

Name: _____

Roll No. _____

Choose only one option which is the most appropriate for questions 1 - 5.

1. Laplace transform of unit impulse input is

- (a) $1/s$
- (b) s
- (c) 1
- (d) t

2. Laplace transform of $c(t)$ (i.e. $C(s)$) as described by equation $T\dot{c}(t) + c(t) = 0$ is

- (a) $c(0)/(s + T)$
- (b) $sc(0)/(Ts + 1)$
- (c) $c(0)/(Ts + 1)$
- (d) $sc(0)/(s + T)$

3. For Laplace transform to exist $f(t)$ should

- (a) tend to zero as $t \rightarrow \infty$
- (b) tend to zero as $t \rightarrow 0$
- (c) be continuous and 1st derivative should exist
- (d) be at least piece-wise continuous

4. In the context of unit impulse response of a second order system, $g(0+)$ is

- (a) $1/m$
- (b) 0
- (c) $1/k$
- (d) $1/c$

5. In the convolution integral approach, input is modelled as a sequence of

- (a) ramps of unit slope
- (b) ramps of width ' $d\tau$ '
- (c) rectangles of unit height
- (d) rectangles of width ' $d\tau$ '

Give short (1 - 2 lines) answer to the questions 6-10.

6. Give the expression for unit impulse response of the following system. $T\dot{c}(t) + c(t) = r(t)$

$$g(t) = \left(\frac{1}{T} \right) e^{-t/T}$$

..... 2 (PTO)

7. Give the expression for $y(t)$ for a system having $g(t)$ as impulse response and $u(t)$ as the input, using the convolution concept.

$$y(t) = \int_0^t g(t-\tau)u(\tau)d\tau$$

8. Give the integral expression for the Laplace transform $F(s)$ of a function $f(t)$.

$$F(s) = \int_0^{\infty} e^{-st} f(t)dt$$

9. What is the main limitation of the convolution integral approach for generating the forced response?

The main limitation of the convolution integral approach is its lack of scalability for higher order systems and arbitrary inputs.

10. How can we obtain the Laplace transform for the integral of a function?

We can obtain the Laplace transform of integral of a function by dividing the Laplace transform of the function by the Laplace variable, 's'.