

(1.)

DFS

DFS stands for Depth First Search is an edge based technique.

It uses Stack data structure.

BFS consider all neighbours first and therefore not suitable for decision making trees used in game or puzzles.

Here, siblings are visited before the children.

In BFS, there is no concept of backtracking

Requires more memory

Application → Bipartite & Shortest path

BFS

BFS stands for Breadth First Search is vertex based technique for finding shortest path in graph.

It uses queue data structure.

DFS is more suitable ~~between nodes~~ ~~between nodes~~ ~~from source~~ for game or puzzle problems.

Here, children are visited before the siblings.

DFS algorithm is recursive algorithm that uses the idea of backtracking.

Require less memory.

→ Acyclic & Topological Order.



2. Breadth first Search uses queue data structure because it remembers to get the next vertex to start a search, when a dead end occurs in any iteration.

Depth first Search use Stack data structure because it remembers to get the next vertex to start a search, when a dead end occurs in any iteration.

3. In a dense graph, every pair of vertices is connected by one edge.

The Sparse graph is completely the opposite if a graph has only a few edges (the number of edges is close to the maximum number of edges), then it is a Sparse graph.

4. Steps involved in detecting cycle in a directed graph using BFS.

Step 1: Compute in-degree (number of incoming ~~edges~~ edges) for each of the vertex present in the graph and initialize the count of visited nodes as 0.

Step 2: Pick all vertices with in-degree as 0 and add them into a queue.



Step 3: Remove a vertex from the queue and then

- ① Increment count of visited nodes by 1.
- ② Decrease in degree by 1 for all its neighbouring nodes.
- ③ If in-degree of a neighbouring nodes is reduced to zero, then add it to the queue.

Step 4: Repeat Step 3 until the queue is empty.

Step 5: If count of visited nodes is not equal to the number of nodes in the graph has cycle, otherwise not.

Using DFS

- ① Create the graph using the given number of edges and vertices.
- ② Create a recursive function that initialize the current index or vertex, visited, & recursion stack.
- ③ Mark the current node as visited and also mark the index in recursion stack

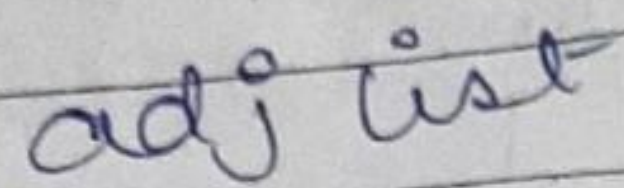


- ④ Find all the vertices which are not visited and are adjacent to the current node. Recursively call the function for those vertices, if the recursive function returns true, return true.
- ⑤ If the adjacent vertices are already marked in the recursion stack then return true, return true.
- ⑥ Create a wrapper class, that calls the recursive function for all the vertices and if any function returns true, return true else if for all vertices the function returns false - return false.

5. The disjoint set data-structure is also known as union-find data structure and merge-find set. It is a data structure that contains a collection of disjoint or non-overlapping sets.

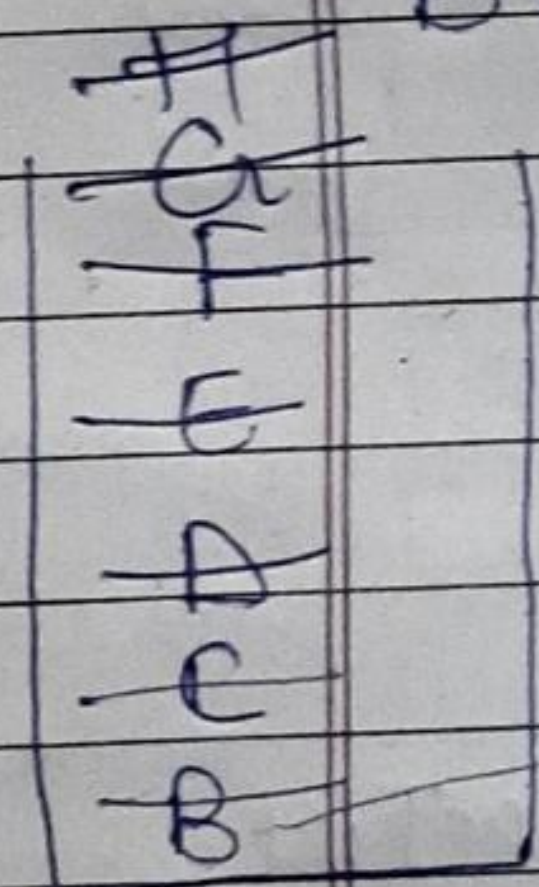
The disjoint set means that when the set is partitioned into the disjoint sets or subsets.



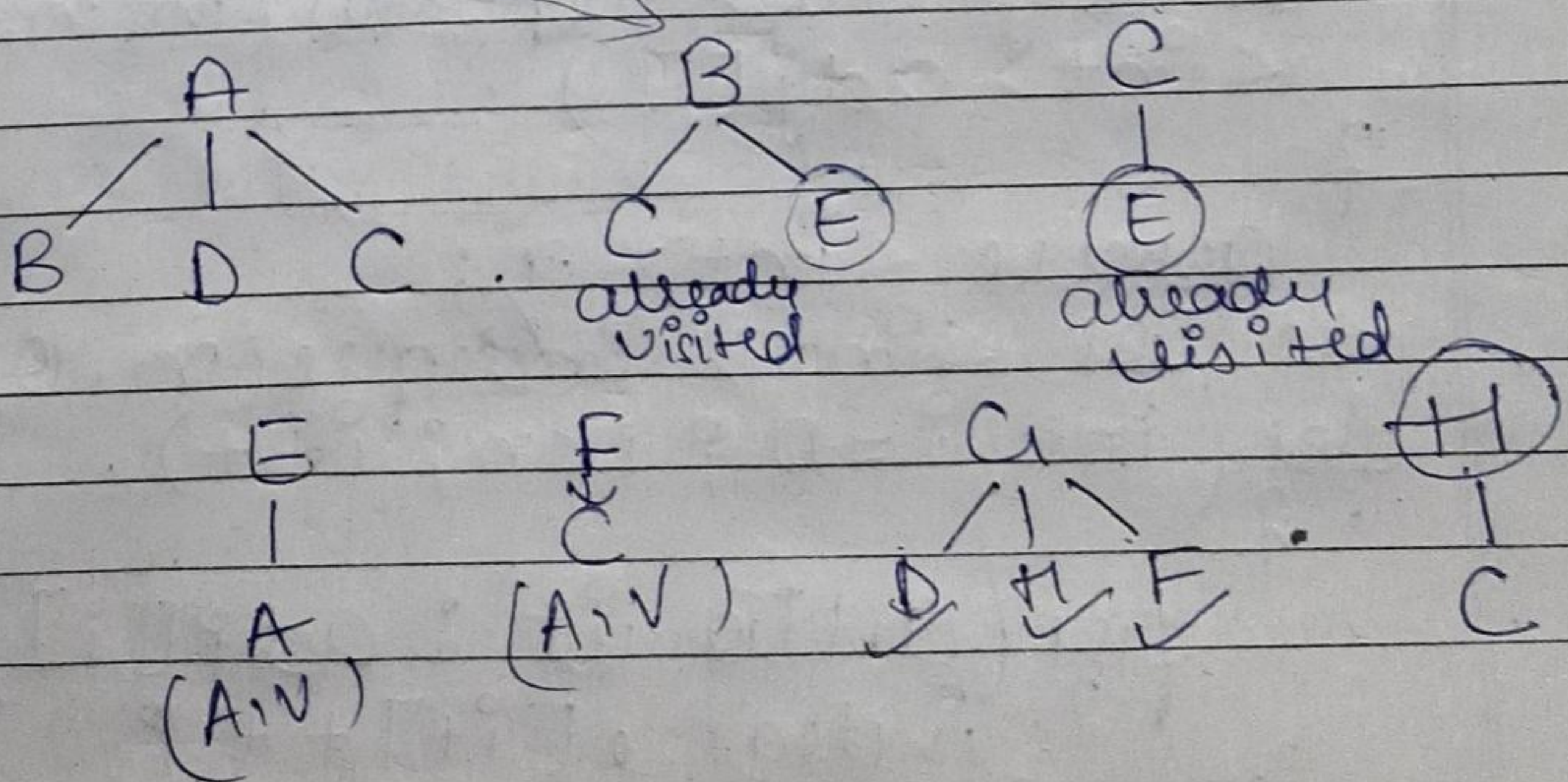


A	B, D, C.
B	C, E
C	E
D	C, F.
E	<del>A</del>
F	C
G	D, H, F.
H	C

BFS,  $src = A$  :  $dest = H$

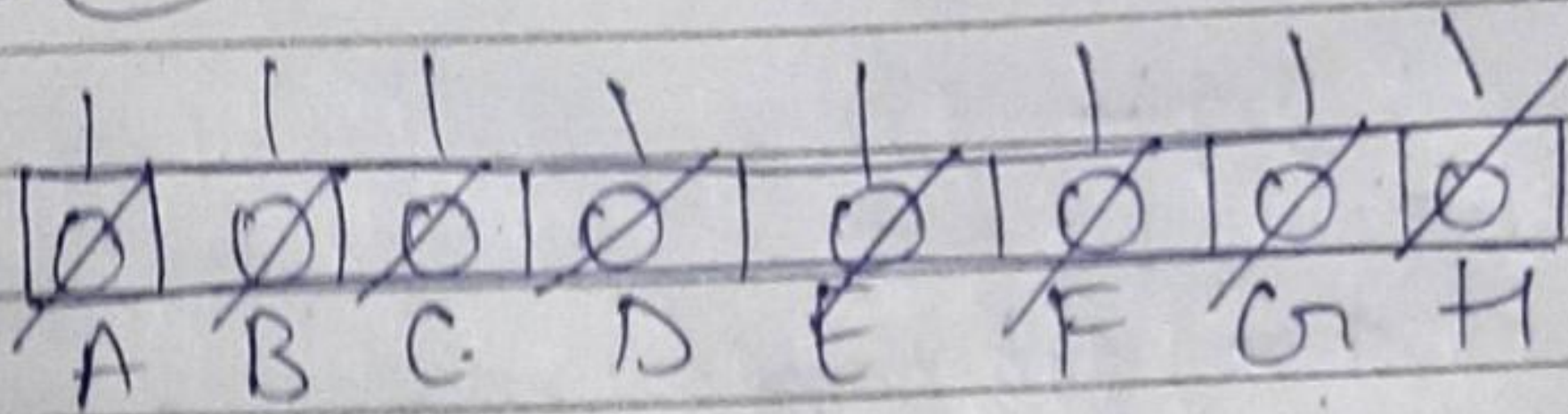
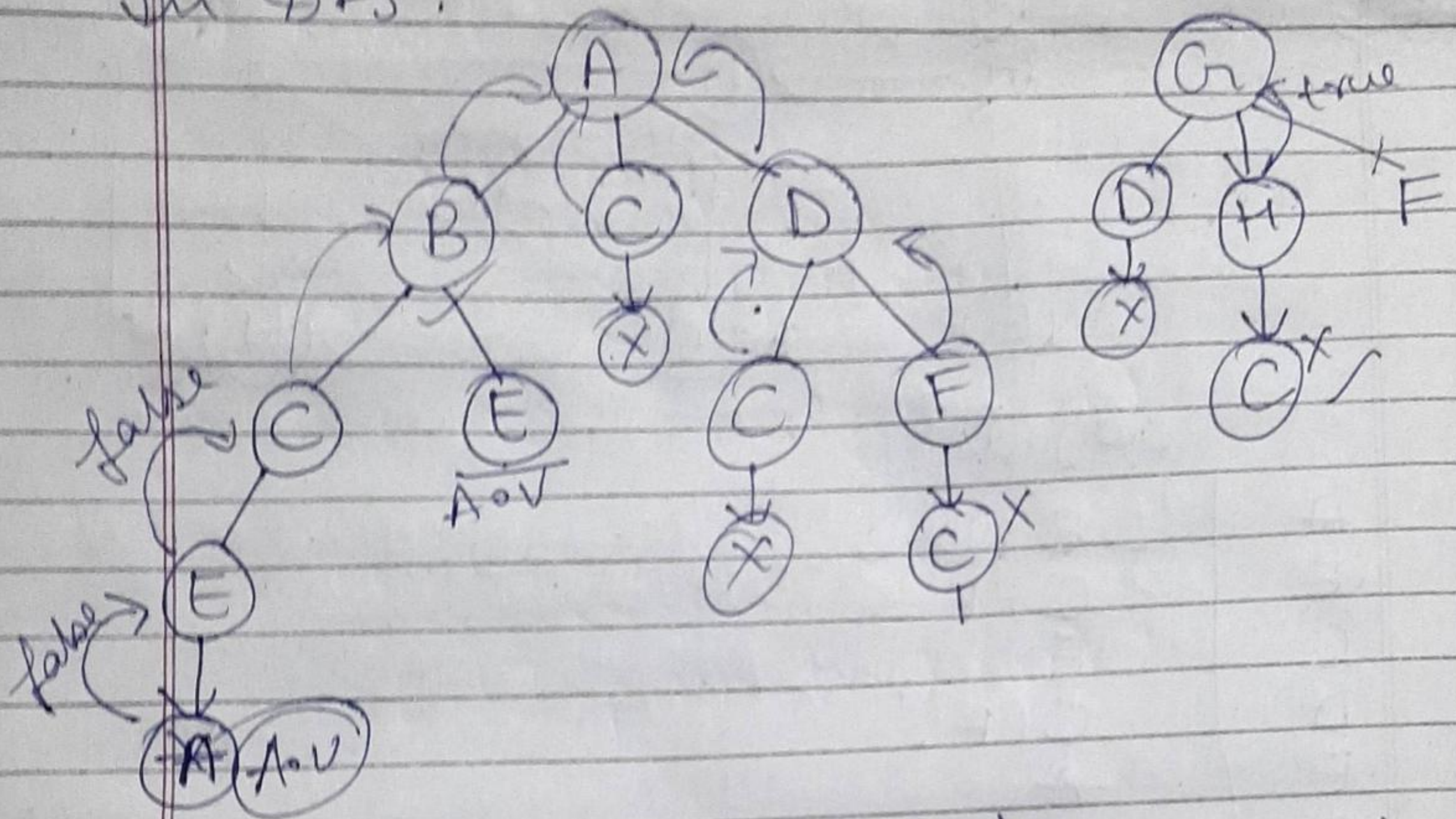


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In DFS.



8. #include <bits/stdc++.h>.  
using namespace std;

class Topological\_Sort.

```
{
public:
vector<int> topSort(int n, vector<int> adj[])
{
    queue<int> q;
    vector<int> indegree(n, 0);
    for (int i = 0; i < n; i++)
    {
        for (auto it : adj[i])
        {
            indegree[it]++;
        }
    }
}
```



```
for (int i = 0; i < n; i++) {
```

```
    cout << indegree[i];
```

```
    cout << endl;
```

```
} for (int i = 0; i < n; i++) {
```

```
    if (indegree[i] == 0) {
```

```
        q.push(i);
```

```
    }
```

```
vector<int> topo;
```

```
while (!q.empty()) {
```

```
    int node = q.front();
```

```
    q.pop();
```

```
    topo.push_back(node);
```

```
    for (auto it : adj[node]) {
```

```
        indegree[it]--;
```

```
        if (indegree[it] == 0) {
```

```
            q.push(it);
```

```
        }
```

```
    }
```

```
    return topo; }
```



```
int main()
{
    int nodes, edges;
    cin >> nodes >> edges;
    vector<int> adj[nodes+1];

    for(int i=0; i<edges; i++)
    {
        int u, v;
        cin >> u >> v;
        adj[u].push_back(v);
    }
}
```

```
Topological-Sort tps;
vector<int> ans;
ans = tps.toposort(nodes+1, adj);

for(int i=0; i<ans.size(); i++)
{
    cout << ans[i];
}

return 0;
}
```



9. ① Every item has priority associated with it.
- ② An element with high priority is dequeued before an element with low priority.
- ③ In two elements have same priority, they are served according to their order in the queue.

Application: Dijkstra's Shortest path Algorithm using priority queue. When the graph is stored in the form of adjlist or matrix, priority queue can be used to extract minimum efficiently when implementing Dijkstra's algorithm.

Prims Algorithms used priority queue.

### 10. Min-heap

In a min-heap the key present at the root node must be less than or equal to among the keys present at all of its children.

In a min-heap, the minimum key element present at the root

### Max-heap

In a max-heap, the key present at the root node must be greater than or equal to among the keys at present at all of its children.

In a max-heap, the maximum key element present at root.



3. A min-heap uses the ascending priority.

4. In the construction of a Min-heap, the smallest element has priority.

5. In a Min-heap, the smallest element is the first to be popped from the heap.

A max heap uses the descending priority.

In the construction of a Max-heap, the greatest element has priority.

In a Max-heap, the greatest element is the first to be popped from the heap.