## AI 1110 Assignment 1

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**12.13.2.12 Question:** A die is tossed thrice. Find the probability of getting an odd number at least once.

**Answer:**  $\frac{7}{8}$  **Solution:** 

Let X,Y,Z be three Bernoulli random variables defined as follows -

 $X = \begin{cases} 1 & \text{,if odd number occurs on the } 1^{st} \text{ roll of die} \\ 0 & \text{,otherwise} \end{cases}$ 

 $Y = \begin{cases} 1 & \text{,if odd number occurs on the } 2^{nd} \text{ roll of die} \\ 0 & \text{,otherwise} \end{cases}$ 

 $Z = \begin{cases} 1 & \text{,if odd number occurs on the } 3^{rd} \text{ roll of die} \\ 0 & \text{,othserwise} \end{cases}$ 

(3)

Let A be the event of getting an odd number at least once and Pr(A) be its probability.

Then Pr(A) is equal to the compliment of getting an even number on every die toss.

:

$$Pr(A) + Pr(\bar{A}) = 1 \tag{4}$$

 $\Longrightarrow$ 

Pr(X=1∪Y=1∪Z=1) = 1 - Pr(X=0∩Y=0∩Z=0) For this event (Pr(X=0∩Y=0∩Z=0)) =  $\frac{3}{6} * \frac{3}{6} * \frac{3}{6}$ ∴ From Equation 4,

$$\Pr(A) = 1 - \left(\frac{3}{6} * \frac{3}{6} * \frac{3}{6}\right)$$

$$\implies \Pr(A) = 1 - \left(\frac{1}{2}\right)^3 = 1 - \frac{1}{8} = \frac{7}{8}$$