



# Control Elements

*Applicable Mathematical Actions*

*Basic Control Actions*



# *Control Element Configuration*

We see that **basic** mathematical **operations** e.g. scaling, (**K**), integration, (**1/s**) and differentiation, (**s**), are **able** to achieve the **desired** performance **attributes**.

Therefore, we can set up **closed** loop control **systems** by incorporating these **mathematical** actions in the unity feedback control **structure**.

However, we need to **understand** their implications so that we can **link** these to complex control **objectives**.

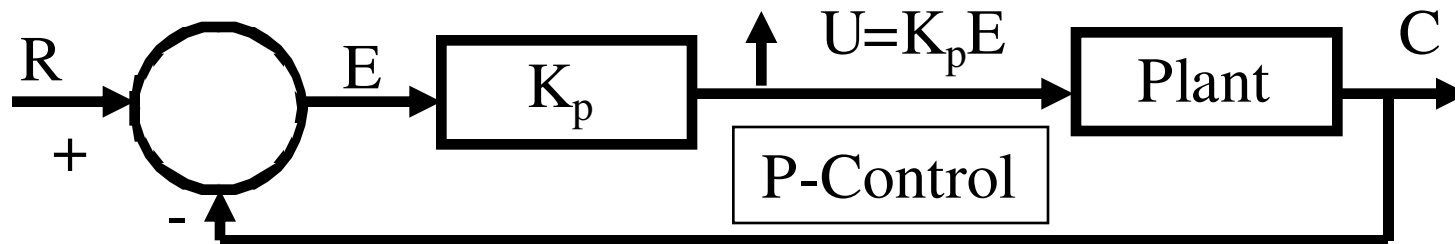


# ***Basic Control Elements***

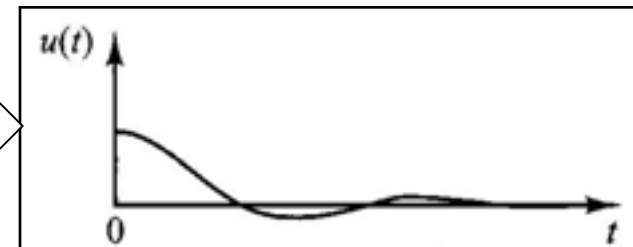
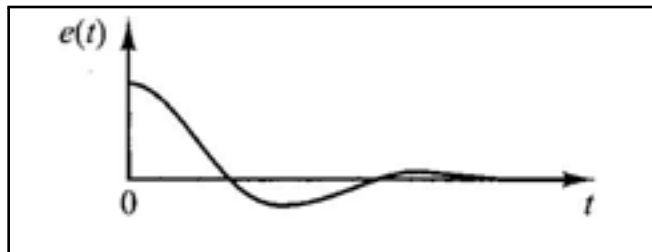


## *Scaling or P- Control Action*

**P – control** is defined by  $H(s) = K_p$ , a constant. The basic **structure** of the control **action** is as shown below.



This is termed ‘**Proportional**’ control due to **input**  $u(t)$  being proportional to **error**  $e(t)$ , as shown below.





## ***P – Control Features***

**P – control** remains **active** for non-zero values of  **$e(t)$** . Further, **higher** error, leads to **larger** action.

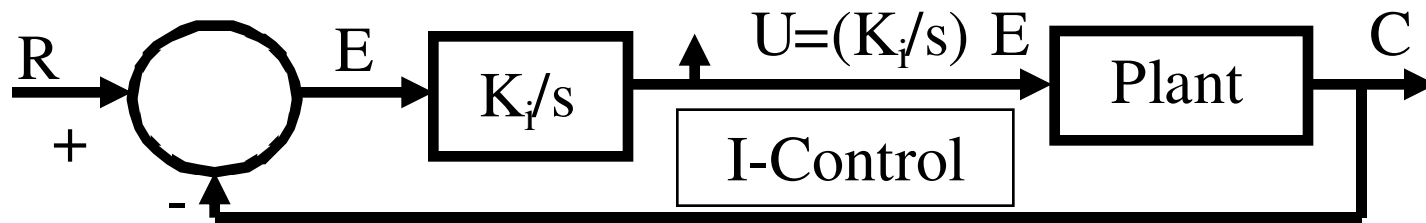
It is also seen that if ' **$K_p$** ' is higher, **same** error results in **larger** control action, causing **tighter** control.

P – control is the **simplest** and hence, is **common** in most **situations** as it has the **ability** to achieve all **objectives**.

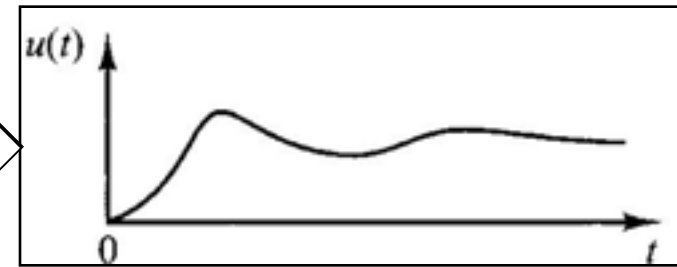
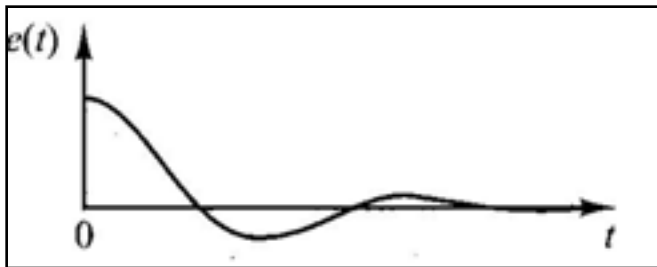


## *Integral or I- Control Action*

**I** (or integral) **control** is defined by  $H(s) = K_i/s$ . Basic **structure** of such a control **action** is as shown below.



This is termed '**I**' **control**, due to **input**  $u(t)$  being proportional to  $\int e(t)$ , as shown below.





## ***I- Control Features***

In this case, the **control** action **continues** till the **accumulated** error remains **non-zero**.

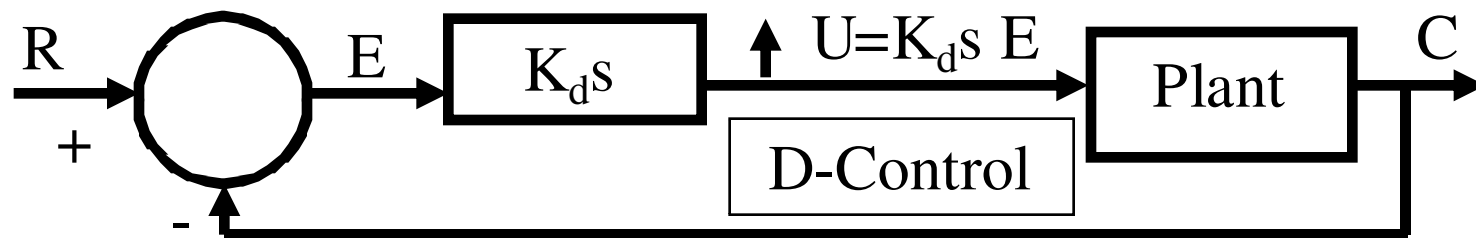
Thus, we find that control **action** continues long after the **instantaneous** error has gone to **zero** and hence, makes the **control** action more **appropriate** for tracking **task**.

However, it also takes a **long time** for  $u(t)$  to go to **zero**, thus **delaying** the steady-state.



## ***Derivative or D- Control Action***

**D** or derivative control action is defined by  $H(s) = K_d s$ . Given below is the **schematic** of the above **action**.



In general, control **element** with a **derivative** action results in a highly **sensitive** system because **u(t)** can be **non-zero** even if the **e(t)** is zero.





## ***D- Control Features***

In the context of **D-control**, the control action starts **even before** the error has time to **build-up**.

This is some form of **anticipation** that the system **acquires**, which does not **allow** error to **build-up** and, therefore, has the ability to reach the steady-state **faster**.

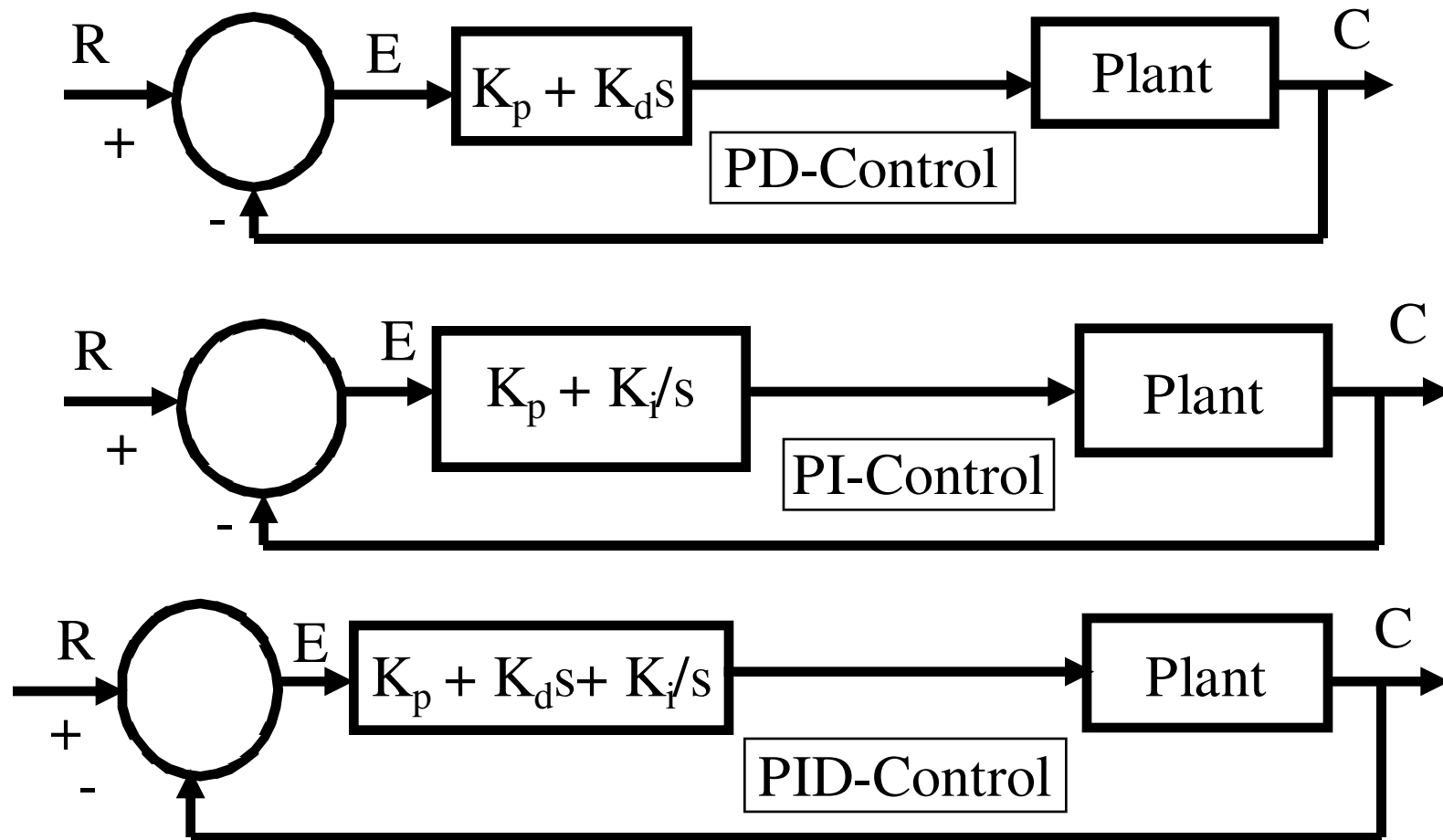
‘**D**’ control is, therefore, **ideal** for disturbance **rejection**.

However, there can be significantly **larger** control input at the **start**, which can also become **unbounded** in some situations and, hence, is generally **not desirable**.



## *Additional Control Actions*

As **P, I & D** actions are **linear**, their **combinations** also result in **additional linear control actions**, as below.





## *Summary*

**P, D & I** are the fundamental **building blocks** of control **elements**, which provide **adequate DOFs** for varied control **objectives**.