

MAT 3005 Applied Numerical Methods

Digital Assignment

Answer all the questions

Instructions: Write the solution in your note book and get signature from the faculty. After verification, upload the pdf copy in VTOP.

1. Find $f(x)$ as a polynomial in x for the following data by Newton's divided difference formula

x	-4	-1	0	2	5
$f(x)$	1245	33	5	9	1335

2. Using Lagrange interpolation, find the unique polynomial $P(x)$ of degree 2 or less such that $P(1) = 1$, $P(3) = 27$, $P(4) = 64$.
3. Using Newton's divided difference method, find $f(1.5)$ using the data $f(1.0) = 0.7651977$, $f(1.3) = 0.6200860$, $f(1.6) = 0.4554022$, $f(1.9) = 0.2818186$, and $f(2.2) = 0.1103623$.
4. Obtain the cubic spline approximation valid in the interval $[1, 2]$, for the function given in the tabular form, under the natural cubic spline conditions $f''(0) = M(0) = 0$, and $f''(3) = M(3) = 0$. Hence, interpolate at $x = 1.5$.

x	0	1	2	3
$f(x)$	1	4	10	8

5. Evaluate $\int_0^2 e^x dx$ using the Simpson's rules with $h = 1$ and $h = 1/2$. Compare with exact solution. Improve the result using Romberg integration.
6. Evaluate $\int_0^6 \frac{dx}{1+x^2}$ (i) trapezoidal rule, (ii) Simpson's rule. Also, check the result by actual integration.
7. Evaluate the integral $I = \int_1^2 \frac{2x}{1+x^4} dx$ using Gauss two point and three point rules. Compare with the exact solution $I = \tan^{-1}(4) - (\pi/4)$.
8. Given $y' = x^3 + y$, $y(0) = 2$, compute $y(0.2)$, $y(0.4)$ and $y(0.6)$ using the Runge-Kutta method of fourth order.

9. Obtain the solution by the fourth order Runge-Kutta method $y'' + y' + y = 0$, $y(0) = 1$, $y'(0) = 0$, find the value of $y(0.1)$.

10. Using the Adams-Bashforth predictor-corrector equations, evaluate $y(1.4)$, if y satisfies

$$\frac{dy}{dx} + \frac{y}{x} = \frac{1}{x^2} \text{ and } y(1) = 1, y(1.1) = 0.996, y(1.2) = 0.986, y(1.3) = 0.972.$$