

5/5 points (100%)

✓ Congratulations! You passed!

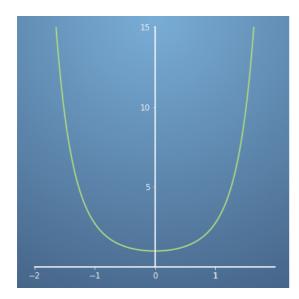
Next Item



1/1 point

1

In the two previous videos, we have shown the short mathematical proofs for the Taylor series, and for special cases when the starting point is x=0, the Maclaurin series. In these set of questions, we will begin to work on applying the Taylor and Maclaurin series formula to obtain approximations of functions.



For the function $f(x) = e^{x^2}$ about x = 0, using the the Maclaurin series formula, obtain an approximation up to the first three non zero terms.

$$f(x) = 1 + x^2 + \frac{x^4}{2} + \dots$$

Correct

We find that only even powers of x appear in the Taylor approximation for this function.

$$\int f(x)=1-x^2-rac{x^4}{2\cdot \cdot \cdot \cdot}$$



1 / 1 point

2

18/04/2019

Applying the Taylor series

Practice Quiz, 5 questions

5/5 points (100%)

Use the Taylor series formula to approximate the first three terms of the function f(x)=1/x, expanded around the point p=4.

- $f(x) = \frac{(x-4)}{16} + \frac{(x-4)^2}{64} \frac{(x-4)^3}{256} \cdots$
- $f(x) = -rac{1}{4} rac{(x+4)}{16} rac{(x+4)^2}{64} \cdots$

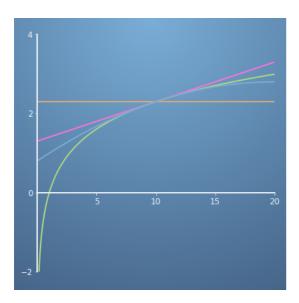
Correct

We find that only even powers of x appear in the Taylor approximation for this function.



1/1 point

3.



By finding the first three terms of the Taylor series shown above for the function $f(x) = \ln(x)$ (green line) about x = 10, determine the difference of using the second order taylor expansion against the first order Taylor expansion when approximating to find the value of f(2).

 $\Delta f(2)=1.0$

 $\Delta f(2) = 0.32$

Correct Applying the Taylor series

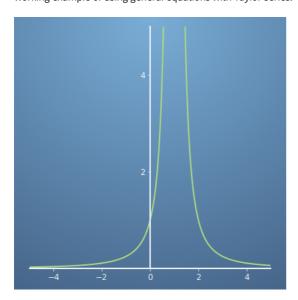
The second orideric Eaylor, appeaxination about the point x=10 is $f(x) = ln(10) + \frac{(x-10)}{10} \frac{(x-10)^2}{200} \dots$, substituting in x=2 gives us $\Delta f(2) = 0.32$

- $\Delta f(2) = 0.5$
- $\Delta f(2) = 0$



1/1 point

In some cases, a Taylor series can be expressed in a general equation that allows us to find a particular n^{th} term of our series. For example the function $f(x)=e^x$ has the general equation $f(x)=\sum_{n=0}^\infty \frac{x^n}{n!}$. Therefore if we want to find the 3^{rd} term in our Taylor series, substituting n=2 into the general equation gives us the term $\frac{x^2}{2}$. We know the Taylor series of the function e^x is $f(x)=1+x+\frac{x^2}{2}+\frac{x^3}{3}+\ldots$. Now let us try a further working example of using general equations with Taylor series.



By evaluating the function $f(x)=rac{1}{(1-x)^2}$ about the origin x=0, determine which general equation for the n^{th} order term correctly represents f(x)

- $\int f(x) = \sum_{n=0}^{\infty} (2+n)(x)^n$
- $\int f(x) = \sum_{n=0}^{\infty} (1+n)x^n$

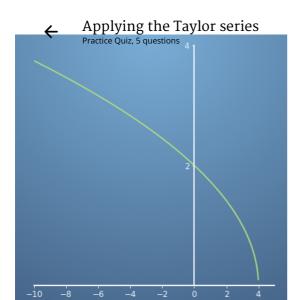
Correct

By doing a Maclaurin series approximation, we obtain $f(x)=1+2x+3x^2+4x^3+5x^4+\ldots$, which satisfies the general equation shown.

 $f(x) = \sum_{n=0}^{\infty} (1+2n)(x)^n$



point



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By evaluating the function $f(x)=\sqrt{4-x}$ at x=0 , find the quadratic equation that approximates this function.

- $\bigcirc \quad f(x) = 2 + x + x^2 \dots$

Correct

The quadratic equation shown is the second order approximation.

