AI 1110 Assignment 1

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12.13.2.12 Question: A die is tossed thrice. Find the probability of getting an odd number at least once.

Answer: $\frac{7}{8}$

Solution:

Let X,Y,Z be three Bernoulli random variables defined as follows -

$$X = \begin{cases} 1 & \text{,if odd number occurs on the } 1^{st} \text{ roll of die} \\ 0 & \text{,otherwise} \end{cases} \tag{1}$$

$$Y = \begin{cases} 1 & \text{,if odd number occurs on the } 2^{nd} \text{ roll of die} \\ 0 & \text{,otherwise} \end{cases} \tag{2}$$

$$Z = \begin{cases} 1 & \text{,if odd number occurs on the } 3^{rd} \text{ roll of die} \\ 0 & \text{,otherwise} \end{cases} \tag{3}$$

Let $'Pr'$ be the probability of getting an odd number atleast once.

Then $'Pr'$ is equal to the compliment of getting an even number on every die toss.

$\because$

$$\Pr(A) + \Pr\left(\bar{A}\right) = 1 \tag{4}$$

$\implies$

Pr(X=1∪Y=1∪Z=1) = 1 - Pr(X=0∩Y=0∩Z=0)

For this event (Pr(X=0∩Y=0∩Z=0)) = $\frac{3}{6} * \frac{3}{6} * \frac{3}{6}$

$\therefore$ From Equation 4,

$$Pr = 1 - \left(\frac{3}{6} * \frac{3}{6} * \frac{3}{6}\right)$$

$$\implies Pr = 1 - \left(\frac{1}{2}\right)^3$$

$$\implies Pr = 1 - \frac{1}{8}$$

$$\implies Pr = \frac{7}{8}$$