

## # Resource allocation graph (RAG)

helps predict deadlock is present in system or not

It has nodes, vertices, edges

process (P)

resource (R)

request

assignment

$R \rightarrow P$   
edge

assignment edge

$P \rightarrow R$  process requesting resource  
request edge

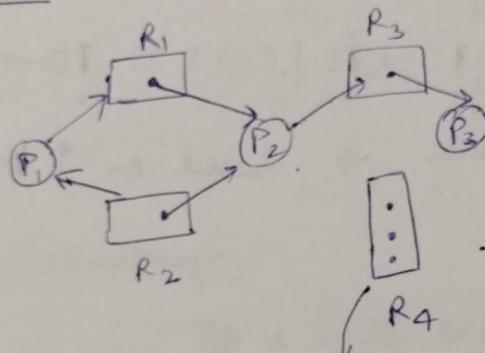
resources assigned  
to process

O process node

□ resource node

e.g. of RAG

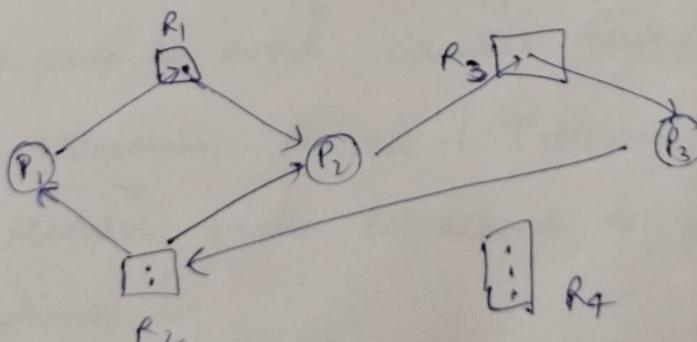
①



(no deadlock occurring)  
→ no cycle, no deadlock

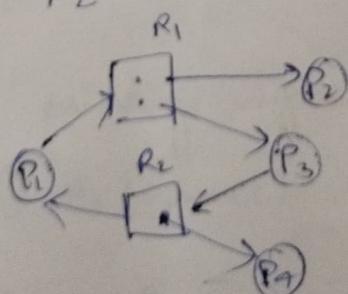
multiple instance of resource

②



cycle occurred  
∴ deadlock

③



→ no deadlock  
cycle detected

If there is a deadlock then there is cycle, if no cycle then no deadlock. If there is cycle, then there may be or may not be a deadlock.

$$D \rightarrow C \approx !C \not\rightarrow !D$$

\* Cycle is necessary for deadlock but not sufficient.

Note: If all R are of single instance then presence of cycle is necessary & sufficient condition for deadlock.

$$[D \geq C \quad | \quad D \rightarrow C] \approx !C \rightarrow !D \quad | \quad C \rightarrow D \approx !D \rightarrow !C]$$

for single instance  $\rightarrow$  based on ↑ order of resources invested.

## → Resource Allocation Graph for deadlock avoidance

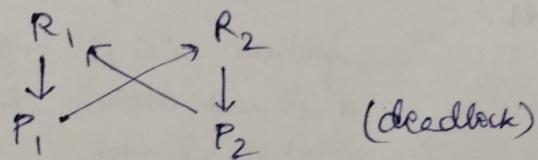
A RAG is a visual representation of how processes request and hold resources in a system. It helps in detecting and preventing deadlocks, where process gets stuck waiting for resources indefinitely.

Example -

Consider 2 processes  $P_1$  &  $P_2$  and 2 resources  $R_1$  &  $R_2$ :

①  $P_1$  holds  $R_1$  & request  $R_2$

$P_2$  holds  $R_2$  & request  $R_1$



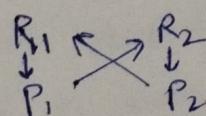
To prevent deadlock -

- ① Detect cycles - If a cycle exists, deadlock is possible.
- ② Use Resource Ordering - Assign a fixed order to resource requests to avoid circular wait.
- ③ Enforce Maximum Request - Processes declare their maximum resource needs beforehand to prevent deadlock-prone situations

Eg: Consider a printing system example:

$R_1$  (printer)  $R_2$  (scanner)  $P_1$  &  $P_2$

Deadlock :



## Deadlock avoidance:

Cycle detection - The system detects a cycle in RAG & prevents the second request.

Resource ordering - This rule could be 'always request scanner before printer to avoid circular waiting.'

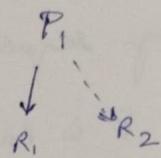
Maximum Request Allocation - Processes must declare in advance which resource they will use together.

## → Mechanism for Handling Deadlocks

① Deadlock Prevention: i) Dissatisfying mutual exclusion  
i.e. sharing resources, Some resources are inherently non-shareable & so it might be impossible to disatisfy M.E.

ii) Dissatisfy no preemption → snatch resources

$P_1$  is holding  $R_1$  & waiting for  $R_2$ .



$R_2$  is free.  $R_2$  is not  
& can be given available & can't  
to  $P_1$ . be given

$P_2$  is running,  
then  $P_1$  must wait  
for  $R_2$   $P_2$  is in waiting  
state then  $R_2$  is  
taken  
& given to  $P_1$

iii) Dissatisfy hold & wait

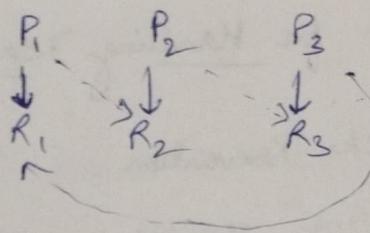
dissatisfy hold  
here, we release  
all held resources.

— Dissatisfy wait → not possible or  
efficient, but ek bounded  
wait hage sake, iske bad Reso-  
urce ho honge.

In one case, dissatisfy wait & in another case, we disatisfy hold. In disatisfy wait, process is allowed to start the execution only if it has been allocated the resources which ideally is not implemented as it isn't possible to know as we don't know how many R are needed by P beforehand. Also, it may result in low utilization of resources.

Dissatisfy hold - processes must release the held R before making any new R request. Next time, either it gets all the R after releasing or may not get many which may lead to starvation.

iv) Dissatisfy Circular Wait  $\rightarrow$



f: Resource set  $\rightarrow$  natural no.

e.g.: f(tape drives)  $\rightarrow$  2

f(hard disks)  $\rightarrow$  4

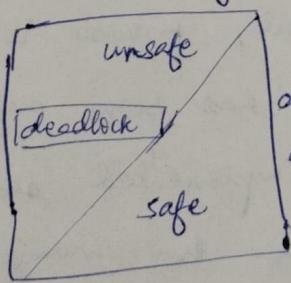
only request resources if:  $f(R_2) < f(R_1)$

If  $P$  is having  $R_i$  & requesting for  $R_j$ ,  $R_j$  will only be given when  $f(R_i) < f(R_j)$ , which means the  $R$  must be given to the processes in ↑ order. of enumeration.  
will dissatisfy circular wait.

### ② Deadlock Avoidance:

Safe state: A state is safe only if there exists a safe sequence. A sequence of processes  $\langle P_1, P_2 \dots P_n \rangle$  is a safe seq. for the current allocation state if for each  $P_i$ , the resource request that  $P_i$  can still make can be satisfied by the currently available resources, + resources held by all  $P_j$  where  $(j < i)$

If no such seq. exists, the system state is said to be unsafe state.



A safe state is not a deadlock state. Conversely, a deadlock is an unsafe state but not all unsafe states are deadlock.

Assignment: Resource Allocatn graph for deadlock avoidance

Ques. 12 R available (tape drives)  $\rightarrow$  3P  $\rightarrow P_0 P_1 P_2$

max. R allocated to each is:	$P_0 \rightarrow$	$\frac{\text{max.}}{10}$	<u>allocated</u>	<u>Need</u>
	$P_1 \rightarrow$	4	5	5
	$P_2 \rightarrow$	9	2	2

$$12 - 9 = 3 \text{ available}$$

$$CA = 3 + 2 + 5 + 2 \Rightarrow 12.$$

Safe seq:  $\langle P_1, P_0, P_2 \rangle$  at to

$\rightarrow$  Banker's Algorithm

Safety Algorithm

Resource Request Algorithm

① Total matrix

It tells how many R are available & in what amount.

$$\text{Total} = [R_1 \ R_2 \ R_3 \ \dots \ R_m]_{1 \times m}$$

② Maximum Matrix

How many R are required by the processes in the system.

$$\begin{matrix} P_1 & R_1 & R_2 & R_3 & R_m \\ P_2 & & & & \\ P_3 & & & & \\ P_n & & & & \end{matrix} \quad n \times m$$

③ Allocation Matrix

How many R the processes have been allocated & of which type.

$$\begin{matrix} P_1 & R_1 & \dots & R_m \\ P_2 & & & \\ P_n & & & \end{matrix} \quad n \times m$$

④ Need Matrix

How many R are further needed by each process.

(need = max - allocation) matrix.

$$\begin{matrix} P_1 & R_1 & \dots & R_m \\ P_2 & & & \\ P_n & & & \end{matrix} \quad n \times m$$

Q: max matrix:

$$\begin{array}{l}
 \text{max matrix:} \\
 \begin{array}{c}
 P_0 \\
 P_1 \\
 P_2 \\
 P_3
 \end{array}
 \left[ \begin{array}{ccc}
 a & b & c \\
 8 & 5 & 4 \\
 3 & 4 & 2 \\
 1 & 0 & 4 \\
 3 & 2 & 5
 \end{array} \right]
 \end{array}
 \quad \text{total matrix:} \\
 \left[ \begin{array}{ccc}
 a & b & c \\
 7 & 9 & 10
 \end{array} \right]$$

allocation matrix:

$$\begin{array}{c}
 P_0 \\
 P_1 \\
 P_2 \\
 P_3
 \end{array}
 \left[ \begin{array}{ccc}
 a & b & c \\
 0 & 3 & 4 \\
 2 & 1 & 2 \\
 0 & 0 & 2 \\
 1 & 2 & 1
 \end{array} \right]
 \Rightarrow \begin{array}{c}
 7 \\ 8 \\ 4 \\ 3
 \end{array}$$

$$\text{and: } \left[ \begin{array}{ccc}
 a & b & c \\
 4 & 3 & 1
 \end{array} \right]$$

Soln.

need matrix:

$$\begin{array}{c}
 P_0 \\
 P_1 \\
 P_2 \\
 P_3
 \end{array}
 \left[ \begin{array}{ccc}
 a & b & c \\
 6 & -2 & 0 \\
 1 & 3 & 0 \\
 1 & 0 & 2 \\
 2 & 0 & 4
 \end{array} \right]
 \quad \begin{array}{c}
 4 & 3 & 3 \\
 6 & 4 & 5 \\
 7 & 6 & 6 \\
 7 & 9 & 10
 \end{array}$$

$$\begin{array}{c}
 6 & 4 & 4 \\
 6 & 7 & 8 \\
 6 & 7 & 9 \\
 7 & 7 & 10
 \end{array}$$

safe sequences:

~~$P_2 P_1 P_3 P_0$~~

$\langle P_1 P_0 P_2 P_3 \rangle \quad \langle P_1 P_0 P_3 P_2 \rangle$

$\langle P_1 P_2 P_3 P_0 \rangle \quad \langle P_1 P_2 P_0 P_3 \rangle$

Safety Algorithm

① let work & finish vectors of length m & n respectively.

Initialize: work = and & finish[i] = false for  $i = 0, 1, \dots, n-1$

② for index 'i' find such that both

a)  $\text{finish}[i] = \text{false}$

b)  $\text{need} \leq \text{work}$

if no such 'i' exists go to 7

③

$\text{work} = \text{work} + \text{allocation};$

$\text{finish}[i] = \text{true}$

goto 2

④ If  $\text{finish}[i] = \text{true}$  for all 'i' system is in safe state.

- steps:
- ① calculate need matrix
  - ② find available  $a, b, c$
  - ③  $CA = Total - avail.$
  - ④  $Need_i \leq C.A.$
  - ⑤ Pick the process & repeat.

$$C.A. = [4 \ 3 \ 1]$$

$$P_0: \begin{matrix} 6 & 2 & 0 \\ 6 \leq 4 & \therefore P_1 \end{matrix}$$

$$P_1: 1 \leq 4 \checkmark \quad 3 \leq 3 \checkmark \quad 0 \leq 1 \checkmark$$

pick  $P_1$

update  $CA_1$

$$\begin{array}{r} 4 \ 3 \ 1 \\ 2 \ 1 \ 2 \\ \hline 6 \ 4 \ 3 \end{array}$$

$\therefore$  write down all steps briefly & you can write only 1 safe sequence (not all needed).

Ques:

$$\begin{matrix} P_0 & \left[ \begin{matrix} x & y & z \\ 1 & 2 & 1 \end{matrix} \right] \\ P_1 & \left[ \begin{matrix} 2 & 0 & 1 \end{matrix} \right] \\ P_2 & \left[ \begin{matrix} 2 & 2 & 1 \\ 5 & 4 & 3 \end{matrix} \right] \end{matrix}$$

allocater matrix

① need matrix

$$\begin{matrix} P_0 & \left[ \begin{matrix} x & y & z \\ 1 & 0 & 3 \end{matrix} \right] \\ P_1 & \left[ \begin{matrix} 0 & 1 & 2 \end{matrix} \right] \\ P_2 & \left[ \begin{matrix} 1 & 2 & 0 \end{matrix} \right] \end{matrix}$$

max. matrix

$$\begin{matrix} P_0 & \left[ \begin{matrix} x & y & z \\ 2 & 2 & 4 \end{matrix} \right] \\ P_1 & \left[ \begin{matrix} 2 & 1 & 3 \end{matrix} \right] \\ P_2 & \left[ \begin{matrix} 3 & 4 & 1 \end{matrix} \right] \\ & \left[ \begin{matrix} x & y & z \\ 5 & 5 & 5 \end{matrix} \right] \text{ Total} \end{matrix}$$

② avl.  $x \ y \ z$

$$\begin{matrix} & \left[ \begin{matrix} 4 & 3 & 4 \end{matrix} \right] \\ ③ CA & = \left[ \begin{matrix} 0 & 1 & 2 \end{matrix} \right] \end{matrix}$$

$$P_0 \Rightarrow 1 \leq 0 \times$$

$$P_1 \quad 0 \leq 0 \checkmark \quad 1 \leq 1 \checkmark \quad 2 \leq 2 \checkmark$$

$\langle P_1 \ P_0 \ P_2 \rangle$

④ pick  $P_1$

⑤  $CA: [2 \ 1 \ 3]$

$$P_0: 1 \leq 2 \checkmark \quad 0 \leq 1 \checkmark \quad 3 \leq 3 \checkmark$$

pick  $P_0$

⑥  $CA: [3 \ 3 \ 4]$

pick  $P_2 \checkmark$

~~Ques.~~ Let  $\text{Request}_i$  be the request vector for process  $P_i$ . If  $\text{request}_i[j] = k$ , then process  $P_i$  wants 'k' instances of resource type  $R_j$ . When a request for resources is made by  $P_i$ , following steps are followed:

### Resource Request Algorithm

- i) if  $\text{Request}_i \leq \text{Need}_i$ , goto 2. Else raise an error, since process has exceeded maximum claim.
- ii) if  $\text{Request}_i \leq \text{Available}$ , goto 3. Else  $P_i$  must wait as resources aren't available.
- iii) Pretend to have allocated the requested resources to  $P_i$  & modify as follows:

$$\text{Available} = \text{available} - \text{Request}_i$$

$$\text{Allocation}_i = \text{Allocation}_i + \text{Request}_i$$

$$\text{Need}_i = \text{Need}_i - \text{Request}_i$$

If resulting resource allocation state is safe, transaction is completed & Process  $P_i$  is allocated the resources. But if new state is unsafe,  $P_i$  waits for  $\text{Request}_i$  & old resource allocation state is restored.

Ques. Take 3 resources A, B, C. At t<sub>0</sub>, allocation matrix instances  $\rightarrow [10 \ 5 \ 7]$

max. matrix	A	B	C
$P_0$	7	5	3
$P_1$	3	2	2
$P_2$	9	0	2
$P_3$	2	2	2
$P_4$	4	3	3

Soln:

$$\text{CA: } [3 \ 3 \ 2]$$

$$3 \ 4 \ 3$$

$$3 \ 4 \ 5$$

$$2 \ 4 \ 5$$

total matrix  $[10 \ 5 \ 7]$

$$\text{need}_{P_0} \left[ \begin{array}{ccc} 7 & 4 & 3 \\ 1 & 2 & 2 \\ 6 & 0 & 0 \\ 0 & 1 & 1 \\ 4 & 3 & 1 \end{array} \right]$$

$$\begin{matrix} P_0 \rightarrow P_4 & \left[ \begin{array}{ccc} 0 & 1 & 0 \\ 2 & 0 & 0 \\ 3 & 0 & 2 \\ 2 & 1 & 1 \\ 0 & 0 & 2 \\ 7 & 2 & 5 \end{array} \right] \\ P_0 & \left[ \begin{array}{ccc} 0 & 1 & 0 \\ 2 & 0 & 0 \\ 3 & 0 & 2 \\ 2 & 1 & 1 \\ 0 & 0 & 2 \\ 7 & 2 & 5 \end{array} \right] \\ P_1 & \left[ \begin{array}{ccc} 0 & 1 & 0 \\ 2 & 0 & 0 \\ 3 & 0 & 2 \\ 2 & 1 & 1 \\ 0 & 0 & 2 \\ 7 & 2 & 5 \end{array} \right] \\ P_2 & \left[ \begin{array}{ccc} 0 & 1 & 0 \\ 2 & 0 & 0 \\ 3 & 0 & 2 \\ 2 & 1 & 1 \\ 0 & 0 & 2 \\ 7 & 2 & 5 \end{array} \right] \\ P_3 & \left[ \begin{array}{ccc} 0 & 1 & 0 \\ 2 & 0 & 0 \\ 3 & 0 & 2 \\ 2 & 1 & 1 \\ 0 & 0 & 2 \\ 7 & 2 & 5 \end{array} \right] \\ P_4 & \left[ \begin{array}{ccc} 0 & 1 & 0 \\ 2 & 0 & 0 \\ 3 & 0 & 2 \\ 2 & 1 & 1 \\ 0 & 0 & 2 \\ 7 & 2 & 5 \end{array} \right] \end{matrix}$$

$$10 \ 4 \ 2 \quad 10 \ 5 \ 7$$

$(P_3 \ P_4 \ P_1 \ P_2 \ P_0) \rightarrow$  safe sequence

Req:  $P_1 < 1 \ 0 \ 2 >$

$$\textcircled{1} \quad R_i \leq N_i \quad 1 \leq 1 \quad 0 \leq 2 \quad 2 \leq 2 \quad \checkmark$$

$$\textcircled{2} \quad R_i \leq A_i \quad 1 \leq 3 = \quad 0 < 3 - \quad 2 \leq 2 \quad \checkmark$$

$$\textcircled{3} \quad \text{avl: } [2 \ 3 \ 0]$$

$$\text{all } P_1: [3 \ 0 \ 2]$$

$$\text{need } P_1: [0 \ 2 \ 0]$$

also	need		
$P_0$	$P_0$	avail	
$\begin{bmatrix} x & y & z \\ 0 & 1 & 0 \\ 3 & 0 & 2 \\ 3 & 0 & 2 \\ 2 & 1 & 1 \\ 0 & 0 & 2 \\ 8 & 2 & 7 \end{bmatrix}$	$P_1$	$\begin{bmatrix} x & y & z \\ 2 & 9 & 3 \\ 0 & 2 & 0 \\ 6 & 0 & 0 \\ 0 & 1 & 1 \\ 4 & 3 & 1 \end{bmatrix}$	$\begin{bmatrix} x & y & z \\ 2 & 3 & 0 \end{bmatrix}$
	$P_2$		5 3 2
	$P_3$		5 3 4
	$P_4$		7 4 5
			7 5 5
			10 5 7

$$< P_1 \ P_4 \ P_3 \ P_0 \ P_2 >$$

Assignment:

A request  $< 3, 3, 0 >$  in this scenario is made by  $P_4$ , it can be granted or not. Can a request by process  $P_0 < 0 \ 0 \ 2 >$  be granted or not after this.

$$P_4 < 3 \ 3 \ 0 >$$

$$\textcircled{1} \quad R_i \leq N_i \quad 3 \leq 4 \quad 3 \leq 3 - \quad 0 \leq 1 \quad \checkmark$$

$$\textcircled{2} \quad R_i \leq A_i \quad 3 \leq 3 \quad 3 \leq 3 \quad 0 \leq 2 \quad \checkmark$$

$$\textcircled{3} \quad \text{avl: } [0, 0, 2]$$

$$\text{all } P_4: [3 \ 3 \ 2]$$

$$\text{need: } P_4: [1, 0, 1]$$

$$\text{avl: } [0, 0, 2]$$

need won't get completed.

Request can't be granted.

$$① \quad 0 \leq 7, \quad 0 \leq 9, \quad 2 \leq 3 \quad \checkmark$$

$$② \quad 0 \leq 3, \quad 0 \leq 3, \quad 2 \leq 2 \quad \checkmark$$

$$③. \quad \text{all: } P_0 [0 \ 1 \ 2]$$

$$C.A.: [3 \ 3 \ 0]$$

$$\text{need: } [7 \ 4 \ 1]$$

Req. can't be granted.

### ③ Deadlock Detection & Recovery -

[only for single instances: wait for graph (for deadlock detection)]

For multiple instances:

1) let work & finish be vectors of length 'm' and 'n' respectively. Initialize work = available for  $i=0, 1, \dots, n-1$  if allocation  $\neq 0$  then  $\text{finish}[i] = \text{false}$  else  $\text{finish}[i] = \text{true}$

2) Find an index 'i' such that

a)  $\text{Finish}[i] == \text{false}$

b)  $\text{Request}_i \leq \text{work}$

If no such 'i' exist goto 4.

3)  $\text{work} = \text{work} + \text{allocation}_i$

$\text{finish}[i] = \text{true}$

goto 2

4) If  $\text{finish}[i] == \text{false}$  for some 'i',  $0 \leq i \leq n$ , then system is deadlocked. Also if  $\text{finish}[i] == \text{false}$ , then process  $P_i$  is deadlocked.

Gives-

Allocation matrix at time t<sub>0</sub>

	A	B	C	total instances	A	B	C
P <sub>0</sub>	0	1	0				
P <sub>1</sub>	2	0	0				
P <sub>2</sub>	3	0	3				
P <sub>3</sub>	2	1	1				
P <sub>4</sub>	0	0	2				
	7	2	6				

Request matrix

P <sub>0</sub>	0	0	0
P <sub>1</sub>	2	0	2
P <sub>2</sub>	0	0	0
P <sub>3</sub>	1	0	0
P <sub>4</sub>	0	0	2

IA: [0 0 0]

Soln.

$$Wode = 0 \quad 0 \quad 0 \quad P_0 \quad P_2 \quad P_3 \quad P_4 \quad P_1 \quad \begin{matrix} 0 & 1 & 0 \\ 3 & 1 & 3 \\ 5 & 2 & 4 \end{matrix}$$

∴ safe sequence ✓

at t<sub>0</sub>: P<sub>2</sub>: 0 0 1

then only P<sub>0</sub> can be fulfilled

∴ P<sub>1</sub>, P<sub>2</sub>, P<sub>3</sub>, P<sub>4</sub> are in deadlock & not finished

### Deadlock Recovery

/ \

Process  
Termination  
Resource  
Preemption

① select a victim

↳ HP will snatch R from low prior. P.

① abort all deadlocked processes

② Rollback

② abort processes one by one

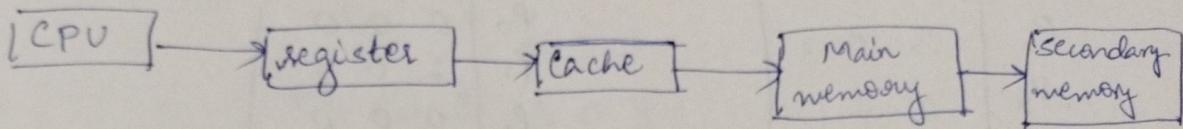
③ Starvation

- ↓
- based on priority
- types of process
- amt. of resources holding
- time of wait & execution

④ Ignorance

## Memory Management

size ↑ per unit cost ↑ access time ↓



Locality of Reference - S.M. is larger & has less per unit cost  
but more access time. ∴ instructions from SM are preferred  
& kept in the main memory for less access time.

Ques.

100 ms to access data from SM

10 ms to access data from MM

hit ratio = 90%. Find total access time.

Soln.

first check in ~~SM~~  $\rightarrow 10 \times 0.9$

then in ~~MM~~  $\rightarrow (10 + 100) 0.1$

Ans.

$$9 + 11 = 20 \text{ ms}$$

OS will translate the logical address generated by CPU  
to the physical address of main memory.

OS decides which data in SM gets which area in the  
main memory.

## Memory Allocation Policies

Contiguous      Non-contiguous

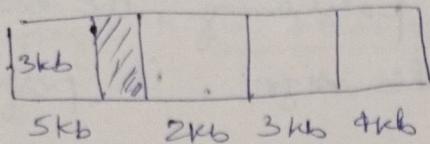
A. Contiguous      static / fixed

variable / dynamic

When bringing a process from SM to MM allocate it  
in MM consecutively together & in continuous partition  
which also has a part further fixed size partitioning &

Variable size partitioning.

e.g:



Internal fragmentation - In fixed size, if any process's size is less than the size of the partition then when the process gets inside the memory it creates a hole which is called as internal fragmentation. No problem in variable size.

External fragmentation - When the memory is sufficiently available to store a process but not in continuous form then we cannot accommodate that process & this is called external fragmentation.

Solution: memory compaction: when memory is reallocated to the processes so that all holes get combined to form one bigger hole & we end an partition allocation algorithm.

- ① Best fit ② Worst fit ③ First fit ④ Next fit

Question: Consider 5 memory partitions of size 100kb, 500kb, 200kb, 300kb, 600kb . If seq. of request for block sizes 212kb, 417kb, 112kb, 426kb arrive in the same order, which of the following makes efficient use of memory?

- ① Best ② First ③ Next ④ Worst

Soln -

	Best	Worst	First	Next
100kb	417	417	212	212
500 kb			112	112
200kb	112			
300kb	212	112		
600kb	426	212	417	417
	433 left	659 left	659	659

(However, keep any process in the left space).

Prove:

Claim 1: If it is fixed size partitioning, the best fit performs best but in variable size, it performs worst.

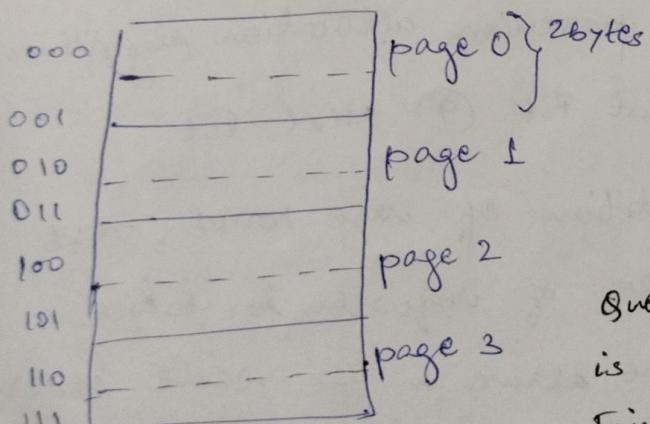
Claim 2: In fixed size partitioning, worst fit performs worst but in variable size, performs best.

If they are right, prove it with examples -

### Non-Contiguous Memory Allocation

#### A: Paging / Segmentation

The logical address space or secondary memory is divided into equal sized partitions & each partition is called a page.

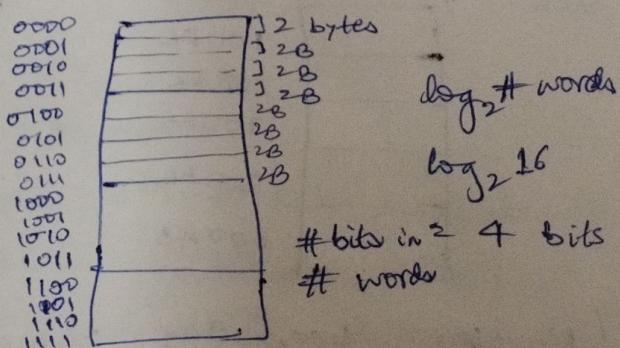


Process A (8 byte)

$$\# \text{Pages} = \frac{\text{logical add. space (LAS)}}{\text{page size}}$$

$$= \frac{8 \text{ bytes}}{2 \text{ bytes}}$$

$$\underline{\text{soln.}} \quad \# \text{words} = 32 / 2 = 16$$



$$\# \text{bits in } 2^4 \text{ bits} \\ \# \text{words}$$

page size = 8 bytes = 4 words

$$\# \text{ pages} = \frac{2^4 \text{ words size}}{4 \text{ words size}} = \frac{32}{8} = 4$$

Page no.	offset
2 bits	2 bits

Ques. [Frame size is just like page size but its in Main memory]. F. size = 2 bytes Here, main memory is Physical address space (PAS) = 8 bytes. Find no. of frames in MM & PA bit & bits division for frame no. & offset.

Sohm  $\frac{8}{2} = 4 = \text{no. of frames in MM.}$

$$\log_2 4 = 2$$

$$8 = 2^3 \rightarrow \text{bits.}$$

frame no.	offset
2	1

Ans.

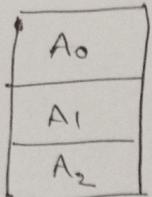
Ques. If LAS = 32 bits, PAS = 8 bits, Page size = 8 bytes. Find LAS, PAS, no. of pages & no. of frames.

Sohm.  $\frac{8}{3} \frac{2^9}{8} = 2^9 = \frac{2^9}{2^9} \Rightarrow \text{no. of pages.}$

PAS:	Page no./offset
$2^{29}$	$2^3$

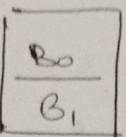
frame no./offset
$2^5 \quad 2^3$

Ans. Here, frame size = page size.



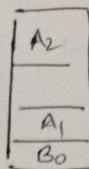
Process A (6B)

pages



Process B (4B)

pages

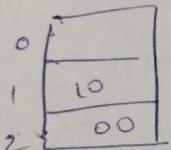


frame 0 = 00  
frame 1 = 01  
frame 2 = 10  
frame 3 = 11

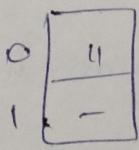
more than one page of  
more than one process.

### Page Table

To know, that which page of which process is running at frame no. in the main memory, page table can be used. More than 1 page of more than 1 processes can be placed anywhere in the main memory



Page table  
for process A



Page table  
for process B

Page table is created for each process that stores the info of frames nos. of respective pages.

# Translation Lookaside Buffer (TLB): some portion of page table cache will be here

In simple paging mechanism, main memory has to be accessed twice, one for accessing the page table through the page no. & then for actually accessing the main memory — PAS (frame + offset). To reduce the effective main memory access time a cache memory that contains some part of the page table is used which is called translation

clockside buffer.

H → hit ratio of TLB cache

M → main memory access time

C → cache memory access time

Effective main memory (EMMAT)  $\Rightarrow$  access time  $H(M+C) + (1-H)(2M+C)$

Ques. Considering a paging mechanism if main memory access time is 100ns & TLB having 80% hit ratio & access time as 20ns.

Soln.

$$\text{EMMAT} = 0.8(100+20) + 0.2(200+20)$$
$$= 190\text{ns.}$$

Page Table uses:

- Which page no. is running on which frame
- Protection Bit
- Page valid/ invalid

Page is in process's LAS  $\Rightarrow$  valid

Ques. LA = 14 bit Page size = 2 kb Process size = 10489 bytes.

Find no. of pages in LAS.

Soln. LAS:  $\Rightarrow 2^{14}$  bytes. Page size =  $2 \cdot 2^{10} = 2^{11}$

Pg 0	v	] <sup>2k</sup>	# pages = $\frac{2^{14}}{2^{11}} = 2^3 = 8$ pages
Pg 1	v	] <sup>2k</sup>	
Pg 2	v	] <sup>2k</sup>	
Pg 3	v	] <sup>2k</sup>	
Pg 4	v	] <sup>2k</sup>	
Pg 5	v	] <sup>2k</sup>	
Pg 6	i	] <sup>2k</sup>	
Pg 7	i	] <sup>2k</sup>	

v → valid  
i → invalid

## Inverted Paging Exist

The memory is being wasted by storing the info about the invalid pages in the page table. The total # valid pages in the system for all processes cannot exceed the no. of frames in each MM to avoid this wasting.

Here, we create the frame table or IPT where no. of entries is same as no. of frames in MM.

Ques: LA = 32 bits PA = 16 bits.

If paging is applied with page size 1024 bytes. If each page table entry contain 4 bytes info. Calculate.

A. ① no. of pages ② # of frame.

B. Page table size in ① simple paging & ② inverted paging

Soln LAS =  $2^{32}$  bytes PAS =  $2^{16}$  bytes

$$\text{Page size} = 2^{10} \quad \therefore \quad \# \text{ pages} = \frac{2^{32}}{2^{10}} = 2^{22}$$

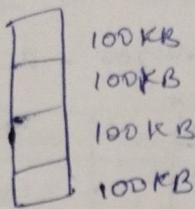
$$\# \text{ frames} = \frac{2^{16}}{2^{10}} = 2^6$$

B. ①  $4 \times 2^{22} = 2^{24}$       ②  $2^6 \times 2^{22} = 2^{28}$

B. Segmentation

## Example 1: Fixed - Size Partitioning

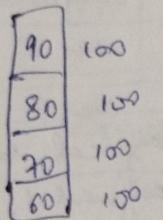
mem. blocks



Processes:

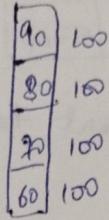
90KB  
80KB  
70KB  
60KB

Best fit



Performs well  
with minimal internal  
fragmentation

Worst fit

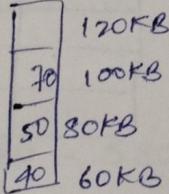


no optimization here

## Example 2: Variable - size Partitioning

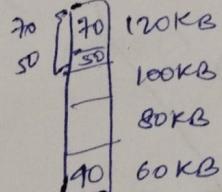
Best

mem. blocks  
70, 50, 40



higher fragmentation  
worst performance

Worst



efficient usage of  
largest memory.

∴ Performs best in this case

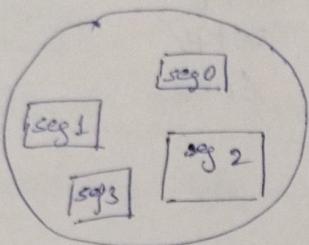
Conclusion:

Claim 1 is True → Best fit  $\Leftarrow$  in fixed size

Claim 2 is True → Worst fit  $\Leftarrow$  in variable size

## B. Segmentation

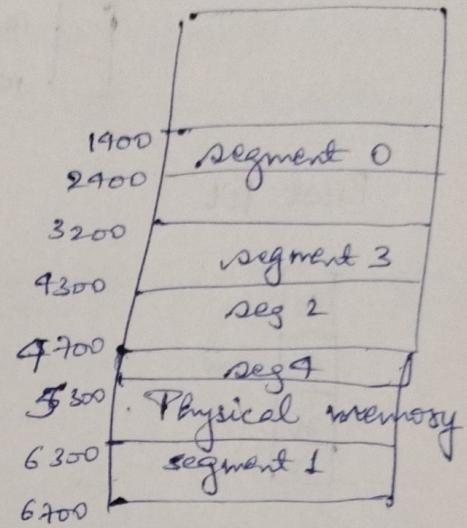
divided it unequal sizes. accessed through M.M.



different sizes

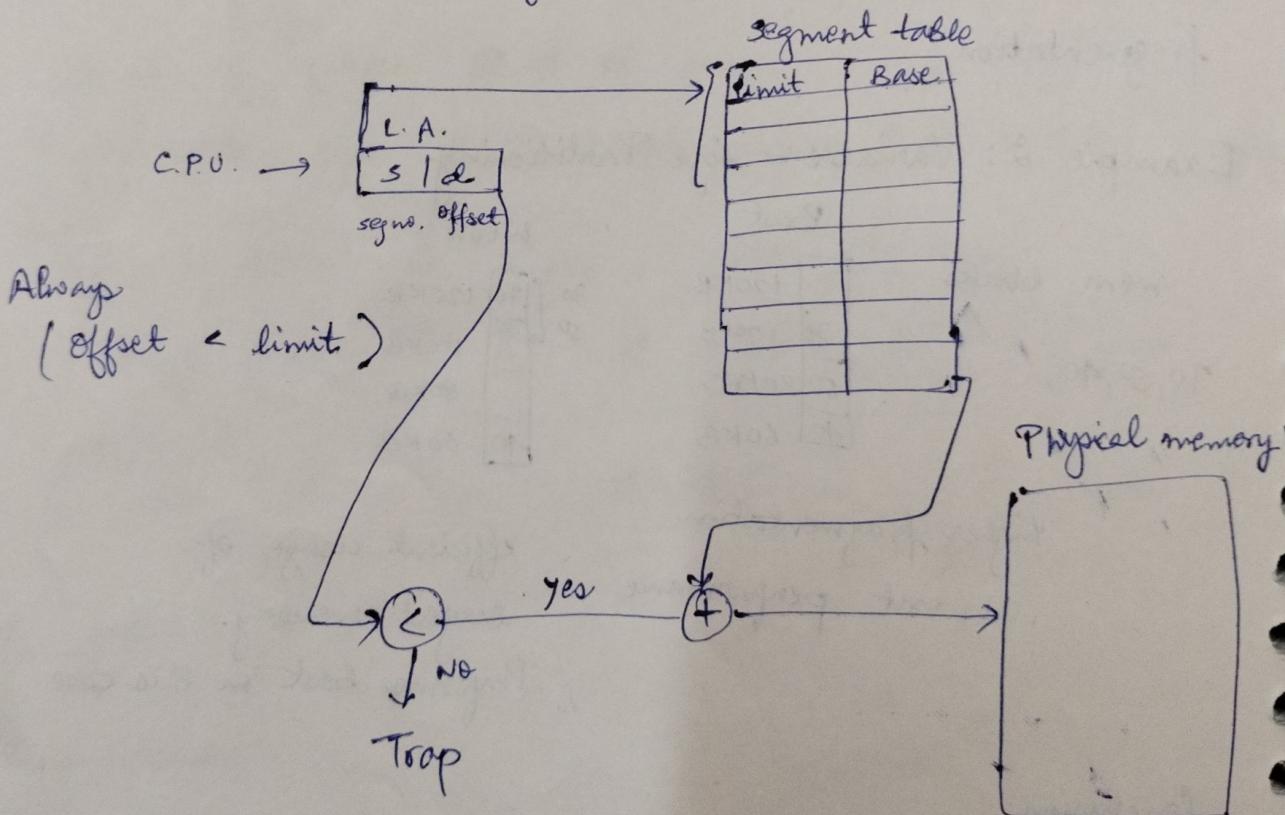
	limit	size
0	1000	1400
1	900	6300
2	900	9300
3	1100	3200
4	1000	9700

segment table



limit is  $\Rightarrow$  length

base is  $\Rightarrow$  starting address



L.A. is divided into segment no. & offset. Seg. no. is used to index into the segment table to obtain the limit & base for that segment.

Offset value is compared  $\in$  the limit. If it is smaller then

it will be added to the base value to obtain PA. Else it results into a trap.

Ques:

Seg.	Base	length
0	219	609
1	2300	14
2	90	100
3	1327	580
4	1952	96

What are the PA for the given LA?

- ① 0, 430
- ② 1, 11
- ③ 2, 500
- ④ 3, 900
- ⑤ 4, 112

Segment table

Soln.

$$\textcircled{1} \quad 0, 430$$

$$430 < 609 \checkmark$$

$$430 + 219 = 649$$

\textcircled{2}

$$11 < 14 \checkmark$$

$$11 + 2300 = 2311$$

\textcircled{3}

$$500 < 100 \times$$

\therefore Trap (error)

\textcircled{4}

$$400 \cancel{580} < 580, \checkmark$$

$$400 + 1327 = 1727$$

\textcircled{5}

$$112 < 96 \times$$

\therefore Trap (error)

## \rightarrow Page Replacement Algorithms

Page fault / miss  $\rightarrow$  Page not found in MM, so we check in SM.

If all pages are filled, we replace it using algos.

Performance of Demand Paging -

$$P \times (\text{page fault time}) \\ + (1-P) \text{ main memory access time}$$

① FIFO Policy -

Reference string  $\langle 7 \ 0 \ 1 \ 2 \ 0 \ 3 \ 0 \ 4 \ 2 \ 3 \ 0 \ 3 \ 1 \ 2 \ 0 \rangle$

frames:

F3		1	1	1	1	0	0	0	3	3	3	3	2	2
F2		0	0	0	0	3	3	2	2	2	2	1	1	1
F1	7	7	2	2	2	2	4	4	0	0	0	0	0	0
	P.F.	P.F.	P.F.	P.F.	H.	P.F.	P.F.	P.F.	P.F.	P.F.	H	P.F.	P.F.	H

$$\text{Hit} = 3$$

$$P.F. = 12$$

$$\frac{12}{15}$$

$$\frac{3}{15}$$

$$P.F. = \frac{4}{5}$$

$$\frac{1}{5} = \text{Hit ratio}$$

80% 20%

Ans.

Ques.

RS.  $\langle 1 \ 2 \ 3 \ 4 \ 1 \ 2 \ 5 \ 1 \ 2 \ 3 \ 4 \ 5 \rangle$

frames:

3		3	3	3	2	2	2	2	2	2	4	4
2		2	2	2	1	1	2	1	1	3	3	3
1	1	1	1	4	4	4	5	5	5	5	5	5

$$H = 3/12 = \frac{1}{4}$$

frames?

4		4	4	4	4	4	4	4	3	3	3
3		3	3	3	3	3	3	2	2	2	2
2		2	2	2	2	2	1	1	1	1	5
1	1	1	1	1	1	5	5	5	5	4	4

$$H = 2/12 = \frac{1}{6}$$

## Belady's Anomaly =

Even after  $\uparrow$  the # page frames, page faults  $\uparrow$   
 which is unexpected, found (in FIFO policy).  
 (like in prev. ques.)

### ② Optimal Page Replacement Algorithm

Replace that page which is not used in longest dimension  
 of time in near future.

Reference string: < 7 0 1 2 0 3 0 4 2 3 0 3 2 1 2 0 1 7 0 1 >  
 strings.

frames: f4		2	2	2	2	2	2	2	2	2	2	2	2	2	7	7	7
f3		1	1	1	1	1	4	4	4	4	4	1	1	1	1	1	1
f2		0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
f1		7	7	7	7	3	3	3	3	3	3	3	3	3	3	3	3
	F	F	F	H	F	H	F	H	H	H	H	F	H	H	F	H	H

Hits = 12

Page faults = 8

$$HR = \frac{12}{20} = \frac{4}{5} \Rightarrow 80\%$$

### ③ Least Recently Used (LRU)

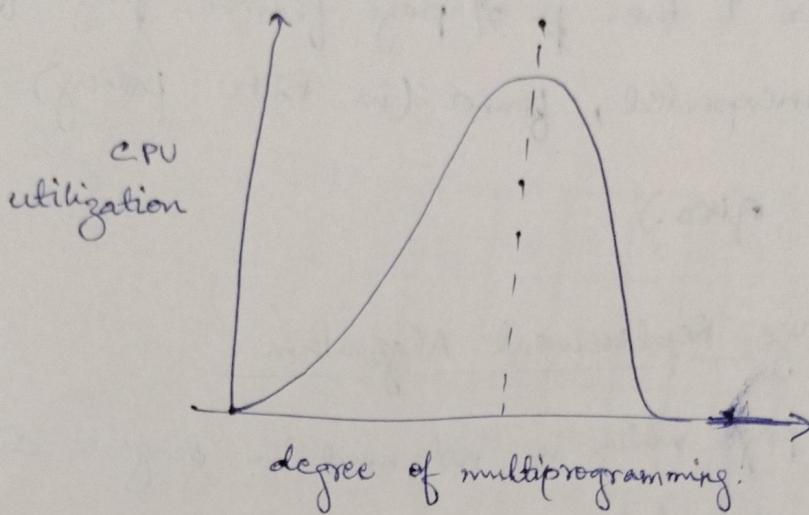
Reference string: < 7 0 1 2 0 3 0 4 2 3 0 3 2 1 2 0 1 7 0 1 >

frames: f4		2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	
f3		1	1	1	1	1	4	4	4	4	4	1	1	1	1	1	
f2		0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
f1		7	7	7	7	3	3	3	3	3	3	3	3	3	7	7	7
	F	F	F	H	F	H	F	H	H	H	H	F	H	H	F	H	H

Hits = 12

Faults = 8

## → Thrashing —



When we ↑ the degree of multiprogramming beyond a certain level, the CPU utilization decreases because the processor is always busy in swapping rather than in useful computation. This happens because the changes that are swapped out are needed in immediate future again & again.

## → Disk Scheduling —

Seek Time - Time required to move the read-write head on the desired track.

But to take the head on the desired sector, the time req. is called rotational latency:-