



## ***2<sup>nd</sup> Order System Bode Plot - Analytical***

Obtain the **asymptotic bode plot** and compare it with the plot from **MATLAB**.

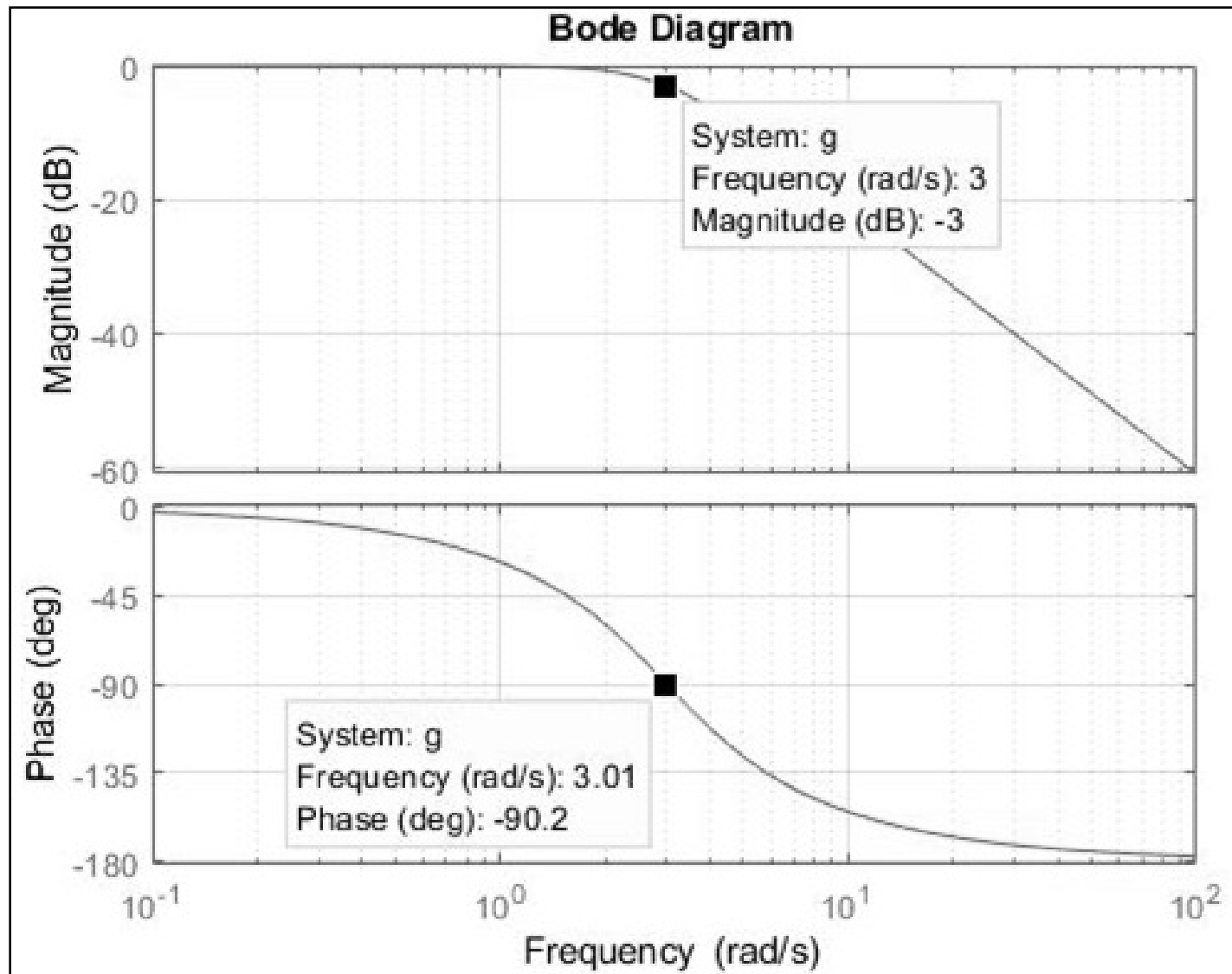
$$G(s) = \frac{9}{(s^2 + 4.24s + 9)}$$

$$\begin{aligned} |G(j0)| &= 0dB; \quad \angle G(j0) = 0^\circ; \quad \frac{d|G(j0)|}{d\omega} = 0dB / dec \\ \frac{dG(j\infty)}{d\omega} &= -40dB / dec; \quad |G(j3)| = -3dB; \quad \angle G(j3) = -90^\circ \\ |G(j\infty)| &= -\infty dB; \quad \angle G(j\infty) = -180^\circ \end{aligned}$$

We see that  $\omega = 3$  acts like a **corner** frequency so that we can **draw** the  $\omega = \infty$  **asymptote** through this **point**.



## *2<sup>nd</sup> Order System Bode Plot - MATLAB*





## *2<sup>nd</sup> Order System Nyquist Plot*

Obtain the one-sided **Nyquist plot** and compare it with the plot from **MATLAB**.

$$G(s) = \frac{9}{(s^2 + 4.24s + 9)}$$

$$\begin{aligned} |G(j0)| &= 1; \quad \angle G(j0) = 0^\circ; \quad |G(j1)| = 0.99; \quad \angle G(j1) = -28^\circ \\ |G(j2)| &= 0.91; \quad \angle G(j2) = -59^\circ; \quad |G(j3)| = 0.707; \quad \angle G(j3) = -90^\circ \\ |G(j4)| &= 0.49; \quad \angle G(j4) = -112^\circ; \quad |G(j\infty)| = 0 \quad \angle G(j\infty) = -180^\circ \end{aligned}$$

We see that for  $\omega = \infty$ , the **plot** is tangent to **–ve real** axis.



## *2<sup>nd</sup> Order System Nyquist Plot - MATLAB*

