

EE301 Tutorial 8 (Antennas)

1. A z-oriented Hertz dipole of 0.1λ length at 10 MHz is located at the origin and excited with 100 A peak current. Find the vector electric and magnetic fields at a distance of 1 m, 100 m and 10 km along the z-axis, and in the xy-plane.
2. For a 1 MHz Hertz dipole, find the distance beyond which the reactive fields are less than 10% of the radiation fields.
3. Find the solid angle Ω on a spherical surface that is between $\theta = 20^\circ$ and $\theta = 40^\circ$ and between $\phi = 30^\circ$ and $\phi = 70^\circ$.
4. Find the maximum electric and magnetic field strengths which one would get from a $\lambda/2$ dipole at 1 GHz at a distance of 10 km from the dipole. The dipole is excited with 10 A rms current.
5. Find total power radiated by antenna in problem 4.
6. An antenna has a field pattern given by $E(\theta) = \cos\theta \cdot \cos 2\theta$ for $0^\circ \leq \theta \leq 90^\circ$. Find (a) the half-power beamwidth (HPBW) and (b) the beamwidth between first nulls (FNBW).
7. The field radiation pattern of an antenna is given by

$$F(\theta) = \frac{1}{2} \cos^4 \theta, \quad 0 \leq \theta \leq \frac{\pi}{2}, \quad 0 \leq \phi \leq 2\pi$$

and zero elsewhere. Find the directivity.

8. The radial component of the radiated power density of an antenna is given by

$$W_{rad} = \hat{a}_r W_r = \hat{a}_r A_0 \sin \theta / r^2 \text{ (W / m}^2\text{)}$$

where,

A_0 is the peak value of the power density,

θ is the usual spherical coordinate, and

\hat{a}_r is the radial unit vector.

Determine the total radiated power.

9. Find the expression for radiation resistance of a loop antenna and find its value for a loop antenna with radius of 4.5 cm carrying peak current of 1 A at 1 GHz.
10. Consider the current distribution on a thin $\lambda/2$ ($= 1\text{m}$) dipole antenna as $[0, 1, 3, 5, 5, 5, 3, 1, 0]$ mA determined by using MoM formulation. Determine the value of electric field at (2 m, 60° , 90°).