

* Strassen's Matrix Multiplication

- Strassen used product matrices to approach this problem:

$$P_1 = A \cdot (F - H) = \text{DC_Mat_Mul}(A, F - H)$$

$$P_2 = (A + B) \cdot H = \text{DC_Mat_Mul}(A + B, H)$$

$$P_3 = (C + D) \cdot E = \text{DC_Mat_Mul}(C + D, E)$$

$$P_4 = D \cdot (G - E) = \text{DC_Mat_Mul}(D, G - E)$$

$$P_5 = (A + D) \cdot (E + H) = \text{DC_Mat_Mul}(A + D, E + H)$$

$$P_6 = (B - D) \cdot (G + H) = \text{DC_Mat_Mul}(B - D, G + H)$$

$$P_7 = (A - C) \cdot (E + F) = \text{DC_Mat_Mul}(A - C, E + F)$$

- We divide our answer matrix in four parts to execute:

$$\begin{bmatrix} P_5 + P_4 - P_2 + P_6 & P_1 + P_2 \\ P_3 + P_4 & P_1 + P_5 - P_3 - P_7 \end{bmatrix}$$

- Complexity Analysis

$$\begin{aligned} T(n) &= 7T(n^2/4) + O(n^2) \\ a > b^d &\Rightarrow T(n) = O(n^{2 \log_4 7}) \\ &= O(n^{\log_4 49}) \\ &= \underline{\underline{O(n^{2.81})}} \end{aligned}$$