 - 0.8660i$$



Nyquist Stability Analysis

Examine **closed loop** absolute stability of following **plant** using **Nyquist** stability criterion and **verify** the same using the actual closed loop pole locations.

$$G(s) = \frac{s^2 + 2s + 1}{s^3 + 0.2s^2 + s + 1}$$



1 Clockwise encirclement
i.e. $N = -2$, $P = 2$, So, $Z = 0$
Closed loop stable.

-0.751
-0.2240 + 1.6200i
-0.2240 - 1.6200i