## Probability Assignment

## GINNA SHREYANI

## 12.13.1.5

If  $\Pr(A) = \frac{6}{11}$ ,  $\Pr(B) = \frac{5}{11}$  and  $\Pr(A+B) = \frac{7}{11}$ , find

- 1. Pr(AB)
- 2.  $Pr(A \mid B)$
- 3.  $Pr(B \mid A)$

## Solution

1. We know that,

$$Pr(AB) = Pr(A) + Pr(B) - Pr(A+B)$$
 (1)

From (1), we get

$$\Pr(AB) = \frac{6}{11} + \frac{5}{11} - \frac{7}{11} \tag{2}$$

$$\Pr\left(AB\right) = \frac{4}{11} \tag{3}$$

2. We know that,

$$\Pr(A \mid B) = \frac{\Pr(AB)}{\Pr(B)} \tag{4}$$

From (4), we get

$$\Pr(A \mid B) = \frac{\frac{4}{11}}{\frac{5}{11}} \tag{5}$$

$$\Pr\left(A \mid B\right) = \frac{4}{5} \tag{6}$$

3. We know that,

$$\Pr(B \mid A) = \frac{\Pr(BA)}{\Pr(A)} \tag{7}$$

From (7), we get

$$\Pr(B \mid A) = \frac{\frac{4}{11}}{\frac{6}{11}}$$

$$\Pr(B \mid A) = \frac{4}{6}$$

$$\Pr(B \mid A) = \frac{2}{3}$$
(9)

$$\Pr\left(B \mid A\right) = \frac{4}{6} \tag{9}$$

$$\Pr\left(B \mid A\right) = \frac{2}{2} \tag{10}$$

As a result,

$$\Pr\left(AB\right) = \frac{4}{11} \tag{11}$$

$$\Pr\left(A \mid B\right) = \frac{4}{5} \tag{12}$$

$$\Pr(A \mid B) = \frac{4}{5}$$
 (12)  
 $\Pr(B \mid A) = \frac{2}{3}$  (13)