2D Taylor series

Practice Quiz, 5 questions

5/5 points (100%)



✓ Congratulations! You passed!

Next Item

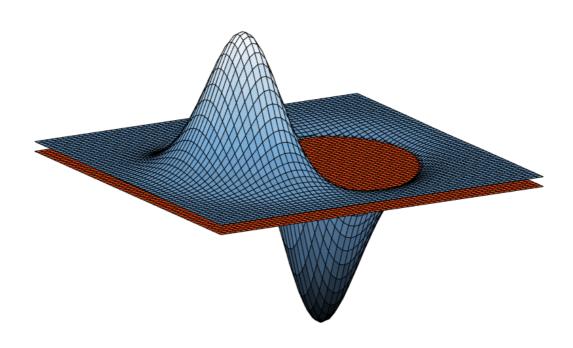


1/1 point

Now you have seen how to calculate the multivariate Taylor series, and what zeroth, first and second order 2D Taylor at the for a function of 2 variables. In this course we won't be considering anything practide global stress or order for functions of more than one variable.

In the following questions you will practise recognising these approximations by thinking about how they behave with different x and y, then you will calculate some terms in the multivariate Taylor series yourself.

The following plot features a surface and its Taylor series approximation in red, around a point given by a red circle. What order is the Taylor series approximation?



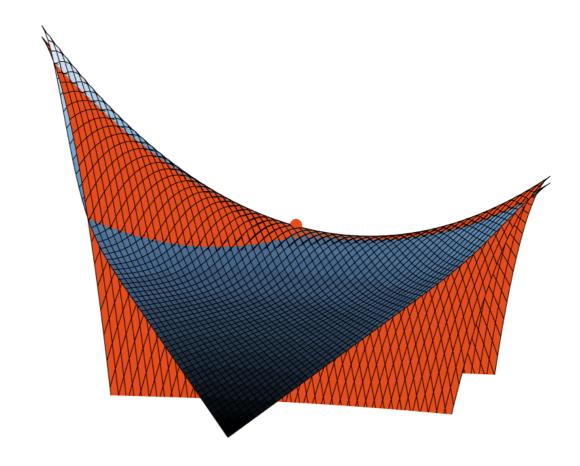
0	Zeroth order	
Correct		
The red surface is constant everywhere and so has no terms in ${f \Delta x}$ or ${f \Delta x}^2$		
\bigcirc	First order	
	Second order	
	None of the above	
	Notic of the above	



5/5 points (100%)

2.

What order Taylor series approximation, expanded around the red circle, is the red surface in the following plot?

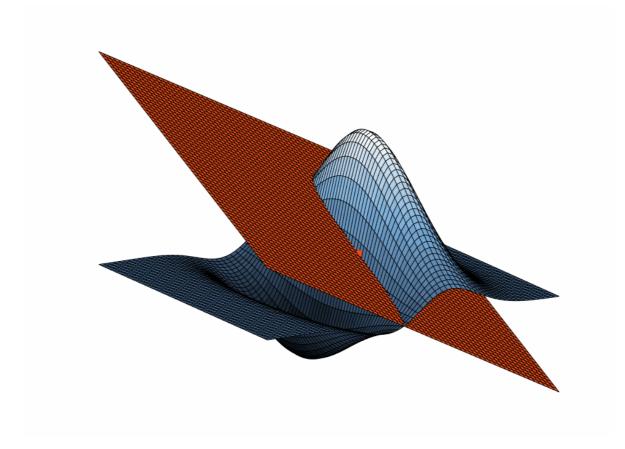


\bigcirc	Zeroth order
	First order
0	Second order
Correct The gradient of the surface is not constant, so we must have a term of higher order than Δx .	
	None of the above



1/1 point 2D TanylordSOrficsin the following images is a first order Taylor series approximation of the blug surface? (100%)
PracticeRevisrigingstions are given, but you don't need to do any calculations.

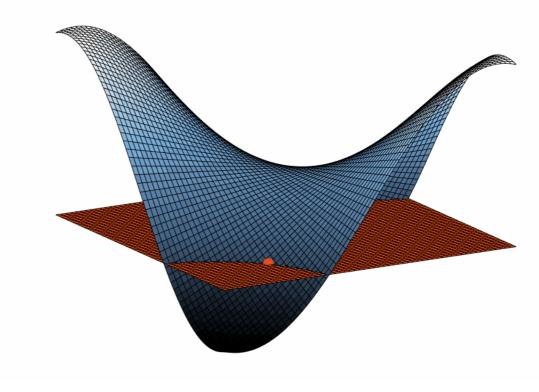
$$\int f(x,y) = (x^2+2x)e^{-x^2-y^2/5}$$



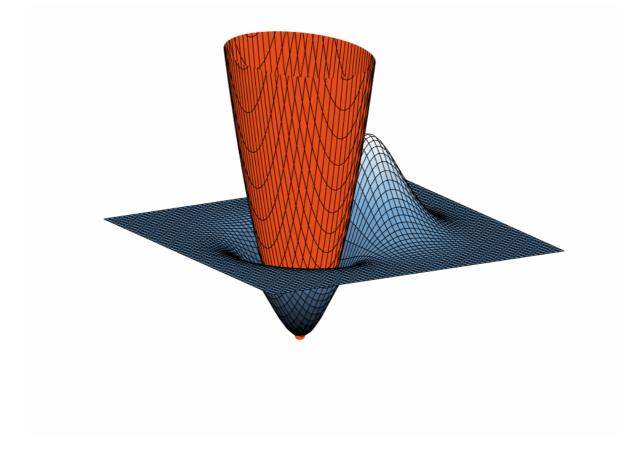
$$\int f(x,y) = \sin(xy/5)$$

2D Taylor series Practice Quiz, 5 questions

5/5 points (100%)



$$\int f(x,y) = xe^{-x^2-y^2}$$

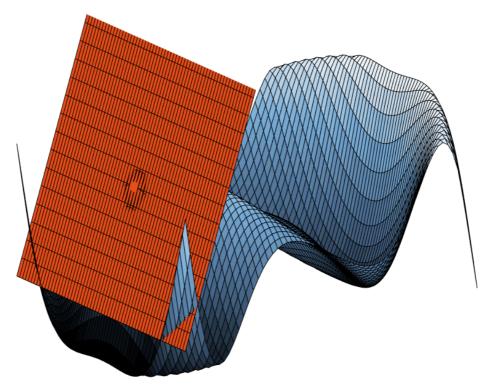


 $f(x,y)=x\sin(x^2/2+y^2/4)$

2D Taylor series

5/5 points (100%)

Practice Quiz, 5 questions



Correct

The gradient of the red surface is non-zero and constant, so the Δx terms are the highest order.



1/1 point

4

Recall that up to second order the multivariate Taylor series is given by $f(\mathbf{x} + \Delta \mathbf{x}) = f(\mathbf{x}) + J_f \Delta \mathbf{x} + \frac{1}{2} \Delta \mathbf{x}^T H_f \Delta \mathbf{x} + \dots$

Consider the function of 2 variables, $f(x,y)=xy^2e^{-x^4-y^2/2}$. Which of the following is the first order Taylor series expansion of f around the point (-1,2)?

$$f_1(-1+\Delta x,2+\Delta y)=-4e^{-3}+16e^{-3}\Delta x-8e^{-3}\Delta y$$

$$\int f_1(-1+\Delta x,2+\Delta y) = -4e^{-3}-4e^{-3}\Delta x + 4e^{-3}\Delta y$$

$$\int \int f_1(-1+\Delta x,2+\Delta y)=2e^{-33/2}-63e^{-33/2}\Delta x-2e^{-33/2}\Delta y$$

$$\int \int f_1(-1+\Delta x,2+\Delta y) = -4e^{-3}-12e^{-3}\Delta x + 4e^{-3}\Delta y$$

2D Taylor series

Practice Quiz, 5 questions

5/5 points (100%)



1/1 point

5

Now consider the function $f(x,y) = \sin(\pi x - x^2 y)$. What is the Hessian matrix H_f that is associated with the second order term in the Taylor expansion of f around $(1,\pi)$?

- $H_f = \begin{pmatrix} -2\pi & -2 \\ -2 & 1 \end{pmatrix}$
- $H_f = \begin{pmatrix} -\pi^2 & \pi \\ \pi & -1 \end{pmatrix}$
- $H_f = \begin{pmatrix} -2 & -2\pi \\ 2\pi & 1 \end{pmatrix}$
- $\begin{array}{ccc}
 & H_f = \begin{pmatrix}
 -2\pi & -2 \\
 -2 & 0
 \end{pmatrix}$



Correct

Good, you can check your second order derivatives here:

$$\partial_{xx} f(x, y) = -2y \cos(\pi x - x^2 y) - (\pi - 2xy)^2 \sin(\pi x - x^2 y)$$

$$\partial_{xy} f(x, y) = -2x \cos(\pi x - x^2 y) - x^2 (\pi - 2xy) \sin(\pi x - x^2 y)$$

$$\partial_{yx} f(x, y) = -2x \cos(\pi x - x^2 y) - x^2 (\pi - 2xy) \sin(\pi x - x^2 y)$$

$$\partial_{yy}f(x,y) = -x^4\sin(\pi x - x^2y)$$



