

MISPLACED TILES

```
def misplaced_tiles(state, goal):
```

```
    count = 0
```

```
    for i in range(3):
```

```
        for j in range(3):
```

```
            if state[i][j] != goal[i][j] and state[i][j] != 0:
```

```
                count += 1
```

```
    return count
```

```
def get_neighbors(state):
```

```
    neighbors = []
```

```
    for i in range(3):
```

```
        for j in range(3):
```

```
            if state[i][j] == 0:
```

```
                x, y = i, j
```

```
                break
```

```
    else:
```

```
        continue
```

```
    break
```

```
moves = [(0, 1), (0, -1), (1, 0), (-1, 0)]
```

```
for dx, dy in moves:
```

```
    nx, ny = x + dx, y + dy
```

```
    if 0 <= nx < 3 and 0 <= ny < 3:
```

```
        new_state = [list(row) for row in state]
```

```
        new_state[x][y], new_state[nx][ny] = new_state[nx][ny], new_state[x][y]
```

```
        neighbors.append(tuple(tuple(row) for row in new_state))
```

```
return neighbors
```

```
def astar_search(initial, goal):
```

```
    frontier = [(misplaced_tiles(initial, goal), 0, initial)]
```

```
    explored = set()
```

```
    parent = {}
```

```
    cost = {initial: 0}
```

```
    while frontier:
```

```

f, g, current = heapq.heappop(frontier)

if current == goal:
    path = []
    while current in parent:
        path.append(current)
        current = parent[current]
    path.append(initial)
    return path[::-1]

explored.add(current)

for neighbor in get_neighbors(current):
    new_cost = cost[current] + 1
    if neighbor not in cost or new_cost < cost[neighbor]:
        cost[neighbor] = new_cost
        priority = new_cost + misplaced_tiles(neighbor, goal)
        heapq.heappush(frontier, (priority, new_cost, neighbor))
        parent[neighbor] = current
return None

def get_state_input(prompt):
    print(prompt)
    state = []
    for _ in range(3):
        row = list(map(int, input().split()))
        state.append(row)
    return tuple(tuple(row) for row in state)

initial_state = get_state_input("Enter the initial state (3 rows of 3 numbers separated by spaces,
use 0 for the blank):")
goal_state = get_state_input("Enter the goal state (3 rows of 3 numbers separated by spaces,
use 0 for the blank):")

path = astar_search(initial_state, goal_state)

if path:
    print("Solution found:")

```

```

for step in path:
    for row in step:
        print(row)
    print()
else:
    print("No solution found.")

```

The screenshot shows a Jupyter Notebook interface with the following content:

Code Cell:

```

print(row)
    print()
else:
    print("No solution found.")

```

Input Prompts and Output:

Enter the initial state (3 rows of 3 numbers separated by spaces, use 0 for the blank):

```

2 8 3
1 6 4
7 0 5

```

Enter the goal state (3 rows of 3 numbers separated by spaces, use 0 for the blank):

```

1 2 3
8 0 4
7 6 5

```

Solution found:

```

(2, 8, 3)
(1, 6, 4)
(7, 0, 5)

(2, 8, 3)
(1, 0, 4)
(7, 6, 5)

(2, 0, 3)
(1, 8, 4)
(7, 6, 5)

(0, 2, 3)
(1, 8, 4)
(7, 6, 5)

(1, 2, 3)
(0, 8, 4)
(7, 6, 5)

(1, 2, 3)
(8, 0, 4)
(7, 6, 5)

```

MANHATTAN DISTANCE

```
import heapq
```

```
def manhattan_distance(state, goal):
    distance = 0
    for i in range(3):
        for j in range(3):
            if state[i][j] != 0:
                value = state[i][j]
                # Find the position of the value in the goal state
                for gi in range(3):
                    for gj in range(3):
                        if goal[gi][gj] == value:
                            goal_pos = (gi, gj)
                            break
                    else:
                        continue
                distance += abs(i - goal_pos[0]) + abs(j - goal_pos[1])
    return distance
```

```
def get_neighbors(state):
    neighbors = []
    for i in range(3):
        for j in range(3):
            if state[i][j] == 0:
                x, y = i, j
                break
        else:
            continue
    break
```

```
moves = [(0, 1), (0, -1), (1, 0), (-1, 0)]
for dx, dy in moves:
    nx, ny = x + dx, y + dy
    if 0 <= nx < 3 and 0 <= ny < 3:
```

```

        new_state = [list(row) for row in state]
        new_state[x][y], new_state[nx][ny] = new_state[nx][ny], new_state[x][y]
        neighbors.append(tuple(tuple(row) for row in new_state))
    return neighbors

```

```

def astar_search_manhattan(initial, goal):
    frontier = [(manhattan_distance(initial, goal), 0, initial)]
    explored = set()
    parent = {}
    cost = {initial: 0}

    while frontier:
        f, g, current = heapq.heappop(frontier)

        if current == goal:
            path = []
            while current in parent:
                path.append(current)
                current = parent[current]
            path.append(initial)
            return path[::-1]

        explored.add(current)

        for neighbor in get_neighbors(current):
            new_cost = cost[current] + 1
            if neighbor not in cost or new_cost < cost[neighbor]:
                cost[neighbor] = new_cost
                priority = new_cost + manhattan_distance(neighbor, goal)
                heapq.heappush(frontier, (priority, new_cost, neighbor))
                parent[neighbor] = current
    return None

```

```

def get_state_input(prompt):
    print(prompt)
    state = []
    for _ in range(3):
        row = list(map(int, input().split()))

```

```
        state.append(row)
    return tuple(tuple(row) for row in state)

initial_state_m = get_state_input("Enter the initial state for Manhattan distance (3 rows of 3
numbers separated by spaces, use 0 for the blank):")
goal_state_m = get_state_input("Enter the goal state for Manhattan distance (3 rows of 3
numbers separated by spaces, use 0 for the blank):")

path_m = astar_search_manhattan(initial_state_m, goal_state_m)

if path_m:
    print("Solution found using Manhattan distance:")
    for step in path_m:
        for row in step:
            print(row)
        print()
else:
    print("No solution found using Manhattan distance.")
```



Q Commands + Code + Text ▶ Run all ▼



```
if path_m:
    print("Solution found using Manhattan distance:")
    for step in path_m:
        for row in step:
            print(row)
        print()
else:
    print("No solution found using Manhattan distance.")
```

Enter the initial state for Manhattan distance (3 rows of 3 numbers separated by spaces, use 0 for the blank):

2 8 3

1 6 4

7 0 5

Enter the goal state for Manhattan distance (3 rows of 3 numbers separated by spaces, use 0 for the blank):

1 2 3

8 0 4

7 6 5

Solution found using Manhattan distance:

(2, 8, 3)

(1, 6, 4)

(7, 0, 5)

(2, 8, 3)

(1, 0, 4)

(7, 6, 5)

(2, 0, 3)

(1, 8, 4)

(7, 6, 5)

(0, 2, 3)

(1, 8, 4)

(7, 6, 5)

(1, 2, 3)

(0, 8, 4)

(7, 6, 5)

(1, 2, 3)

(8, 0, 4)

(7, 6, 5)

8-9-25

LAB IV - A* ALGORITHM

1

Misplaced
Tiles

Manhattan
Distance

| | | |
|---|---|---|
| 2 | 8 | 3 |
| 1 | 6 | 4 |
| 7 | | 5 |

I x

| | | |
|---|---|---|
| 1 | 2 | 3 |
| 8 | | 4 |
| 7 | 6 | 5 |

F

$$f(n) = g(n) + h(n)$$

| | | |
|---|---|---|
| 2 | 8 | 3 |
| 1 | 6 | 4 |
| 7 | | 5 |

| | | |
|---|---|---|
| 2 | 8 | 3 |
| 1 | 6 | 4 |
| 7 | | 5 |

| | | |
|---|---|---|
| 2 | 8 | 3 |
| 1 | 6 | 4 |
| 7 | | 5 |

| | | |
|---|---|---|
| 2 | 8 | 3 |
| 1 | 6 | 4 |
| 7 | | 5 |

① Misplaced

① Misplaced Tiles

| | | |
|---|---|---|
| 2 | 8 | 3 |
| 1 | 6 | 4 |
| 7 | | 5 |

R

U

L

| | | |
|---|---|---|
| 2 | 8 | 3 |
| 1 | 6 | 4 |
| 7 | 5 | |

$$1+5=6$$

| | | |
|---|---|---|
| 2 | 8 | 3 |
| 1 | | 4 |
| 7 | 6 | 5 |

$$1+3=4$$

| | | |
|---|---|---|
| 2 | 8 | 3 |
| 1 | 6 | 4 |
| | 7 | 5 |

$$1+5=6$$

R

U

L

| | | |
|---|---|---|
| 2 | 8 | 3 |
| 1 | 4 | |
| 7 | 6 | 5 |

$$2+4=6$$

| | | |
|---|---|---|
| 2 | | 3 |
| 1 | 8 | 4 |
| 7 | 6 | 5 |

$$2+3=5$$

| | | |
|---|---|---|
| 2 | 8 | 3 |
| | 1 | 4 |
| 7 | 6 | 5 |

$$2+3=5$$

L

R

U

D

| | | |
|---|---|---|
| | 2 | 3 |
| 1 | 8 | 4 |
| 7 | 6 | 5 |

$$3+2=5$$

| | | |
|---|---|---|
| 2 | 3 | |
| 1 | 8 | 4 |
| 7 | 6 | 5 |

$$3+3=6$$

| | | |
|---|---|---|
| | 8 | 3 |
| 2 | 1 | 4 |
| 7 | 6 | 5 |

$$3+3=6$$

| | | |
|---|---|---|
| 2 | 8 | 3 |
| 7 | 1 | 4 |
| | 6 | 5 |

$$3+4=7$$

| | | |
|---|---|---|
| 1 | 2 | 3 |
| | 8 | 4 |
| 7 | 6 | 5 |

$$4+1=5$$

R

| | | |
|---|---|---|
| 1 | 2 | 3 |
| 8 | | 4 |
| 7 | 6 | 5 |

goal state

(II) Manhattan Distance →

| | | |
|---|---|---|
| 1 | 2 | 3 |
| 4 | 5 | 6 |
| 7 | 8 | |

Final

| | | |
|---|---|---|
| 1 | 5 | 8 |
| 3 | 2 | |
| 4 | 6 | 7 |

R

| | | |
|---|---|---|
| 1 | 5 | 8 |
| 3 | | 2 |
| 4 | 6 | 7 |

D

| | | |
|---|---|---|
| 1 | 5 | 8 |
| 3 | 2 | 7 |
| 4 | 6 | |

U

| | | |
|---|---|---|
| 1 | 5 | |
| 3 | 2 | 8 |
| 4 | 6 | 7 |

1 2 3 4 5 6 7 8
0 2 3 1 1 2 2 3

$$14 + 1 = 15$$

1 2 3 4 5 6 7 8
0 1 3 1 1 2 3 3

$$14 + 1 = 15$$

1 2 3 4 5 6 7 8
0 1 3 1 1 2 2 2

$$12 + 1 = 13$$

L

| | | |
|---|---|---|
| 1 | | 5 |
| 3 | 2 | 8 |
| 4 | 6 | 7 |

1 2 3 4 5 6 7 8
0 1 3 1 2 2 2 2

$$13 + 2 = 15$$

L

| | | |
|---|---|---|
| | 1 | 5 |
| 3 | 2 | 8 |
| 4 | 6 | 7 |

1 2 3 4 5 6 7 8
1 1 3 1 2 2 2 2

$$14 + 3 = 17$$

D

| | | |
|---|---|---|
| 1 | 2 | 5 |
| 3 | | 8 |
| 4 | 6 | 7 |

1 2 3 4 5 6 7 8
0 0 3 1 2 2 2 2

$$12 + 3 = 15$$

state loop