



Time Domain Specifications

For a closed loop **2nd order** transfer function having a peak overshoot of **9.5%** and settling time (5%) of **1 sec**, determine the **rise** time and **peak** time and **verify** these.

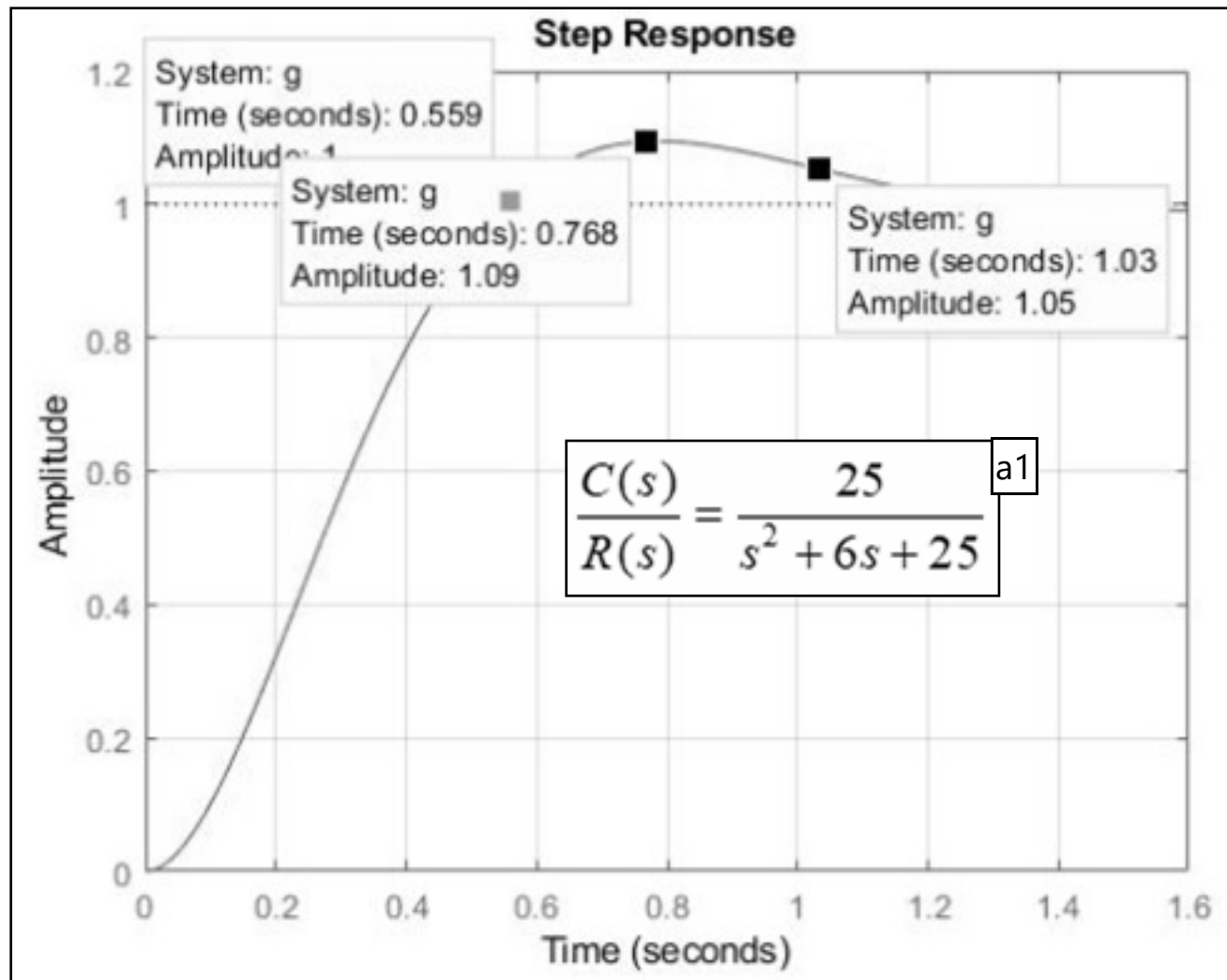
$$M_p = 0.095 = e^{-\pi\zeta/\sqrt{1-\zeta^2}} \rightarrow \frac{\zeta}{\sqrt{1-\zeta^2}} = 0.749$$

$$\zeta = 0.6; \quad T_s(5\%) = 1 = \frac{3}{\sigma} \rightarrow \sigma = 3; \quad \omega_n = 5.0$$

$$\omega_d = 4.0; \quad T_p = \frac{\pi}{\omega_d} = 0.78s; \quad T_r = \frac{1}{\omega_d} \tan^{-1} \left(\frac{\omega_d}{-\sigma} \right) = 0.55s$$



Verification with MATLAB



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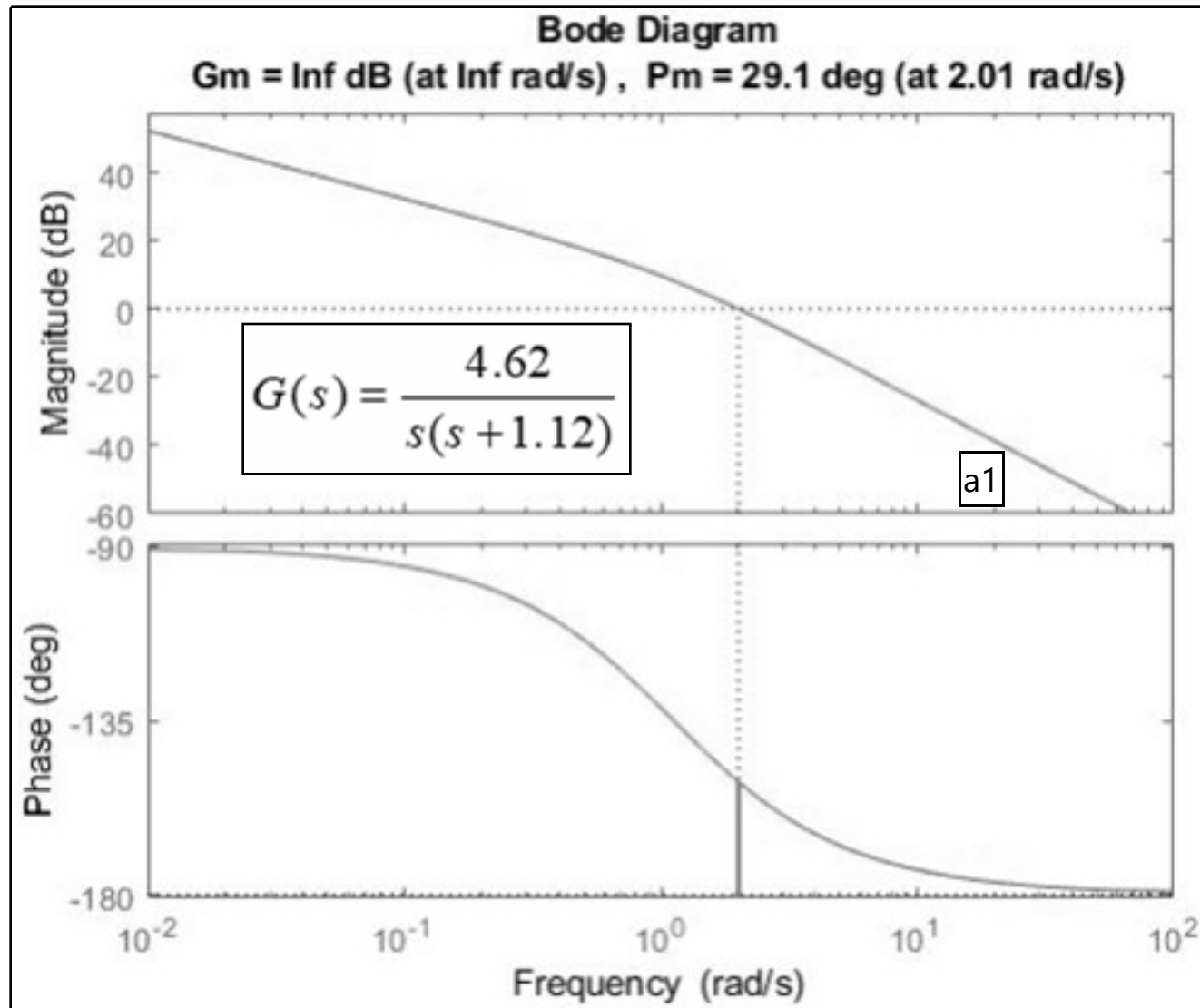
PM & GCO Specifications

A **closed loop** system needs to have a **PM of 30°** at a **GCO of 2 rad/s**. Determine corresponding closed loop **transfer function** and time domain **response** features.

$$PM^\circ = 30 \rightarrow \zeta \approx 0.3(0.26); \quad \omega_{GCO} = 2 = \omega_n \sqrt{\sqrt{1 + 4\zeta^4} - 2\zeta^2}$$
$$\omega_n = 2.15; \quad \sigma = 0.56; \quad \frac{C(s)}{R(s)} = \frac{4.62}{s^2 + 1.12s + 4.62}$$



Verification with MATLAB



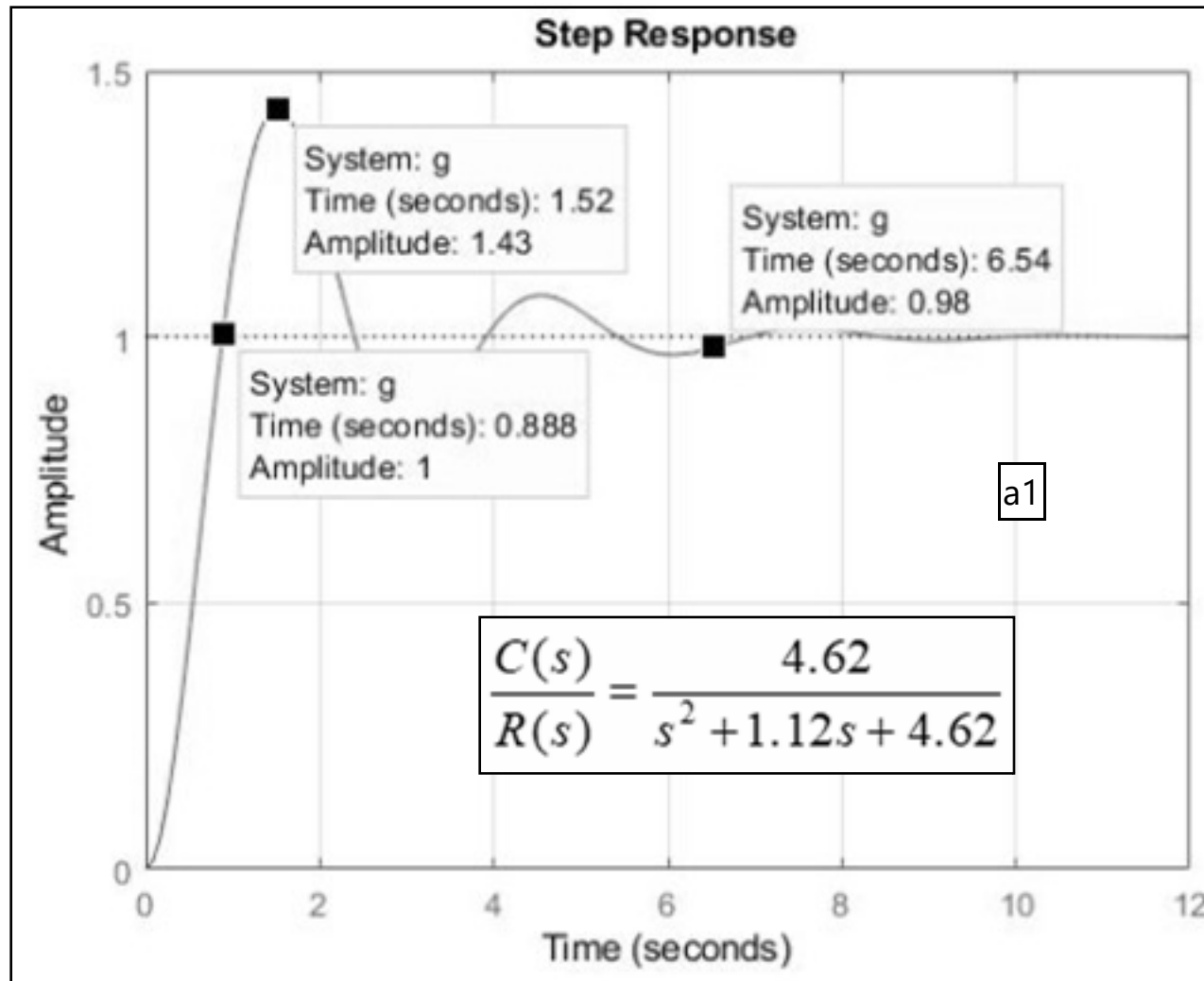
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Resonant Peak & Bandwidth

Consider a closed loop system with M_r of 2 dB and **bandwidth** of 3 rad/s. **Determine** the peak overshoot, settling time (2%), **including** GCO and PM.

$$M_r = 2dB = 1.26 = \frac{1}{2\zeta\sqrt{1-\zeta^2}} \rightarrow \zeta = 0.196; \quad \omega_r = 1.88$$

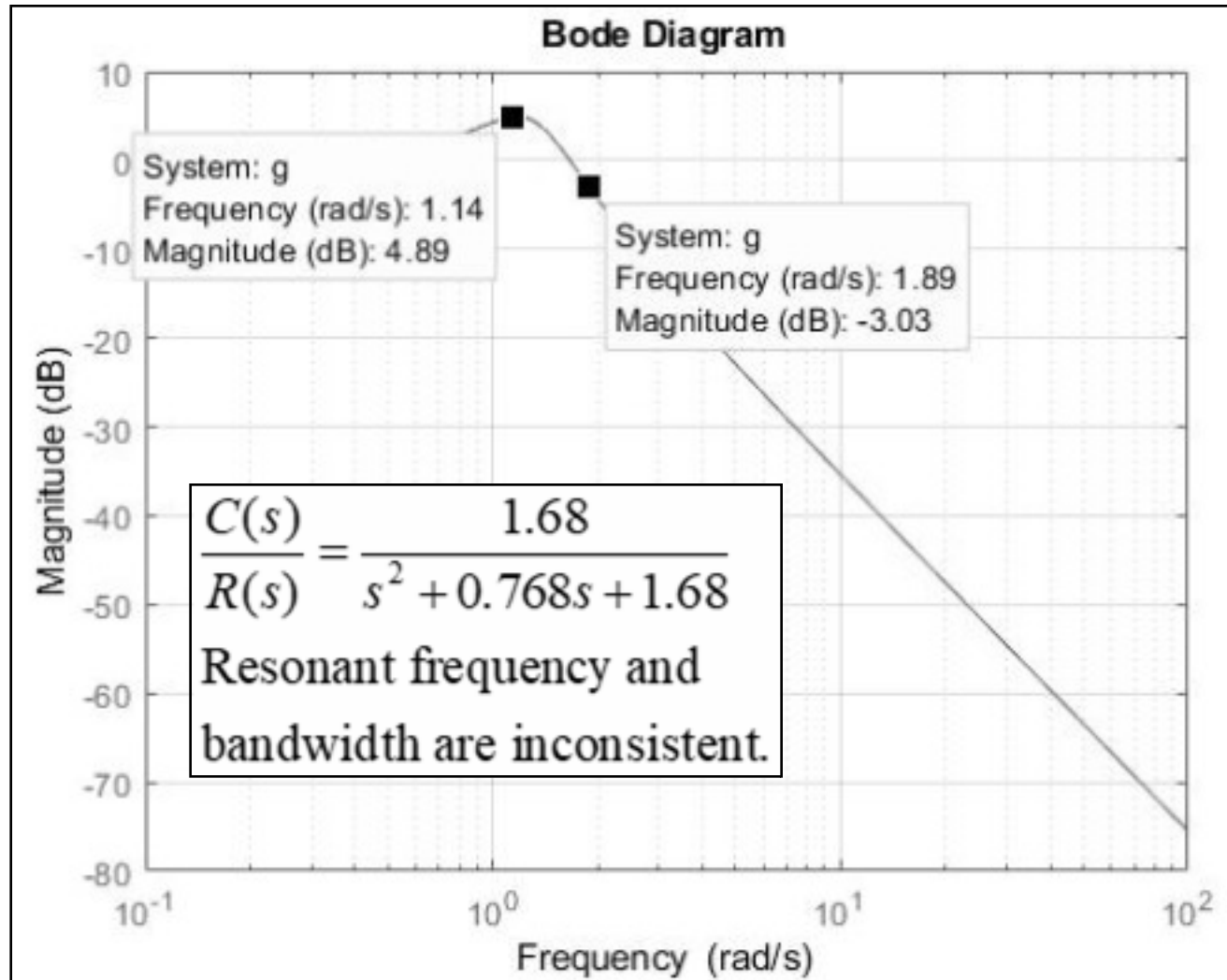
$$\omega_b = 3 = \omega_n \sqrt{\sqrt{(1-2\zeta^2)^2 + 1} + (1-2\zeta^2)} \rightarrow \omega_n = 1.96$$

$$\sigma = 0.384; \quad \omega_d = 1.92; \quad M_p = 0.53(53\%); \quad T_s = \frac{4}{\sigma} = 10.4s$$

$$PM \approx 19.6^\circ; \quad \omega_{GCO} = \omega_n \sqrt{\sqrt{1+4\zeta^4} - 2\zeta^2} = 1.29$$

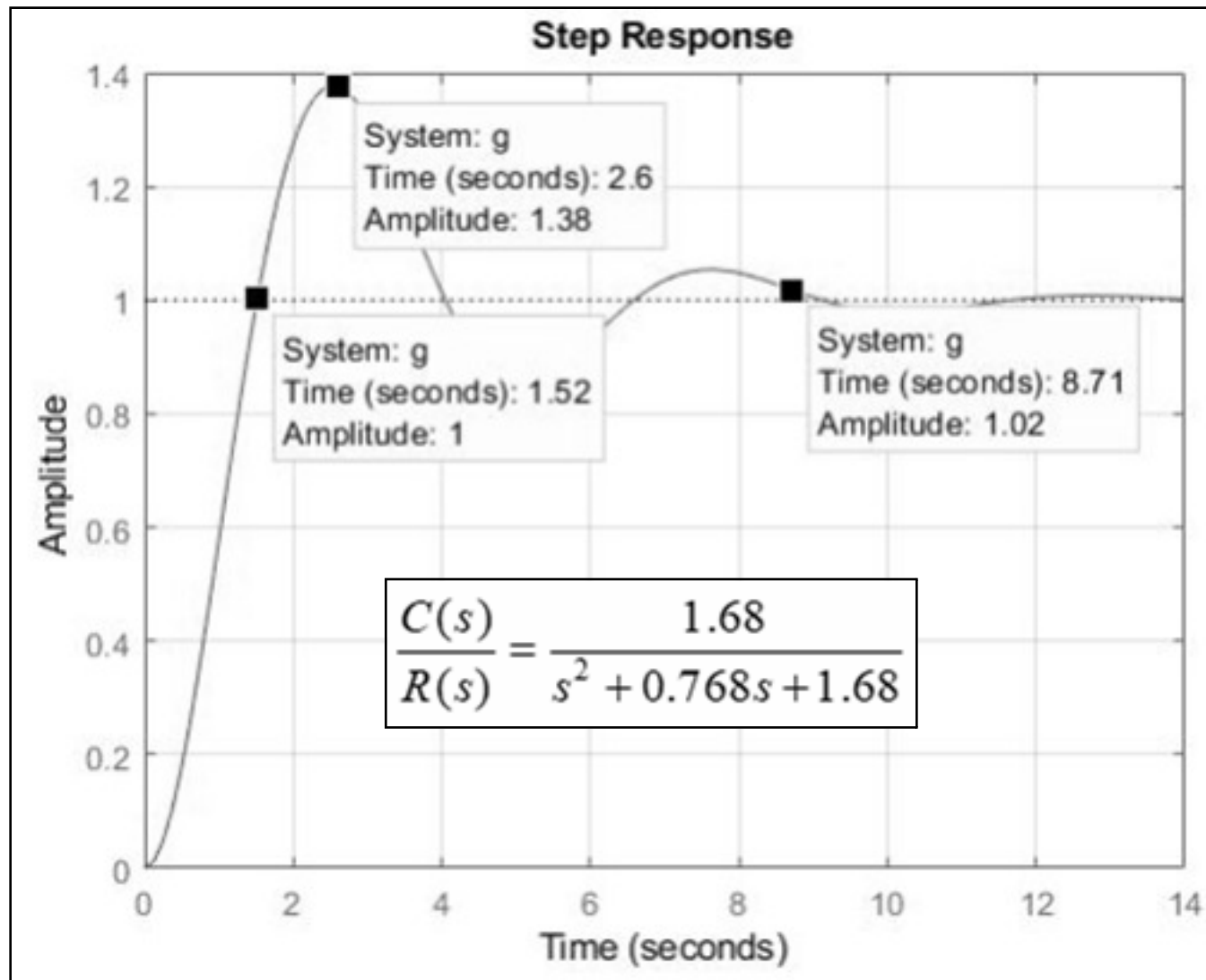


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