## 1

## AI 1110 Assignment 1

Name: Shreyas Premkhede Roll no.: CS22BTECH11053

**12.13.2.12 Question:** A die is tossed thrice. Find the probability of getting an odd number at least once.

Answer:  $\frac{7}{8}$ 

**Solution:** Let a binomial random variable be:

$$X \sim Bin(n, p)$$
 (1)

where, p be the probability of getting odd number on one throw of dice.

n is the number of times dice is rolled.

Let *i* be the number of times odd number occurs.

$$\therefore \Pr(X = i) = {}^{n}C_{i} \cdot p^{i} \cdot (1 - p)^{n - i}$$
 (2)

$$\implies p = \frac{1}{2} \tag{3}$$

$$\implies n = 3$$
 (4)

Let Cumulative Distribution function be:

$$F_X(i) = \Pr\left(X \le i\right) \tag{5}$$

$$\Pr(X = i) = {}^{3}C_{i} \cdot p^{i} \cdot (1 - p)^{3 - i}$$
(6)

$$\therefore F_X(i) = \sum_{r=0}^{i} {}^{3}C_r p^r (1-p)^{3-r}$$
 (7)

$$\implies F_X(0) = {}^{3}C_0 p^0 (1 - p)^{3 - 0} \tag{8}$$

$$\implies F_X(0) = {}^{3}C_0 \cdot p^0 \cdot (1-p)^{3-0} = \frac{{}^{3}C_0}{8} = \frac{1}{8} \quad (9)$$

$$F_X(3) = 1 \tag{10}$$

٠.,

$$\implies \Pr(X > 1) = \sum_{i=1}^{3} \Pr(X = i)$$
 (11)

$$= F_X(3) - F_X(0) \tag{12}$$

$$=1-\frac{1}{8}$$
 (13)

$$=\frac{7}{8}\tag{14}$$