## 1

## AI 1110 Assignment 1

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**12.13.2.12 Question:** A die is tossed thrice. Find the probability of getting an odd number at least once.

Answer:  $\frac{7}{8}$ 

**Solution:** Let A be the required event.

Let i be the number of times odd number occurs.

Let *p* be the probability of getting odd number on one throw of dice.

:. 
$$\Pr(X = i) = {}^{3}C_{i} \cdot p^{i} \cdot (1 - p)^{3-i}$$
  
 $p = \frac{1}{2}$ 

Let Cumulative Distribution function be:

$$\implies F_X(i) = \Pr(X \le i)$$
 (1)

$$\Pr(X = i) = {}^{3}C_{i} \cdot p^{i} \cdot (1 - p)^{3 - i}$$
 (2)

$$\therefore F_X(i) = \sum_{r=0}^{i} {}^{3}C_r p^r (1-p)^{3-r}$$
 (3)

$$\implies F_X(0) = {}^{3}C_0 p^0 (1 - p)^{3 - 0} \tag{4}$$

$$\implies F_X(0) = {}^{3}C_0 \cdot p^0 \cdot (1-p)^{3-0} = \frac{{}^{3}C_0}{8} = \frac{1}{8} \quad (5)$$

$$\implies F_X(1) = \frac{1}{8} + {}^{3}C_1 \times \frac{1}{2} \times \left(1 - \frac{1}{2}\right)^2 = \frac{4}{8}$$
 (6)

$$\implies F_X(2) = \frac{1}{8} + {}^{3}C_1 \times \frac{1}{2} \times \left(1 - \frac{1}{2}\right)^2$$

$$+{}^{3}C_{2} \times \left(\frac{1}{2}\right)^{2} \times \left(1 - \frac{1}{2}\right) = \frac{7}{8}$$
 (7)

$$F_X(3) = 1 \tag{8}$$

·.,

$$Pr(A) = F_X(3) - F_X(0)$$
 (9)

$$=1-\frac{1}{8}$$
 (10)

$$=\frac{7}{8}\tag{11}$$