

ME634A End-Sem assignment - Part I:
Two-dimensional stretching of a circle in a shear velocity field
using CLSVOF method

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Problem Description

- Periodic boundary condition in z direction.
- 3D laminar problem.
- Solved for a uniform grid (though the code is well-equipped to solve for a non-uniform grid as well).
- Equations to be solved:

$$\phi_t + \mathbf{u} \cdot \nabla \phi = 0$$

$$F_t + \mathbf{u} \cdot \nabla F = 0$$

- Shearing velocity field (Dirichlet B.C. in x-y):

$$u = -(\sin \pi x)^2 \sin(2\pi y) \cos(\pi t/T)$$

$$v = (\sin \pi y)^2 \sin(2\pi x) \cos(\pi t/T)$$

$$w = 0$$

where $T = 8$.

- Neumann B.C. for Level Set function (ϕ) and Volume of Fluid function (F) in x-y directions.
- Interface thickness: $\epsilon = 1.75 * (\text{grid size})$
- Domain: $[0,1] \times [0,1] \times [0,0.5]$
- Circle radius = 0.15; circle-center = (0.5,0.75,0.25)

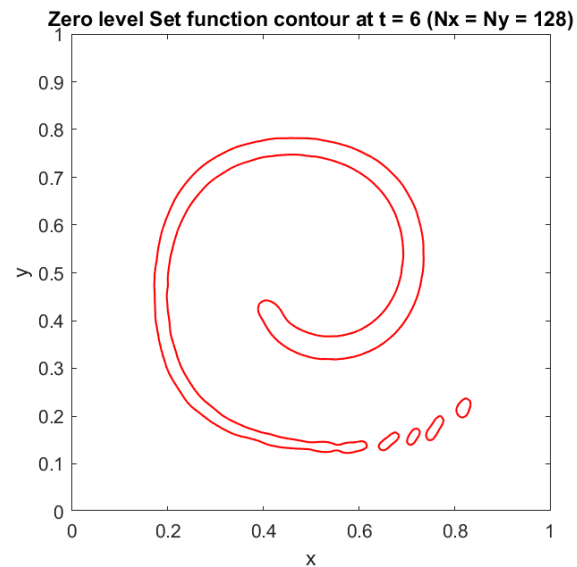
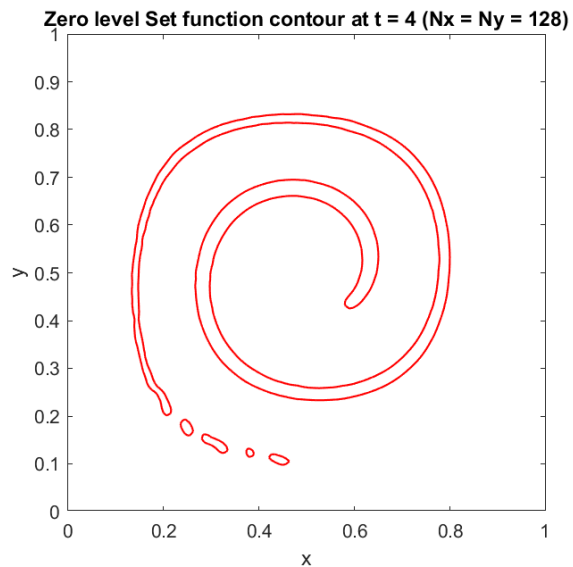
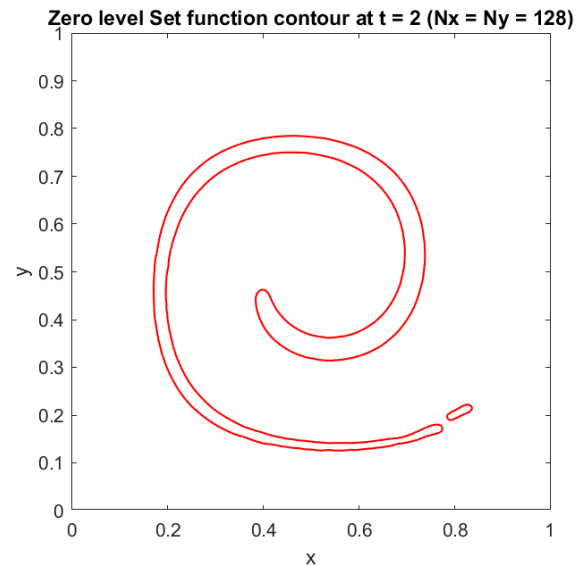
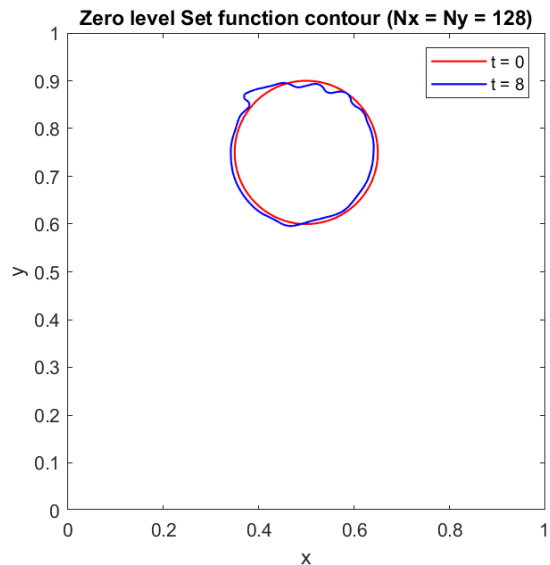
2D code results

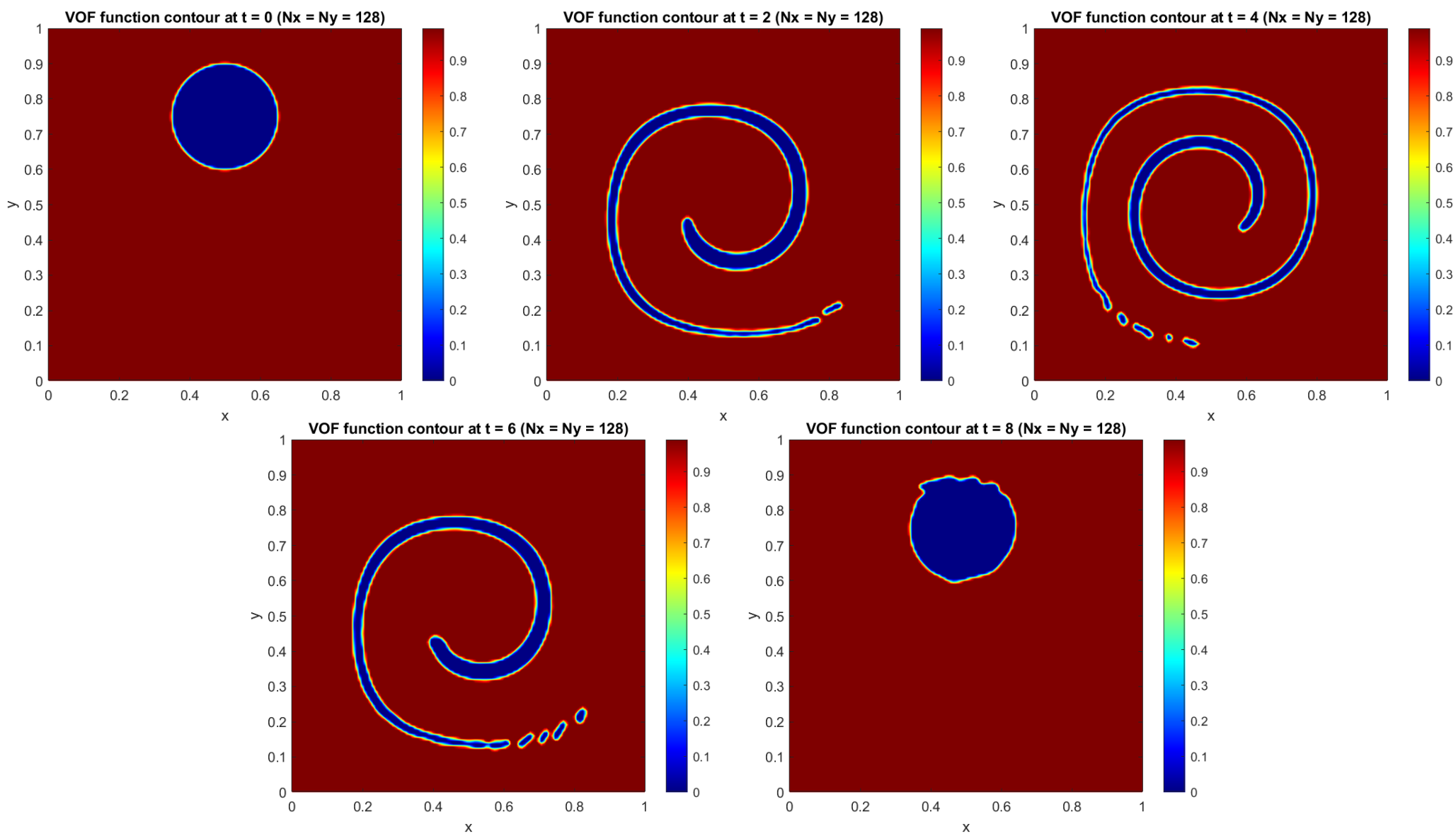
No. of Cells:

$$N_x = 128$$

$$N_y = 128$$

CFL no. = 0.25



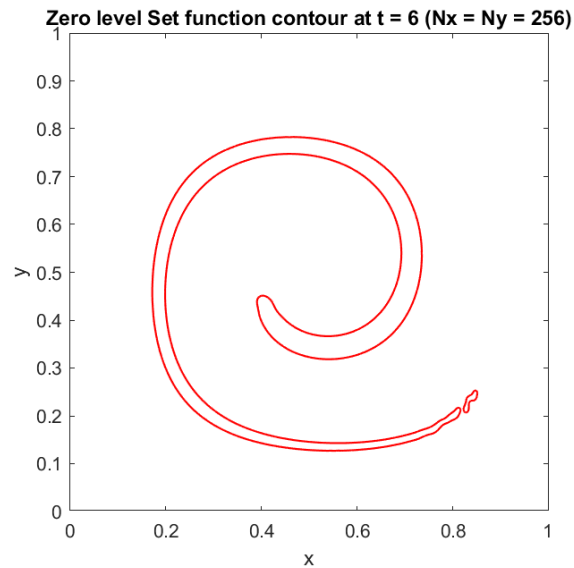
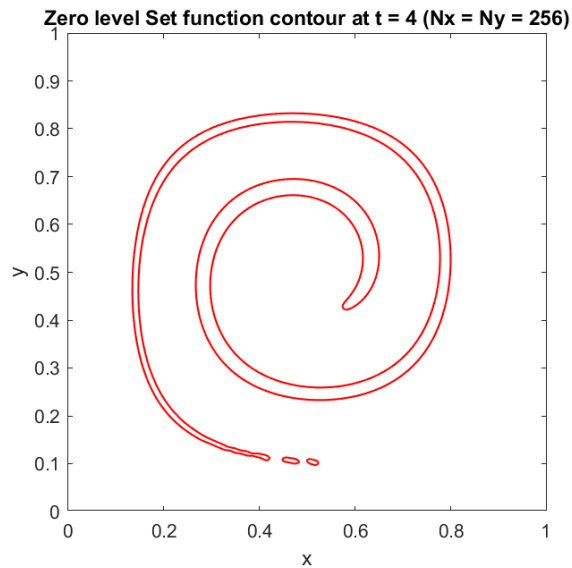
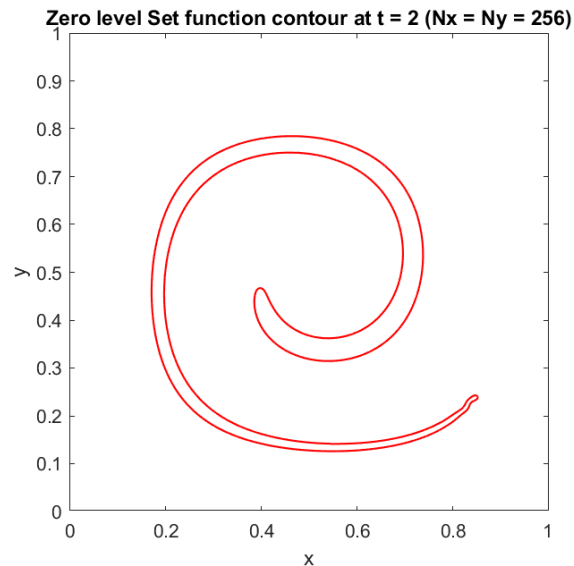
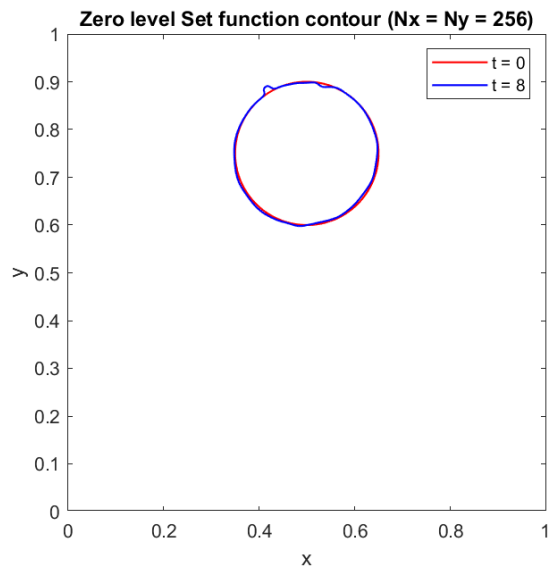


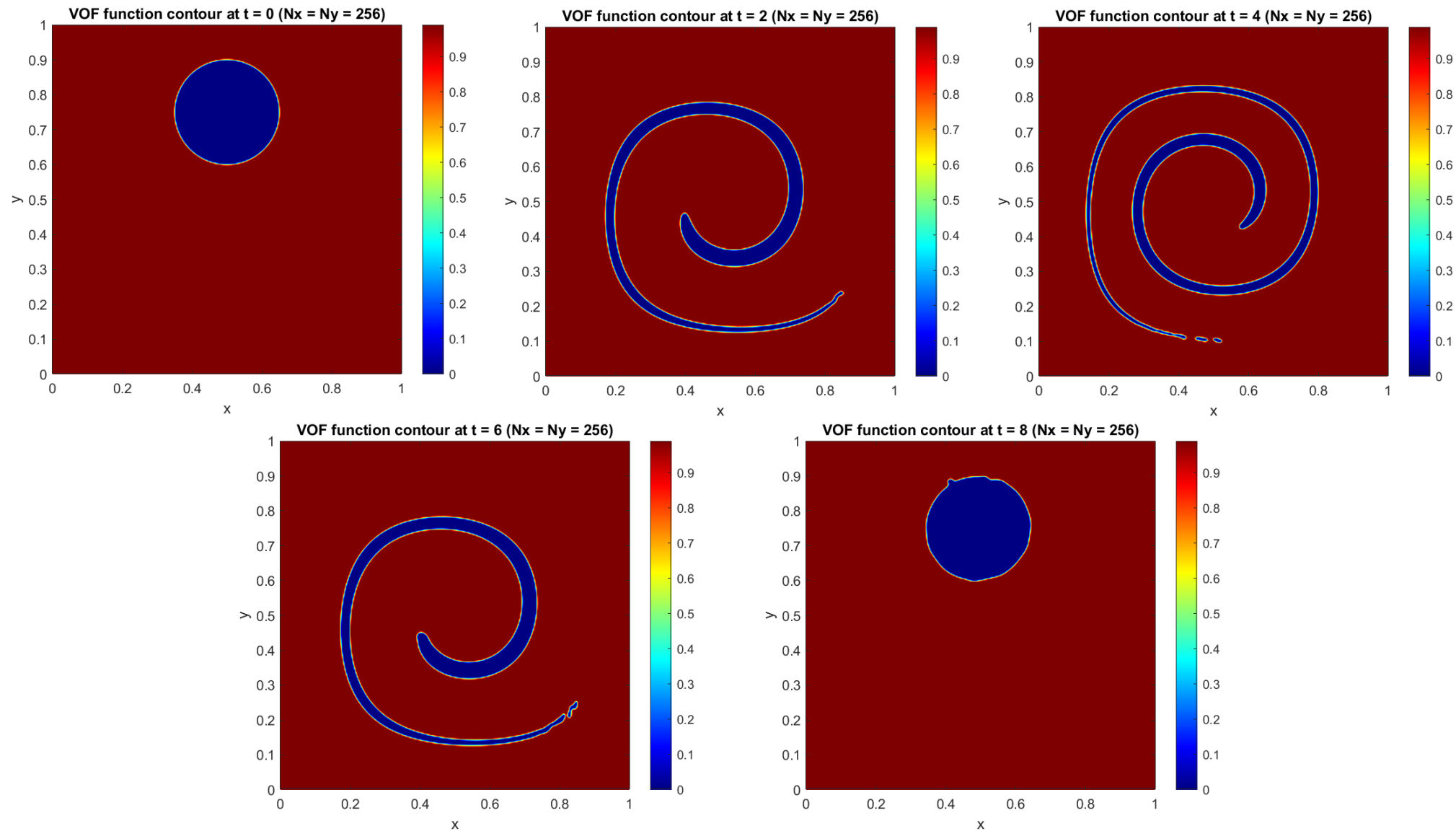
No. of Cells:

$$N_x = 256$$

$$N_y = 256$$

CFL no. = 0.25





3D code results (at mid-z plane)

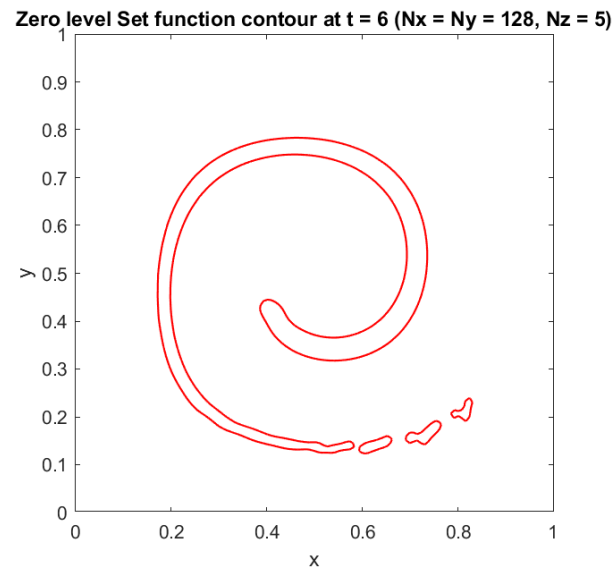
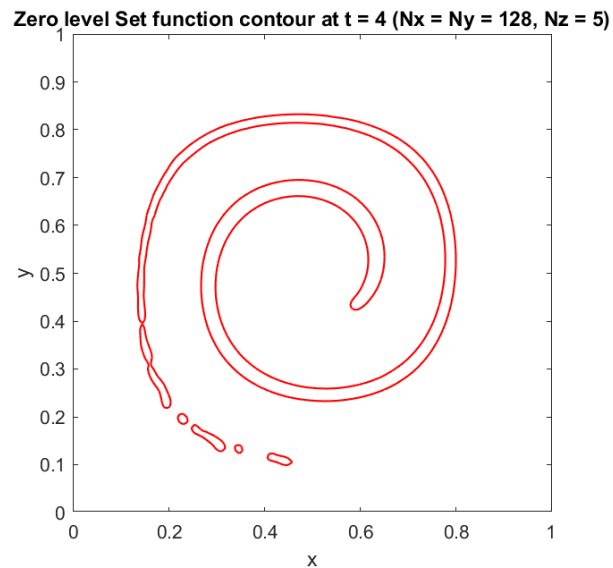
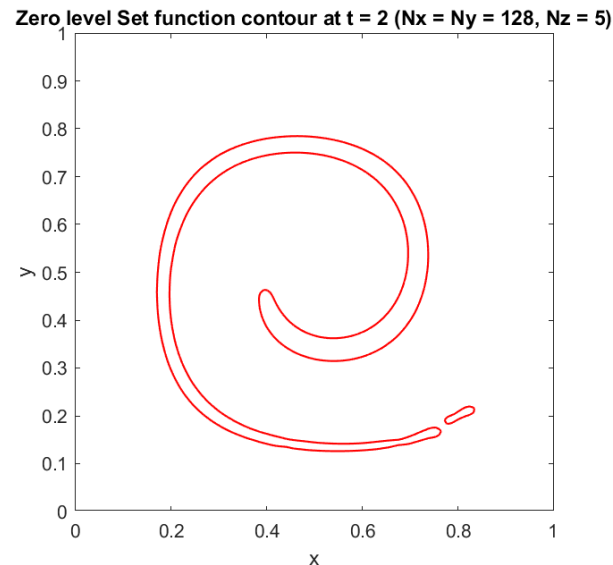
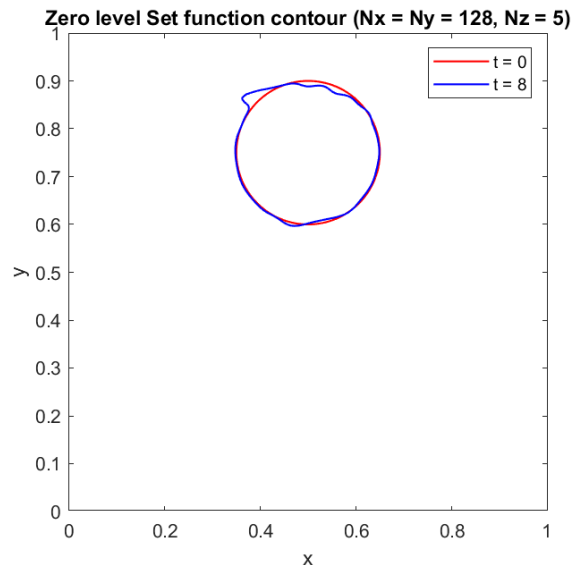
No. of Cells:

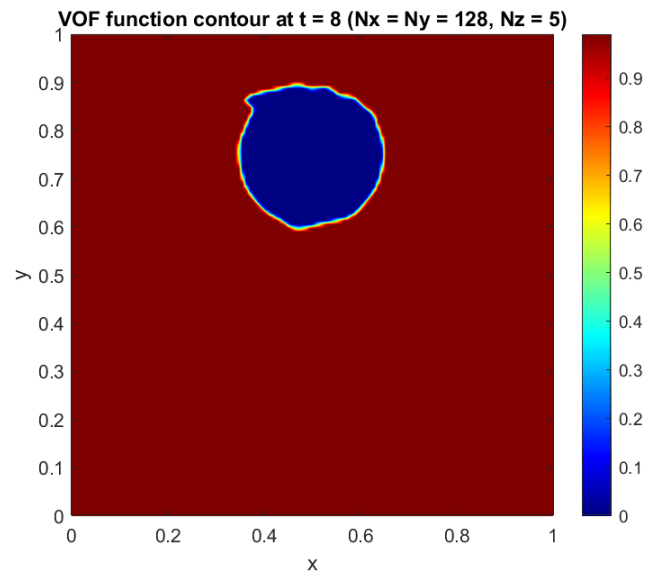
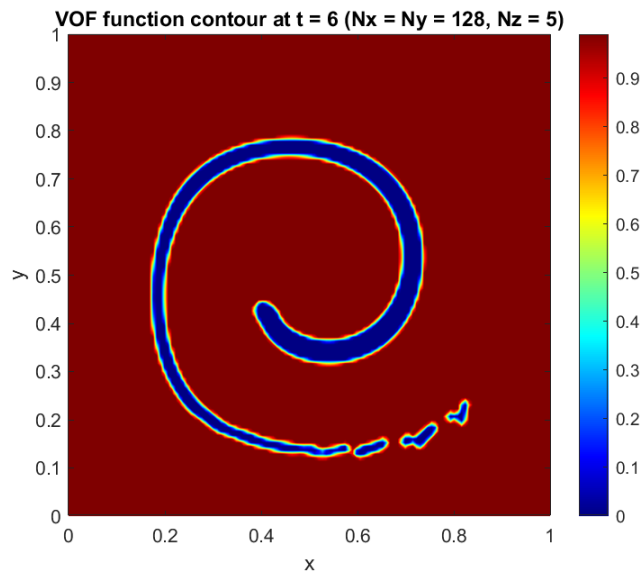
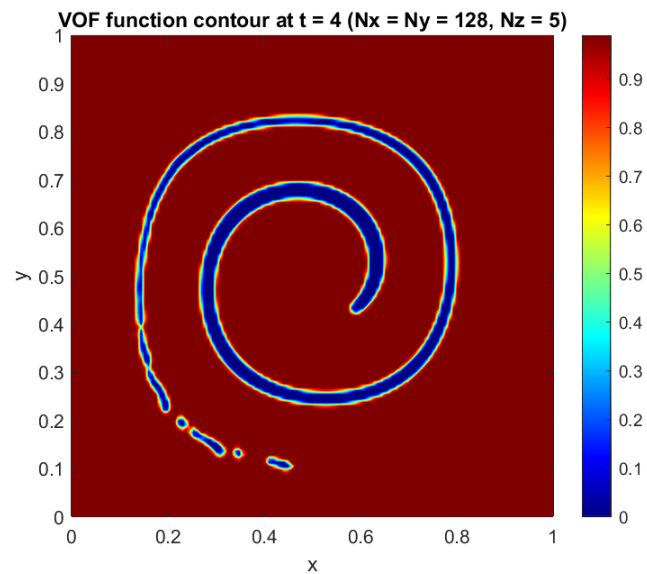
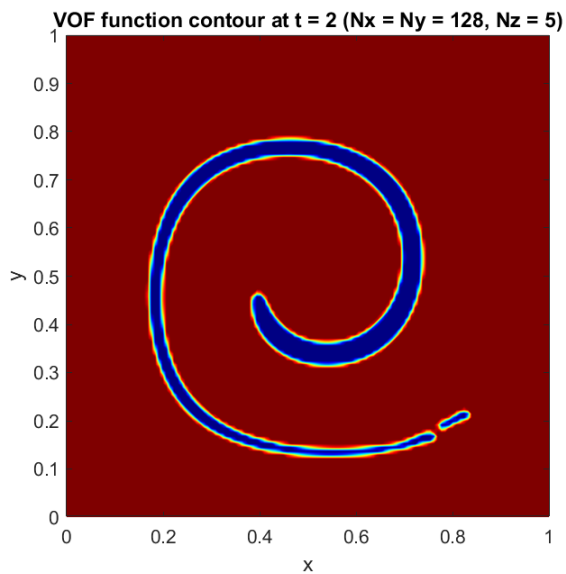
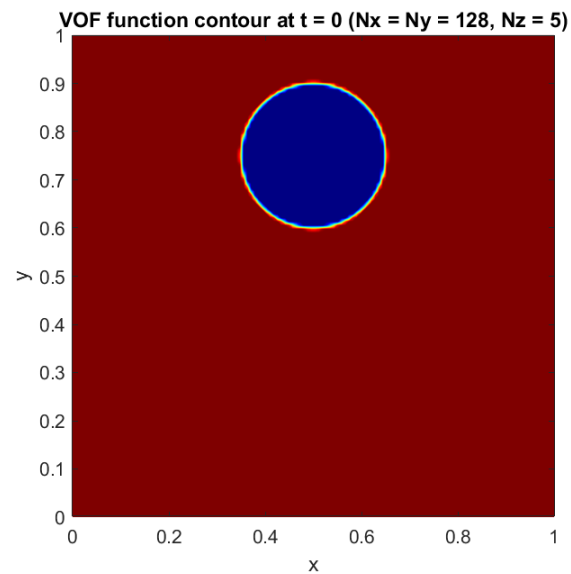
$$N_x = 128$$

$$N_y = 128$$

$$N_z = 5$$

CFL no. = 0.05





ME634A End-Sem assignment – Part II :
Three-dimensional deformation of a sphere in a shear velocity field
using CLSVOF method

Problem Description

- 3D laminar problem.
- Solved for a uniform grid (though the code is well-equipped to solve for a non-uniform grid as well).
- Equations to be solved:

$$\phi_t + \mathbf{u} \cdot \nabla \phi = 0$$

$$F_t + \mathbf{u} \cdot \nabla F = 0$$

- Shearing velocity field (Dirichlet B.C. in x-y-z):

$$u = 2(\sin \pi x)^2 \sin(2\pi y) \sin(2\pi z) \cos(\pi t/T)$$

$$v = -(\sin \pi y)^2 \sin(2\pi x) \sin(2\pi z) \cos(\pi t/T)$$

$$w = -(\sin \pi z)^2 \sin(2\pi x) \sin(2\pi y) \cos(\pi t/T)$$

where $T = 3$.

- Neumann B.C. for Level Set function (ϕ) and Volume of Fluid function (F) in x-y-z directions.
- Interface thickness: $\epsilon = 1.75 * (\text{grid size})$
- Domain: $[0,1] \times [0,1] \times [0,1]$
- Circle radius = 0.15; circle-center = (0.35,0.35,0.35)

No. of Cells:

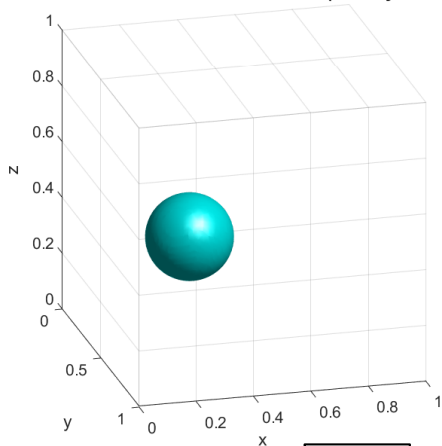
$$N_x = 64$$

$$N_y = 64$$

$$N_z = 64$$

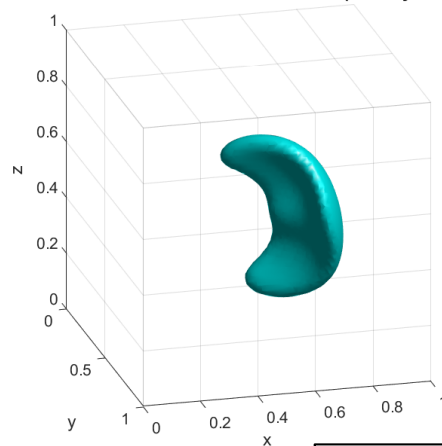
CFL no. = 0.25

Zero level Set function contour at $t = 0$ ($N_x = N_y = N_z = 64$)



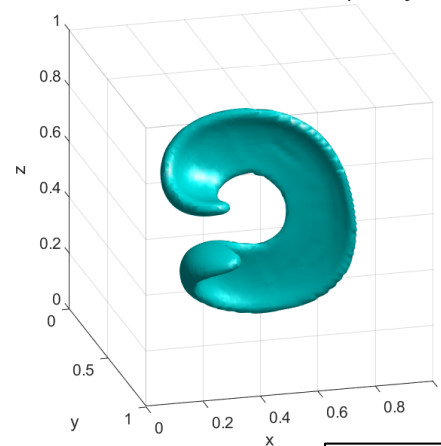
$t = 0$

Zero level Set function contour at $t = 0.48$ ($N_x = N_y = N_z = 64$)



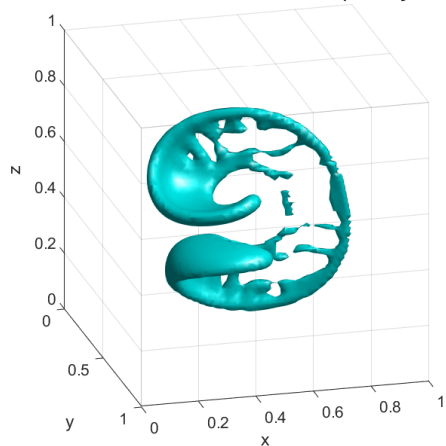
$t = 0.48$

Zero level Set function contour at $t = 0.98$ ($N_x = N_y = N_z = 64$)



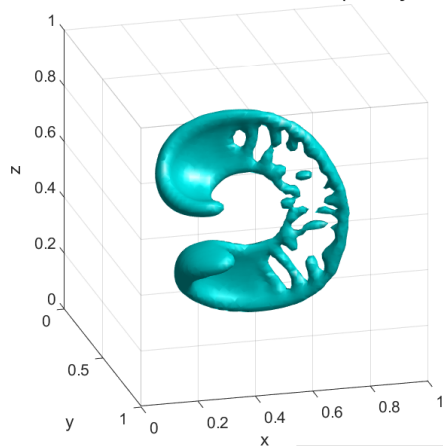
$t = 0.98$

Zero level Set function contour at $t = 1.49$ ($N_x = N_y = N_z = 64$)



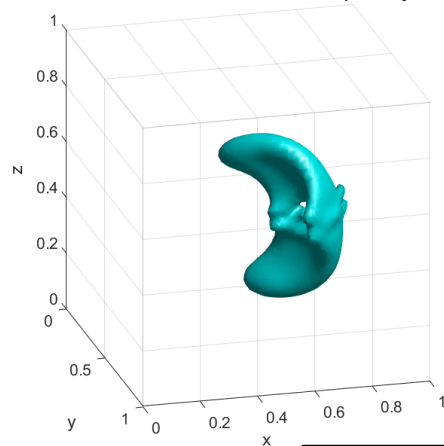
$t = 1.49$

Zero level Set function contour at $t = 1.98$ ($N_x = N_y = N_z = 64$)



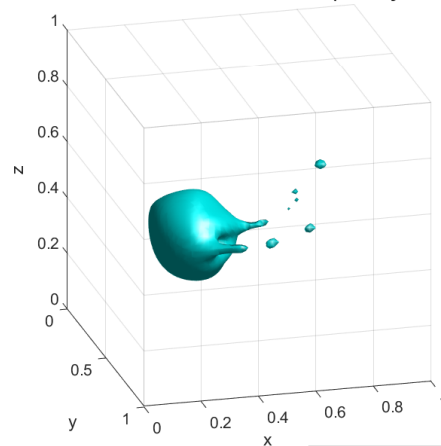
$t = 1.98$

Zero level Set function contour at $t = 2.48$ ($N_x = N_y = N_z = 64$)



$t = 2.48$

Zero level Set function contour at $t = 3$ ($N_x = N_y = N_z = 64$)



$t = 3 = T$

No. of Cells:

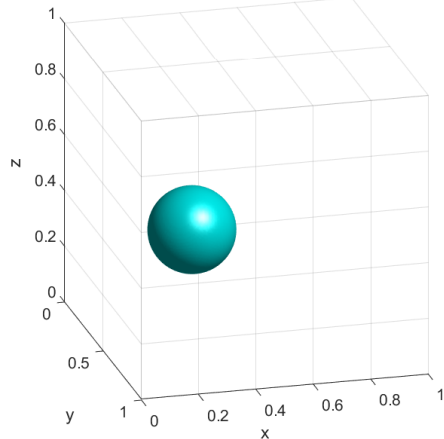
$$N_x = 128$$

$$N_y = 128$$

$$N_z = 128$$

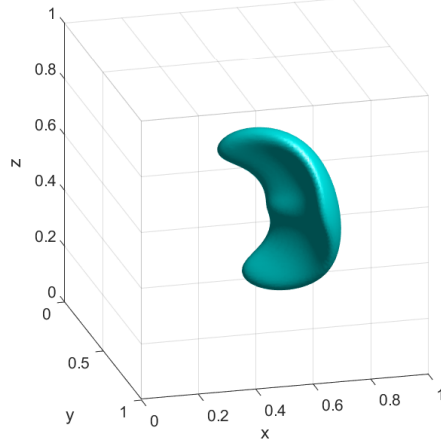
CFL no. = 0.25

Zero level Set function contour at $t = 0$ ($N_x = N_y = N_z = 128$)



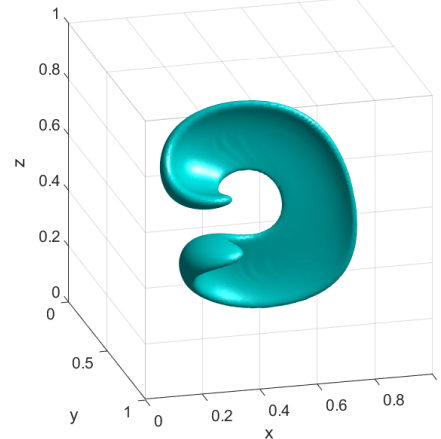
$t = 0$

Zero level Set function contour at $t = 0.48$ ($N_x = N_y = N_z = 128$)



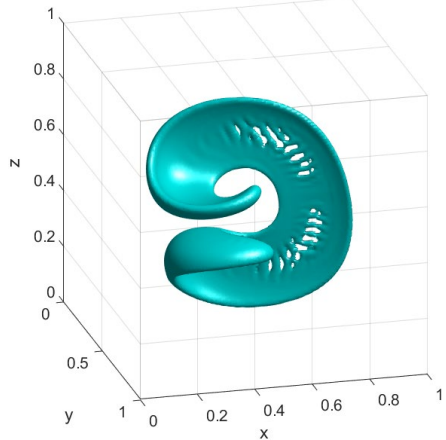
$t = 0.48$

Zero level Set function contour at $t = 0.98$ ($N_x = N_y = N_z = 128$)



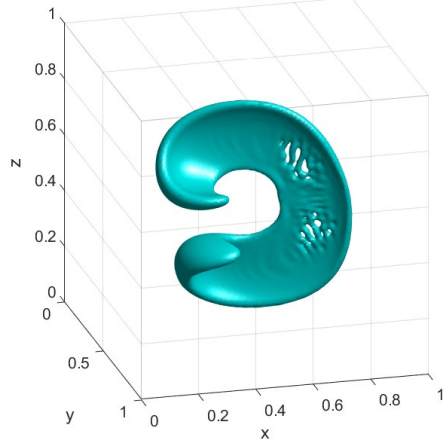
$t = 0.98$

Zero level Set function contour at $t = 1.49$ ($N_x = N_y = N_z = 128$)



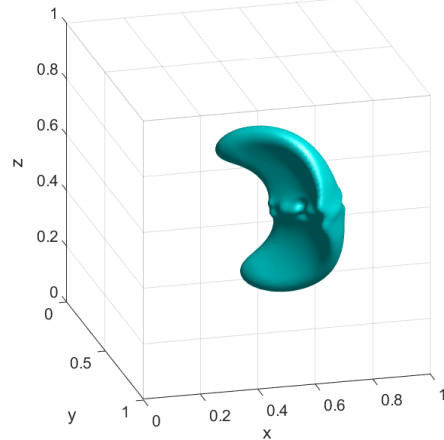
$t = 1.49$

Zero level Set function contour at $t = 1.98$ ($N_x = N_y = N_z = 128$)



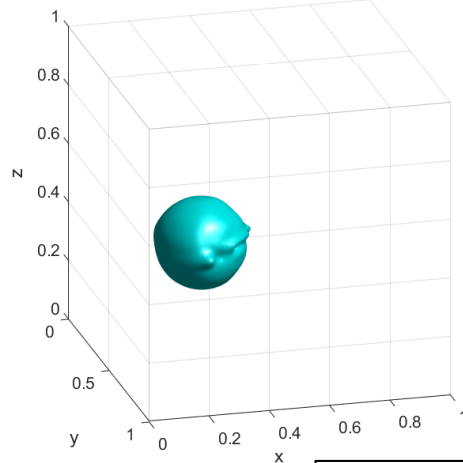
$t = 1.98$

Zero level Set function contour at $t = 2.48$ ($N_x = N_y = N_z = 128$)



$t = 2.48$

Zero level Set function contour at $t = 3$ ($N_x = N_y = N_z = 128$)



$t = 3 = T$