

## Lab - 4 : Thermodynamic Properties and Ensemble Averages

Aim :- Given time evolution of volume and energy at 6 pressure values. Evaluate compressibility and specific heat as function of pressure.

Theory :-

$$\text{Compressibility, } \kappa_p = \frac{\langle (\Delta V)^2 \rangle}{\langle \Delta V \rangle^2 k_B T} = \frac{\langle (V - \langle V \rangle)^2 \rangle}{\langle \Delta V \rangle^2 k_B T}$$

$$\text{Specific Heat, } C_V = \frac{\langle (\Delta E)^2 \rangle}{k_B T^2} = \frac{\langle (E - \langle E \rangle)^2 \rangle}{k_B T^2}$$

$$\langle \Delta x \rangle = \frac{1}{N} \sum_{i=1}^N x_i$$

## Lab4-Fluctuations.py

```
1 import numpy as np
2 import matplotlib.pyplot as plt
3
4 def read_xvg_file(file_path):
5     data = np.loadtxt(file_path, comments=['#', '@'])
6     return data[:, 1]
7
8 T = 300
9 k_B = 1.380649e-23
10
11 Ps = [0.1, 1, 10, 100, 1000, 10000]
12 Kps = []
13 Cvs = []
14
15 for P in Ps:
16     volume_data = read_xvg_file(f'npt_fluctuations/npt{P}/volume.xvg')
17     energy_data = read_xvg_file(f'npt_fluctuations/npt{P}/energy.xvg')
18
19     avg_volume = np.mean(volume_data)
20     avg_volume_2 = np.mean((volume_data-avg_volume)**2)
21
22     avg_energy = np.mean(energy_data)
23     avg_energy_2 = np.mean((energy_data-avg_energy)**2)
24
25     Kp = avg_volume_2/((avg_volume**2) * k_B * T)
26     Cv = avg_energy_2 / (k_B * (T**2))
27
28     Kps.append(Kp)
29     Cvs.append(Cv)
30
31 # Plot Compressibility vs Pressure
32 plt.figure(figsize=(10, 5))
33 plt.subplot(1, 2, 1)
34 plt.plot(Ps, Kps, label='Compressibility ( $\kappa$ )', marker='o', color='b')
35 plt.xscale('log') # Log scale for pressure
36 plt.xlabel('Pressure (P)')
37 plt.ylabel('Compressibility ( $\kappa$ )')
38 plt.title(f'Compressibility vs Pressure at {T}K')
39 plt.grid(True)
40
41 # Plot Specific Heat vs Pressure
42 plt.subplot(1, 2, 2)
43 plt.plot(Ps, Cvs, label='Specific Heat ( $C_V$ )', marker='s', color='r')
44 plt.xscale('log') # Log scale for pressure
45 plt.xlabel('Pressure (P)')
46 plt.ylabel('Specific Heat ( $C_V$ )')
47 plt.title(f'Specific Heat vs Pressure at {T}K')
48 plt.grid(True)
49
50 # Show the plots
51 plt.tight_layout()
```

```
52 | plt.show()
```

