



Minimum Phase Root Locus

Generate **straight line** root locus of following **plant** and determine the **approximate** value of '**K**' for which the **closed loop** system has all **poles** to the left of **-0.5**.

$$G(s) = \frac{K}{(s+1)^4}$$

Poles: $-1, -1, -1, -1$; $n = 4$; $m = 0$; $n - m = 4$

Real axis: No root on real axis as $(n + m) = 0$ on both sides.

Asymptotes: $\phi = \frac{\pm(2k+1)180}{n-m} = \pm 45^\circ; \pm 135^\circ; \sigma = -1$

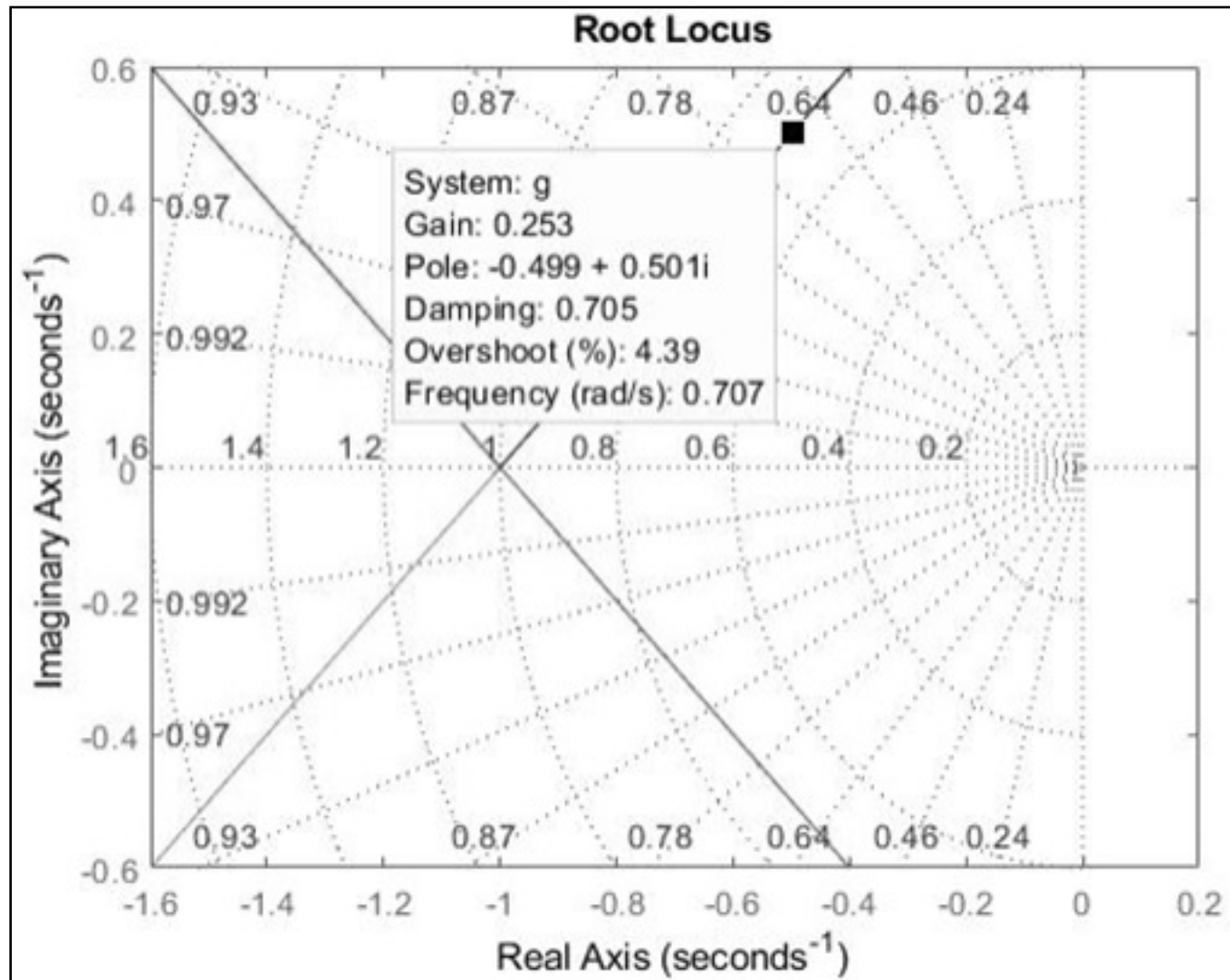
Break-away: $K(s) = -(s+1)^4 \rightarrow \frac{dK}{ds} = -4(s+1)^3 = 0 \rightarrow s = -1$

Imaginary axis: $s^4 + 4s^3 + 6s^2 + 4s + (K+1) = 0 \rightarrow K = 4; s = \pm j1$

Dominant Poles: $s = -0.5 \pm j0.5; K = -(0.5 + j0.5)^4 = 0.25$



Verification with MATLAB





Non-minimum Phase Root Locus

Generate and **sketch** the asymptotic root locus **plot** for the following **system** and compare it with the case when there is **no time delay**. (Use 1st order Pade' approximation).

$$G(s) = \frac{4e^{-2s}}{(s+1)^3}$$

$$G(s) = \frac{4(1-s)}{(s+1)^4}; \quad \text{Poles: } -1, -1, -1, -1; \quad \text{Zero: } 1; \quad n-m=3$$

Real axis: RL between +1 & ∞ ; Asymptotes: $\phi = \pm 120, +360$

$\sigma = -2/3$; BA: $s = -1; +5/3$; Imag axis: $K = 0.475$; $\omega = 0.73$

$$G(s) = \frac{4}{(s+1)^3}; \quad \text{Poles: } -1, -1, -1; \quad n-m=3$$

Real axis: No RL; Asymptotes: $\phi = \pm 60, 180$; $\sigma = -1$

BA: $s = -1$; Imag axis: $K = 2$; $s = -\sqrt{3}$



Verification with MATLAB

