

# **VISVESVARAYA TECHNOLOGICAL UNIVERSITY**

**“JnanaSangama”, Belgaum -590014, Karnataka.**



## **LAB RECORD**

### **Bio Inspired Systems (23CS5BSBIS)**

*Submitted by*

**Shreyas Rao M(1BM22CS272)**

*in partial fulfillment for the award of the degree of*

**BACHELOR OF ENGINEERING  
*in*  
COMPUTER SCIENCE AND ENGINEERING**



**B.M.S. COLLEGE OF ENGINEERING  
(Autonomous Institution under VTU)  
BENGALURU-560019  
Sep-2024 to Jan-2025**

**B.M.S. College of Engineering,**  
**Bull Temple Road, Bangalore 560019**  
(Affiliated To Visvesvaraya Technological University, Belgaum)  
**Department of Computer Science and Engineering**



**CERTIFICATE**

This is to certify that the Lab work entitled “ Bio Inspired Systems (23CS5BSBIS)” carried out by **Shreyas Rao M (1BM22CS272)**, who is bonafide student of **B.M.S. College of Engineering**. It is in partial fulfillment for the award of **Bachelor of Engineering in Computer Science and Engineering** of the Visvesvaraya Technological University, Belgaum. The Lab report has been approved as it satisfies the academic requirements of the above mentioned subject and the work prescribed for the said degree.

Prof. Spoorthi D M Assistant Professor Department of CSE, BMSCE	Dr. Kavitha Sooda Professor & HOD Department of CSE, BMSCE
---	--

## **Index**

<b>Sl. No.</b>	<b>Date</b>	<b>Experiment Title</b>	<b>Page No.</b>
1	24-10-2024	Genetic Algorithm for Optimization Problems	3-5
2	7-11-2024	Particle Swarm Optimization for Function Optimization	6-8
3	14-11-2024	Ant Colony Optimization for the Traveling Salesman Problem	9-12
4	21-11-2024	Cuckoo Search Optimization	13-15
5	28-11-2024	Grey Wolf Optimizer	16-19
6	18-12-2024	Parallel Cellular Algorithms and Programs	20-22
7	18-12-2024	Optimization via Gene Expression Algorithms	23-25

Github Link: [https://github.com/ShreyasRaoM07/BIS\\_LAB](https://github.com/ShreyasRaoM07/BIS_LAB)

## **Program 1**

Problem statement

Genetic Algorithm for Optimization Problems:

Genetic Algorithms (GA) are inspired by the process of natural selection and genetics, where the fittest individuals are selected for reproduction to produce the next generation. GAs are widely used for solving optimization and search problems. Implement a Genetic Algorithm using Python to solve a basic optimization problem, such as finding the maximum value of a mathematical function.

Algorithm:

## Genetic algorithm

### Algorithm

- Objective function  
~~Evaluate fitness (x):~~  
  // input : x - The current chromosome value  
  // Output: The value of the function.  
  return  $x^2$
- generate\_population (size, range):  
  // input : size - Number of chromosomes need to be generated  
  range - Specifies the range within which the population is to be generated  
  return random values of 'size' within range[0] and range[1]
- evaluate\_fitness (population):  
  // input - Receive the current population  
  // output - Return an array of all the objective fn values  
  return [Objective function (x) for x in range population]
- selection (population, fitness):  
  // input: population - To select two chromosomes from the whole population to act as parents  
  // output: Two parents  
  probabilities = fitness / fitness sum(s)  
  return random two chromosomes based on probabilities

Bafna Gold  
Date: Page: 2

```

crossover(parent1, parent2):
    // Input: parent1 & parent2 - Parents whose chromosomes is
    // used to generate a new child
    // Output: A child or the parent itself based on
    // success of the crossover
    if random.crossover_rate:
        return (parent1 + parent2)/2
    else:
        return parent1 or parent2 if parent.random() < 0.5
mutation(indi, mut_rate, value_range):
    // Input: indi - the chromosome to mutate
    // Output: mutated or non mutated individual
    if random.no < mut_rate:
        return random value in range
    else:
        return indi

genetic_alg():
    population = generate_population(size, range)
    best_solution = None
    best_fitness = -infinity

    for generation in num_gen:
        fitness = evaluate_fitness(population)
        max_index = max(fitness)

        if fitness(max_index) > best_fitness:
            best_solution = population[max_index]
            best_fitness = fitness(max_index)

```

~~for i in population:~~  
 parent1, parent2 = selection(population)  
 offspring = crossover(parent1, parent2)  
 offspring = mutation(offspring, mut\_rate, value)  
 new\_population = population + offspring  
 return best\_solution, best\_fitness

population\_size = 10  
 num\_generations = 100  
 mutation\_rate = 0.1  
 crossover\_rate = 0.7  
 value = (-5, 5)

20/10/29

Code:

```
import numpy as np
```

```
def objective_function(x):
    return x ** 2
```

```
population_size = 100
num_generations = 50
mutation_rate = 0.1
crossover_rate = 0.7
value_range = (-10, 10)
```

```
def initialize_population(size, value_range):
    return np.random.uniform(value_range[0], value_range[1], size)
```

```
def evaluate_fitness(population):
    return np.array([objective_function(x) for x in population])
```

```

def selection(population, fitness):
    probabilities = fitness / fitness.sum()
    return population[np.random.choice(len(population), size=2, p=probabilities)]

def crossover(parent1, parent2):
    if np.random.rand() < crossover_rate:
        return (parent1 + parent2) / 2 # Simple averaging crossover
    return parent1 if np.random.rand() < 0.5 else parent2

def mutate(individual, mutation_rate, value_range):
    if np.random.rand() < mutation_rate:
        return np.random.uniform(value_range[0], value_range[1])
    return individual

def genetic_algorithm():
    population = initialize_population(population_size, value_range)
    best_solution = None
    best_fitness = -np.inf

    for generation in range(num_generations):
        fitness = evaluate_fitness(population)

        current_best_index = np.argmax(fitness)
        if fitness[current_best_index] > best_fitness:
            best_fitness = fitness[current_best_index]
            best_solution = population[current_best_index]

        new_population = []
        for _ in range(population_size):
            parent1, parent2 = selection(population, fitness)
            offspring = crossover(parent1, parent2)
            offspring = mutate(offspring, mutation_rate, value_range)
            new_population.append(offspring)

        population = np.array(new_population)

    return best_solution, best_fitness

best_solution, best_fitness = genetic_algorithm()

print(f"Best solution found: x = {best_solution:.2f}")
print(f"Maximum value of f(x) = x^2: f(x) = {best_fitness:.2f}")

```

```

Best solution found: x = 10.00
Maximum value of f(x) = x^2: f(x) = 99.95

```

## Program 2

Problem statement

Particle Swarm Optimization for Function Optimization:

Particle Swarm Optimization (PSO) is inspired by the social behavior of birds flocking or fish schooling. PSO is used to find optimal solutions by iteratively improving a candidate solution with regard to a given measure of quality. Implement the PSO algorithm using Python to optimize a mathematical function.

Algorithm:

Bafna Gold  
Date: Page 4

Particle Swarm Optimization.

```

Objective function (position)
    return position[0]^2 + position[1]^2

class particle
    position = random number within [bounds[0], bounds[1]]
    velocity = random in [-1, 1]
    best_position = position
    best_score = Objective function (position)

    update_velocity(global_best_position):
        velocity = inertia * velocity + cognitive + social
        cognitive = cog_coeff * r1 * (best_position - position)
        social = soc_coeff * r2 * (global_best_position - position)
        r1 = random number [0 to 1]
        r2 = random number [0 to 1]

    update_position():
        position += velocity
        if position > bounds:
            position = bounds

    evaluate():
        score = objective function (position)
        if score < best_score:
            best_position = position
            best_score = score

```

swarm = list of particles (size = n)  
 global\_best\_position = swarm[0].best\_position  
 global\_best\_score = objective function (global\_best\_positio  
 for i in range (max\_iter):
 for particle in swarm:
 update\_velocity(global\_best\_position)
 update\_position()
 evaluate()
 if particle.best\_score < global\_best\_score:
 global\_best\_position = particle.best\_position
 global\_best\_score = particle.best\_score
 Return: global\_best\_position, global\_best\_score

(Date: 02/01/20)

Code:

```
import numpy as np

# Define the objective function to be optimized (e.g., f(x, y) = x^2 + y^2)
def objective_function(position):
    return position[0] ** 2 + position[1] ** 2

# Particle class to represent each particle in the swarm
class Particle:
    def __init__(self, bounds):
        # Initialize position and velocity randomly within bounds
        self.position = np.array([np.random.uniform(bound[0], bound[1]) for bound in bounds])
        self.velocity = np.array([np.random.uniform(-1, 1) for _ in bounds])
        self.best_position = self.position.copy()
        self.best_score = objective_function(self.position)

    def update_velocity(self, global_best_position, inertia_weight, cognitive_coef, social_coef):
        # Generate random factors for stochastic update
        r1, r2 = np.random.rand(2)

        # Update velocity based on inertia, cognitive, and social components
        cognitive_component = cognitive_coef * r1 * (self.best_position - self.position)
        social_component = social_coef * r2 * (global_best_position - self.position)

        self.velocity = inertia_weight * self.velocity + cognitive_component + social_component

    def update_position(self, bounds):
        # Update position based on velocity
        self.position += self.velocity
        # Enforce boundary conditions
        for i in range(len(bounds)):
            if self.position[i] < bounds[i][0]:
                self.position[i] = bounds[i][0]
            elif self.position[i] > bounds[i][1]:
                self.position[i] = bounds[i][1]

    def evaluate(self):
        # Evaluate the fitness of the particle
        score = objective_function(self.position)
        # Update personal best if the new position is better
        if score < self.best_score:
            self.best_score = score
            self.best_position = self.position.copy()

# Particle Swarm Optimization (PSO) algorithm
def particle_swarm_optimization(num_particles, bounds, inertia_weight, cognitive_coef, social_coef,
```

```

max_iterations):
    # Initialize swarm
    swarm = [Particle(bounds) for _ in range(num_particles)]
    global_best_position = swarm[0].position.copy()
    global_best_score = objective_function(global_best_position)

    # Find initial global best
    for particle in swarm:
        if particle.best_score < global_best_score:
            global_best_score = particle.best_score
            global_best_position = particle.best_position.copy()

    # Optimization loop
    for iteration in range(max_iterations):
        for particle in swarm:
            # Update particle velocity and position
            particle.update_velocity(global_best_position, inertia_weight, cognitive_coef, social_coef)
            particle.update_position(bounds)
            particle.evaluate()

            # Update global best if the particle's best position is better
            if particle.best_score < global_best_score:
                global_best_score = particle.best_score
                global_best_position = particle.best_position.copy()

    # After all iterations, print the final global best score
    print(f'Final Iteration {max_iterations}, Global Best Score: {global_best_score}')
    return global_best_position, global_best_score

# Define the parameters for PSO
num_particles = 30          # Number of particles in the swarm
bounds = [(5, 10), (5, 10)]  # Bounds for the search space (e.g., x and y can vary from -10 to 10)
inertia_weight = 0.5          # Inertia weight
cognitive_coef = 1.5         # Cognitive (personal best) coefficient
social_coef = 1.5             # Social (global best) coefficient
max_iterations = 100          # Number of iterations to run the algorithm

# Run PSO to find the minimum of the objective function
best_position, best_score = particle_swarm_optimization(num_particles, bounds, inertia_weight,
cognitive_coef, social_coef, max_iterations)

print(f'Best Position: {best_position}')
print(f'Best Score: {best_score}')

Final Iteration 100, Global Best Score: 50.0
Best Position: [5. 5.]
Best Score: 50.0

```

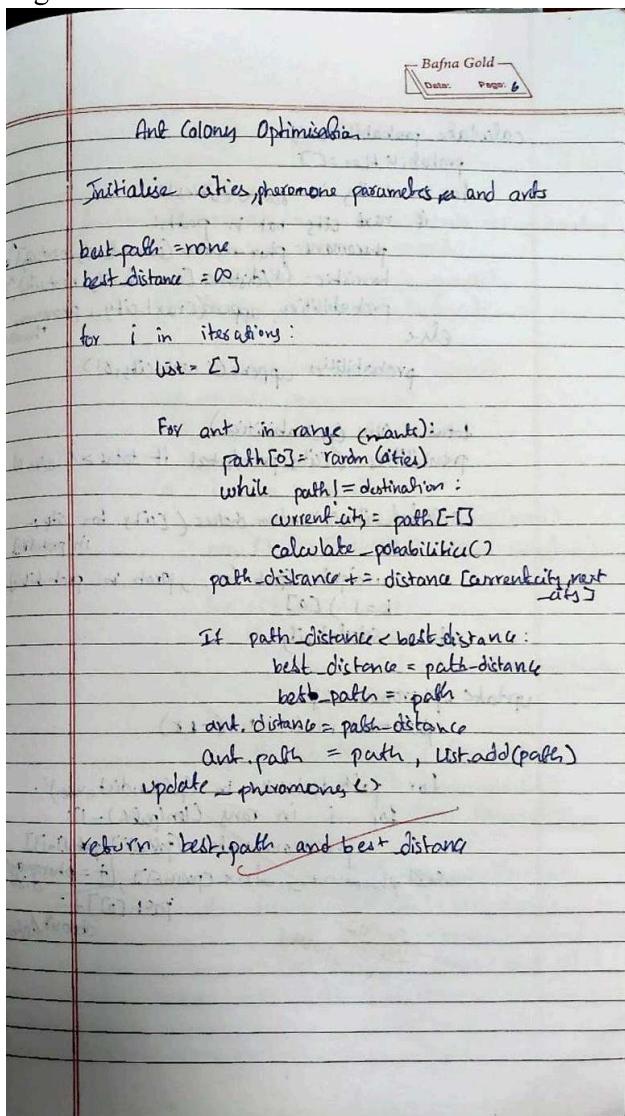
### Program 3

Problem statement

Ant Colony Optimization for the Traveling Salesman Problem:

The foraging behavior of ants has inspired the development of optimization algorithms that can solve complex problems such as the Traveling Salesman Problem (TSP). Ant Colony Optimization (ACO) simulates the way ants find the shortest path between food sources and their nest. Implement the ACO algorithm using Python to solve the TSP, where the objective is to find the shortest possible route that visits a list of cities and returns to the origin city

Algorithm:



Code:

```

import numpy as np
import random

class ACO:
    def __init__(self, n_ants, n_iterations, alpha, beta, rho, pheromone_deposit, cities):
        self.n_ants = n_ants
        self.n_iterations = n_iterations
        self.alpha = alpha # importance of pheromone
        self.beta = beta # importance of heuristic information
        self.rho = rho # pheromone evaporation rate
        self.pheromone_deposit = pheromone_deposit # pheromone deposit for the best path
        self.cities = cities
        self.num_cities = len(cities)
        self.distances = self.calculate_distances(cities)
        self.pheromone_matrix = np.ones((self.num_cities, self.num_cities))

    def calculate_distances(self, cities):
        distances = np.zeros((len(cities), len(cities)))
        for i, (x1, y1) in enumerate(cities):
            for j, (x2, y2) in enumerate(cities):
                distances[i, j] = np.sqrt((x1 - x2) ** 2 + (y1 - y2) ** 2)
        return distances

    def run(self):
        best_distance = float('inf')
        best_path = None

        for iteration in range(self.n_iterations):
            all_paths = []
            all_distances = []

            for ant in range(self.n_ants):
                path = self.construct_solution()
                path_distance = self.calculate_path_distance(path)
                all_paths.append(path)
                all_distances.append(path_distance)

                if path_distance < best_distance:
                    best_distance = path_distance
                    best_path = path

            self.update_pheromones(all_paths, all_distances)
            print(f"Iteration {iteration+1}: Best Distance = {best_distance}")

        return best_path, best_distance

    def construct_solution(self):
        path = [random.randint(0, self.num_cities - 1)]
        while len(path) < self.num_cities:
            current_city = path[-1]
            next_city = self.choose_next_city(current_city, path)
            path.append(next_city)

```

```

return path

def choose_next_city(self, current_city, path):
    probabilities = []
    for next_city in range(self.num_cities):
        if next_city not in path:
            pheromone = self.pheromone_matrix[current_city, next_city] ** self.alpha
            heuristic = (1.0 / self.distances[current_city, next_city]) ** self.beta
            probabilities.append((next_city, pheromone * heuristic))
        else:
            probabilities.append((next_city, 0))

    total = sum(prob for _, prob in probabilities)
    probabilities = [(city, prob / total if total > 0 else 0) for city, prob in probabilities]

    selected_city = random.choices(
        [city for city, _ in probabilities],
        weights=[prob for _, prob in probabilities],
        k=1
    )[0]
    return selected_city

def calculate_path_distance(self, path):
    distance = 0
    for i in range(len(path) - 1):
        distance += self.distances[path[i], path[i + 1]]
    distance += self.distances[path[-1], path[0]] # return to start
    return distance

def update_pheromones(self, paths, distances):
    self.pheromone_matrix *= (1 - self.rho) # evaporate pheromones

    # deposit pheromones based on path quality
    for path, distance in zip(paths, distances):
        for i in range(len(path) - 1):
            self.pheromone_matrix[path[i], path[i + 1]] += self.pheromone_deposit / distance
        self.pheromone_matrix[path[-1], path[0]] += self.pheromone_deposit / distance # return to start

# Example usage with random cities
cities = [(random.randint(0, 100), random.randint(0, 100)) for _ in range(10)]
print(cities)
aco = ACO(n_ants=10, n_iterations=100, alpha=1, beta=2, rho=0.5, pheromone_deposit=10, cities=cities)
best_path, best_distance = aco.run()

print("\nBest Path:", best_path)
print("Best Distance:", best_distance)

```

```
Iteration 60: Best Distance = 326.99882689334635
Iteration 61: Best Distance = 326.99882689334635
Iteration 62: Best Distance = 326.99882689334635
Iteration 63: Best Distance = 326.99882689334635
Iteration 64: Best Distance = 326.99882689334635
Iteration 65: Best Distance = 326.99882689334635
Iteration 66: Best Distance = 326.99882689334635
Iteration 67: Best Distance = 326.99882689334635
Iteration 68: Best Distance = 326.99882689334635
Iteration 69: Best Distance = 326.99882689334635
Iteration 70: Best Distance = 326.99882689334635
Iteration 71: Best Distance = 326.99882689334635
Iteration 72: Best Distance = 326.99882689334635
Iteration 73: Best Distance = 326.99882689334635
Iteration 74: Best Distance = 326.99882689334635
Iteration 75: Best Distance = 326.99882689334635
Iteration 76: Best Distance = 326.99882689334635
Iteration 77: Best Distance = 326.99882689334635
Iteration 78: Best Distance = 326.99882689334635
Iteration 79: Best Distance = 326.99882689334635
Iteration 80: Best Distance = 326.99882689334635
Iteration 81: Best Distance = 326.99882689334635
Iteration 82: Best Distance = 326.99882689334635
Iteration 83: Best Distance = 326.99882689334635
Iteration 84: Best Distance = 326.99882689334635
Iteration 85: Best Distance = 326.99882689334635
Iteration 86: Best Distance = 326.99882689334635
Iteration 87: Best Distance = 326.99882689334635
Iteration 88: Best Distance = 326.99882689334635
Iteration 89: Best Distance = 326.99882689334635
Iteration 90: Best Distance = 326.99882689334635
Iteration 91: Best Distance = 326.99882689334635
Iteration 92: Best Distance = 326.99882689334635
Iteration 93: Best Distance = 326.99882689334635
Iteration 94: Best Distance = 326.99882689334635
Iteration 95: Best Distance = 326.99882689334635
Iteration 96: Best Distance = 326.99882689334635
Iteration 97: Best Distance = 326.99882689334635
Iteration 98: Best Distance = 326.99882689334635
Iteration 99: Best Distance = 326.99882689334635
Iteration 100: Best Distance = 326.99882689334635

Best Path: [7, 9, 5, 4, 1, 3, 8, 0, 6, 2]
Best Distance: 326.99882689334635
```

## Program 4

Problem statement

Cuckoo Search (CS):

Cuckoo Search (CS) is a nature-inspired optimization algorithm based on the brood parasitism of some cuckoo species. This behavior involves laying eggs in the nests of other birds, leading to the optimization of survival strategies. CS uses Lévy flights to generate new solutions, promoting global search capabilities and avoiding local minima. The algorithm is widely used for solving continuous optimization problems and has applications in various domains, including engineering design, machine learning, and data mining.

Algorithm:

```

Bafna Gold
Date: Page 8

Cuckoo Search Algorithm

function CuckooSearch (func, bounds, n_nests = 5, n_iterations = 1000, pa = 0.25):
    nests = InitializeNests(bounds, n_nests)
    fitness = EvaluateFitness(nests, func)

    best_idx = index_of_minimum(fitness)
    best_solution = nests[best_idx]
    best_fitness = fitness[best_idx]

    for i=1 to n_iterations:
        new_nests = GenerateNewSolutions(nests)
        new_fitness = EvaluateFitness(new_nests, func)

        for i=1 to n_nests:
            if random < pa:
                new_nests[i] = GenerateRandomSolution(bounds)

        for i=1 to n_nests:
            if new_fitness[i] < fitness[i]:
                nests[i] = new_nests[i]
                fitness[i] = new_fitness[i]

        best_idx = index_of_minimum(fitness)
        if fitness[best_idx] < best_fitness:
            best_solution = nests[best_idx]
            best_fitness = fitness[best_idx]

    return best_solution, best_fitness

function InitializeNests (bounds; n_nests):
    nests = random_array(n_nests, length(bounds))
    for i=1 to length(bounds):
        nests[i] = random_value_in_range(bounds[i])
    return nests

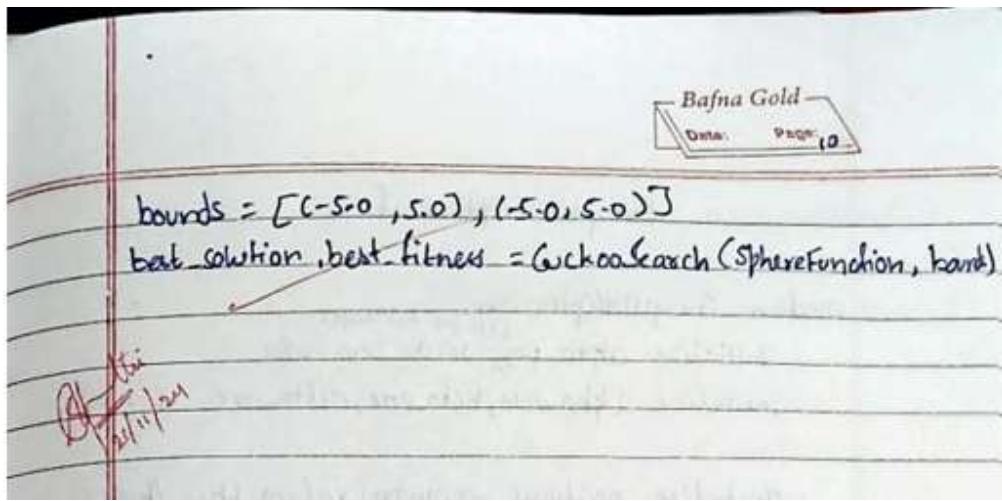
function EvaluateFitness (nests, func):
    fitness = []
    for each nest in nests:
        fitness.append(func(nest))
    return fitness

function GenerateNewSolutions(nests):
    new_nests = copy(nests)
    levy_flight = random_normal(0, 1, size=nests.shape) * absolute(CrandomNormal(0, 1, size=nests.shape))
    new_nests = new_nests + levy_flight
    return new_nests

function GenerateRandomSolution (bounds):
    random_solution = []
    for i=1 to length(bounds):
        random_solution[i] = random_value_in_range(bounds[i])
    return random_solution

function sphere_function(x):
    return sum(x[i]**2 for all i)

```



Code:

```
import numpy as np
```

```

def cuckoo_search(func, bounds, n_nests=25, n_iterations=1000, pa=0.25):
    dim = len(bounds)
    nests = initialize_nests(bounds, n_nests)
    fitness = evaluate_fitness(nests, func)
    best_idx = np.argmin(fitness)
    best_solution = nests[best_idx]
    best_fitness = fitness[best_idx]

    for iteration in range(n_iterations):
        new_nests = generate_new_solutions(nests)
        new_fitness = evaluate_fitness(new_nests, func)

        for i in range(n_nests):
            if np.random.rand() < pa:
                new_nests[i] = generate_random_solution(bounds)

        for i in range(n_nests):
            if new_fitness[i] < fitness[i]:
                nests[i] = new_nests[i]
                fitness[i] = new_fitness[i]

        best_idx = np.argmin(fitness)
        if fitness[best_idx] < best_fitness:
            best_solution = nests[best_idx]
            best_fitness = fitness[best_idx]

    #print(f'Iteration {iteration + 1}/{n_iterations}, Best Fitness: {best_fitness}')

    return best_solution, best_fitness
  
```

```

def initialize_nests(bounds, n_nests):
    nests = np.random.rand(n_nests, len(bounds))
    for i in range(len(bounds)):
        nests[:, i] = bounds[i][0] + (bounds[i][1] - bounds[i][0]) * nests[:, i]
    return nests

def evaluate_fitness(nests, func):
    return np.array([func(nest) for nest in nests])

def generate_new_solutions(nests):
    new_nests = np.copy(nests)
    levy_flight = np.random.normal(0, 1, size=nests.shape) * np.abs(np.random.normal(0, 1, size=nests.shape))
    new_nests += levy_flight
    return new_nests

def generate_random_solution(bounds):
    return np.array([np.random.uniform(bounds[i][0], bounds[i][1]) for i in range(len(bounds))])

def sphere_function(x):
    return np.sum(x**2)

bounds = [(-5.0, 5.0), (-5.0, 5.0)]

best_solution, best_fitness = cuckoo_search(sphere_function, bounds)

print("Best Solution:", best_solution)
print("Best Fitness:", best_fitness)

```

**Best Solution: [-0.00143299 0.00383832]**  
**Best Fitness: 1.6786154692913296e-05**

## Program 5

Problem statement

Grey Wolf Optimizer (GWO):

The Grey Wolf Optimizer (GWO) algorithm is a swarm intelligence algorithm inspired by the social hierarchy and hunting behavior of grey wolves. It mimics the leadership structure of alpha, beta, delta, and omega wolves and their collaborative hunting strategies. The GWO algorithm uses these social hierarchies to model the optimization process, where the alpha wolves guide the search process while beta and delta wolves assist in refining the search direction. This algorithm is effective for continuous optimization problems and has applications in engineering, data analysis, and machine learning.

Algorithm:

The image shows two pages of handwritten notes for the Grey Wolf Optimization algorithm.

**Page 1 (Left):**

- Header:** Grey Wolf Optimization
- Function:** GreyWolfOptimizer
  - Inputs:  $\text{lb}$ ,  $\text{ub}$ ,  $\text{n_wolves}$ ,  $\text{max_iter}$ ,  $\text{c1}$ ,  $\text{c2}$ ,  $\text{A_min}$ ,  $\text{A_max}$ ,  $\text{C_min}$ ,  $\text{C_max}$
  - Initializations:
    - Initialize  $\text{alpha\_pos}$  as a zero vector
    - Initialize  $\text{alpha\_score}$ ,  $\text{beta\_score}$ ,  $\text{delta\_score}$  as infinity
    - Initialize positions → random values btw  $\text{lb}$  &  $\text{ub}$
    - Initialize scores as a zero vector
  - Loop for  $t = 1$  to  $\text{max\_iter}$ :
    - Update  $\text{A} = \text{A}_{\min} + (\text{A}_{\max} - \text{A}_{\min}) * (t / \text{max\_iter})$
    - For  $i = 1$  to  $n_{\text{wolves}}$ :
      - Calculate  $\text{score} = \text{obj\_func}(\text{positions}[i])$
      - Update  $\text{scores}[i] = \text{score}$
      - If  $\text{score} < \text{alpha\_score}$ :
        - Update  $\text{alpha\_score} = \text{score}$
        - Update  $\text{alpha\_pos} = \text{positions}[i]$
      - Else if  $\text{score} < \text{beta\_score}$ :
        - Update  $\text{beta\_score} = \text{score}$
        - Update  $\text{beta\_pos} = \text{positions}[i]$
      - Else if  $\text{score} < \text{delta\_score}$ :
        - Update  $\text{delta\_score} = \text{score}$
        - Update  $\text{delta\_pos} = \text{positions}[i]$
    - For  $i = 1$  to  $n_{\text{wolves}}$ :
      - Update  $\text{r1} = \text{random values in bounds}$
      - Update  $\text{r2} = \text{random values in bounds}$
      - Update  $\text{A} = \text{A} * \text{A} * \text{r1} - \text{A}$
      - Update  $\text{C} = \text{C} * \text{r2}$

Code:

import numpy as np

```

# Objective function (Example: Sphere function)
def objective_function(x):
    return np.sum(x**2)

# Grey Wolf Optimization Algorithm
class GreyWolfOptimizer:
    def __init__(self, obj_func, dim, n_wolves, max_iter, lb, ub):
        self.obj_func = obj_func # Objective function
        self.dim = dim          # Dimensionality of the problem
        self.n_wolves = n_wolves # Number of wolves
        self.max_iter = max_iter # Maximum number of iterations
        self.lb = lb             # Lower bound of the search space
        self.ub = ub             # Upper bound of the search space
        self.alpha_pos = np.zeros(dim) # Position of alpha wolf
        self.alpha_score = float("inf") # Fitness of alpha wolf
        self.beta_pos = np.zeros(dim) # Position of beta wolf
        self.beta_score = float("inf") # Fitness of beta wolf
        self.delta_pos = np.zeros(dim) # Position of delta wolf
        self.delta_score = float("inf") # Fitness of delta wolf
        self.positions = np.random.rand(n_wolves, dim) * (ub - lb) + lb # Initial positions of wolves
        self.scores = np.zeros(n_wolves) # Fitness scores

    def optimize(self):
        # Main optimization loop
        for t in range(self.max_iter):
            a = 2 - t * (2 / self.max_iter) # Decreases linearly from 2 to 0
            for i in range(self.n_wolves):
                # Evaluate fitness of each wolf
                self.scores[i] = self.obj_func(self.positions[i])

                # Update alpha, beta, and delta wolves
                if self.scores[i] < self.alpha_score:
                    self.alpha_score = self.scores[i]
                    self.alpha_pos = self.positions[i]
                elif self.scores[i] < self.beta_score:
                    self.beta_score = self.scores[i]
                    self.beta_pos = self.positions[i]
                elif self.scores[i] < self.delta_score:
                    self.delta_score = self.scores[i]
                    self.delta_pos = self.positions[i]

            # Update the positions of the wolves
            for i in range(self.n_wolves):
                # Calculate random values for A and C
                r1 = np.random.rand(self.dim)
                r2 = np.random.rand(self.dim)

```

```

A = 2 * a * r1 - a
C = 2 * r2

# Update the position of the wolf
D_alpha = np.abs(C * self.alpha_pos - self.positions[i])
D_beta = np.abs(C * self.beta_pos - self.positions[i])
D_delta = np.abs(C * self.delta_pos - self.positions[i])

X1 = self.alpha_pos - A * D_alpha
X2 = self.beta_pos - A * D_beta
X3 = self.delta_pos - A * D_delta

# Calculate new position for the wolf
self.positions[i] = (X1 + X2 + X3) / 3

# Apply boundary constraints (if any)
self.positions[i] = np.clip(self.positions[i], self.lb, self.ub)

# Optionally, print the best solution found so far
#print(f"Iteration {t+1}/{self.max_iter} - Best Score: {self.alpha_score}")

# Return the best solution found
return self.alpha_pos, self.alpha_score

# Hyperparameters
dim = 30          # Number of dimensions (variables)
n_wolves = 50      # Number of wolves (population size)
max_iter = 1000    # Maximum number of iterations
lb = -10          # Lower bound of search space
ub = 10          # Upper bound of search space

# Instantiate the optimizer
optimizer = GreyWolfOptimizer(obj_func=objective_function, dim=dim, n_wolves=n_wolves,
max_iter=max_iter, lb=lb, ub=ub)

# Perform optimization
best_position, best_score = optimizer.optimize()

# Output the best solution found
print("\nBest Position: ", best_position)
print("Best Score: ", best_score)

```

```
Best Position: [ 3.31543532e-28 -2.57971219e-28 2.90350626e-28 -3.27713250e-28
3.52185014e-28 2.80085911e-28 -3.38381673e-28 -2.97466794e-28
-2.31745008e-28 3.13252393e-28 -2.87816050e-28 1.79119454e-28
-2.84588645e-28 2.90763602e-28 -3.38953643e-28 -3.35192731e-28
-2.62987429e-28 -3.10876600e-28 3.13119841e-28 3.25839295e-28
-2.77855075e-28 3.09139060e-28 2.99660816e-28 2.85167667e-28
-2.75530248e-28 -3.56770417e-28 2.01980511e-28 3.23116555e-28
-3.70571356e-28 3.36635177e-28]
Best Score: 2.744736165706468e-54
```

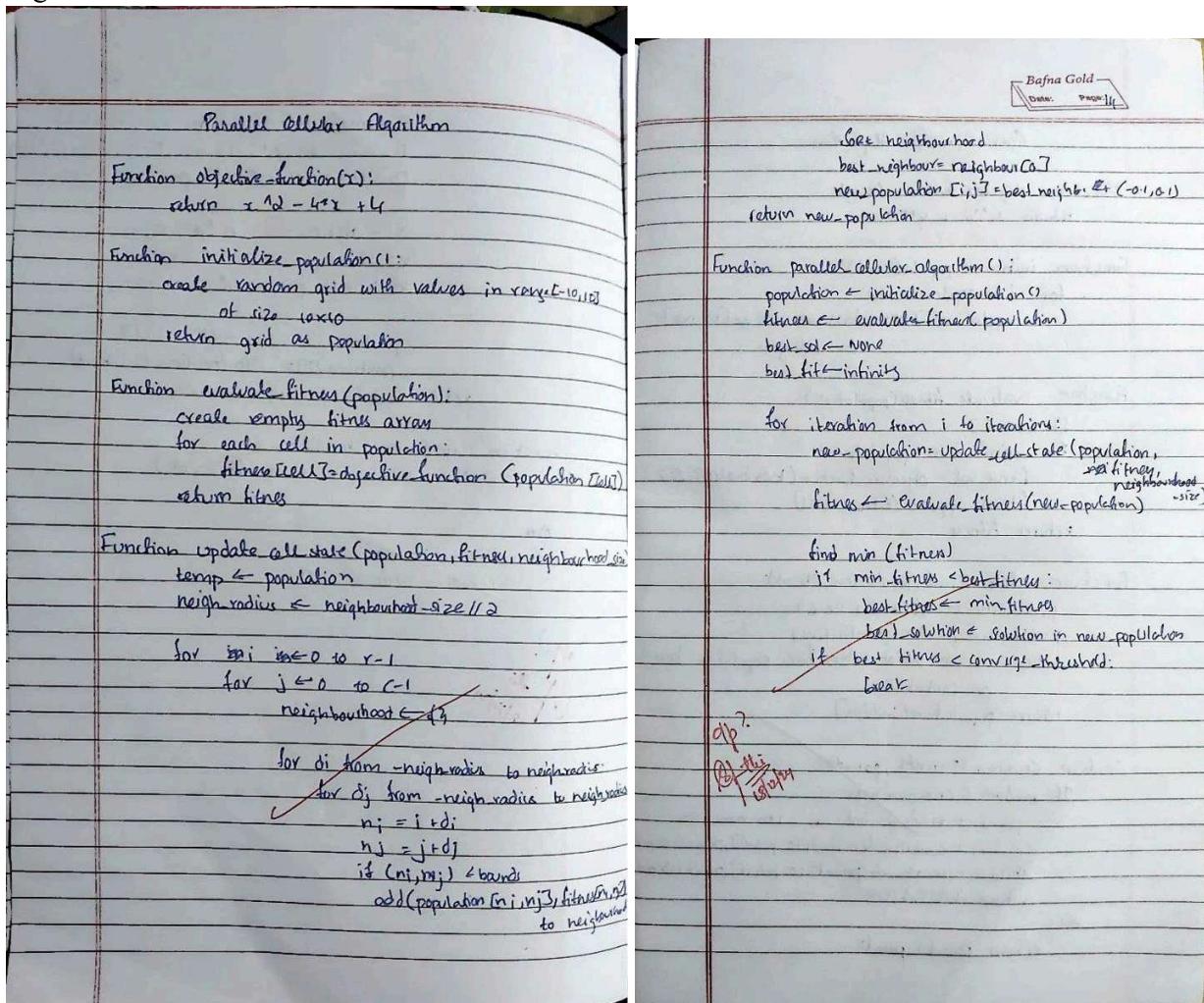
## Program 6

Problem statement

Parallel Cellular Algorithms and Programs:

Parallel Cellular Algorithms are inspired by the functioning of biological cells that operate in a highly parallel and distributed manner. These algorithms leverage the principles of cellular automata and parallel computing to solve complex optimization problems efficiently. Each cell represents a potential solution and interacts with its neighbors to update its state based on predefined rules. This interaction models the diffusion of information across the cellular grid, enabling the algorithm to explore the search space effectively. Parallel Cellular Algorithms are particularly suitable for large-scale optimization problems and can be implemented on parallel computing architectures for enhanced performance.

Algorithm:



Code:

```
import numpy as np
```

```

import random

# Step 1: Define the optimization function (Example: minimizing the function f(x) = x^2)
def objective_function(x):
    return x ** 2 - 4*x+4

# Step 2: Initialize parameters
num_cells = 100      # Number of cells (solutions)
grid_size = (10, 10)   # Grid size (10x10)
iterations = 1000      # Number of iterations
neighborhood_size = 3  # Neighborhood size (3x3)
convergence_threshold = 0.000001 # Convergence threshold

# Step 3: Initialize the population (randomly generate cell positions)
def initialize_population():
    # Create a grid with random positions for each cell in the search space [-10, 10]
    population = np.random.uniform(-10, 10, size=(grid_size[0], grid_size[1]))
    return population

# Step 4: Evaluate the fitness of each cell
def evaluate_fitness(population):
    # Apply the objective function to each cell
    fitness = np.vectorize(objective_function)(population)
    return fitness

# Step 5: Define a function to update the state of each cell based on neighboring cells
def update_cell_state(population, fitness, neighborhood_size):
    rows, cols = population.shape
    new_population = population.copy()

    # Define the neighborhood boundaries
    neighborhood_radius = neighborhood_size // 2

    for i in range(rows):
        for j in range(cols):
            # List of neighboring cell positions, including the current cell
            neighborhood = []
            for di in range(-neighborhood_radius, neighborhood_radius + 1):
                for dj in range(-neighborhood_radius, neighborhood_radius + 1):
                    ni, nj = i + di, j + dj
                    if 0 <= ni < rows and 0 <= nj < cols: # Ensure indices are within bounds
                        neighborhood.append((population[ni, nj], fitness[ni, nj]))

            # Sort neighbors based on fitness value (ascending order: better solutions have lower fitness)
            neighborhood.sort(key=lambda x: x[1])
            best_neighbor = neighborhood[0]

            # Update the current cell based on the best neighbor (with some random fluctuation)
            new_population[i, j] = best_neighbor[0] + random.uniform(-0.1, 0.1) # Slight random movement
    return new_population

# Step 6: Iterate to update the states of the cells
def parallel_cellular_algorithm():

```

```

population = initialize_population()
fitness = evaluate_fitness(population)

best_solution = None
best_fitness = float('inf')

for iteration in range(iterations):
    print(f"Iteration {iteration + 1}/{iterations}")

    # Update cell states in parallel (Here we simulate parallel updates by using numpy)
    new_population = update_cell_state(population, fitness, neighborhood_size)

    # Evaluate the new population's fitness
    fitness = evaluate_fitness(new_population)

    # Track the best solution found so far
    min_fitness_index = np.argmin(fitness)
    min_fitness_value = fitness.flatten()[min_fitness_index]

    if min_fitness_value < best_fitness:
        best_fitness = min_fitness_value
        best_solution = new_population.flatten()[min_fitness_index]

    population = new_population # Update population for next iteration

    # Check for convergence (early stop if we find a very small fitness value)
    if best_fitness < convergence_threshold:
        print("Convergence reached!")
        break

return best_solution, best_fitness

# Step 7: Run the algorithm and output the best solution
best_solution, best_fitness = parallel_cellular_algorithm()

print(f"The best solution found is: {best_solution}")
print(f"The corresponding fitness (objective function value) is: {best_fitness}")

```

```

Iteration 1/1000
Iteration 2/1000
Iteration 3/1000
Convergence reached!
The best solution found is: 1.9995331188038894
The corresponding fitness (objective function value) is: 2.1797805116463564e-07

```

## Program 7

### Problem statement

Optimization via Gene Expression Algorithms:

Gene Expression Algorithms (GEA) are inspired by the biological process of gene expression in living organisms. This process involves the translation of genetic information encoded in DNA into functional proteins. In GEA, solutions to optimization problems are encoded in a manner similar to genetic sequences. The algorithm evolves these solutions through selection, crossover, mutation, and gene expression to find optimal or near-optimal solutions. GEA is effective for solving complex optimization problems in various domains, including engineering, data analysis, and machine learning.

Algorithm:

The image shows two pages of handwritten pseudocode for a Gene Expression Algorithm (GEA). The left page contains the main pseudocode, and the right page contains a detailed implementation of the mutation function.

**Gene Expression Algorithm**

```

Function objective_function(x, y):
    return  $x^{1/2} + y^{1/2}$ 

Function initialize_population():
    for i in population_size:
        population[i] ← random val in range [bounds]
        for each gen

Function evaluate_fitness(population):
    fitness ← []
    for individual in population:
        fitness_val = objective_function(individual[0], individual[1])
        fitness.append(fitness_val)
    return fitness

Function select_bounds(population, fitness):
    probabilities ← 1/(fitness + 1e-6)
    probabilities / = sum(probabilities)
    indices = random set of indices from population based
    on probabilities
    return population[indices]

Function Crossover(parent1, parent2):
    If random < crossover_rate:
        point ← random int in 1 to num_genes
        child1 = concatenate(parent1[0:point], parent2[point])
        child2 = concatenate(parent2[0:point], parent1[point])
    else:
        return parent1, parent2
    return child1, child2
  
```

**Function mutate(individual):**

```

for i ← 0 to num_genes:
    if random() < mutation_rate:
        individual[i] = individual[i] + Random(-1, 1)
        individual[i] = clip(individual[i], bounds)
    return individual
  
```

**Function gene\_expression\_algorithm():**

```

population = initialize_population()
best_solution ← NULL
best_fitness ← INFINITY

For generations from 1 to num_generations:
    fitness = evaluate_fitness(population)

    if min(fitness) < best_fitness:
        best_fitness = min(fitness)
        best_solution = population(fitness)

    parents = select_parents(population, fitness)

    offspring ← []

    for i ← 0 to population_size with step size - 2
        parent1 = parents[i]
        parent2 = parents[i+1]
        child1, child2 = crossover(parent1, parent2)
        offspring.append(mutate(child1))
        offspring.append(mutate(child2))

    return best_solution, best_fitness
  
```

Bafna Gold  
Date: Page 16

(S) 10/10/21

Code:

```

import numpy as np

# Problem definition
def objective_function(x, y):
    return x**2 + y**2 # Example function to minimize

# Initialize parameters
population_size = 100
num_genes = 2 # For (x, y) problem
mutation_rate = 0.1
crossover_rate = 0.7
num_generations = 50
gene_bounds = (-10, 10) # Range for each gene (x, y)

# Helper functions
def initialize_population():
    return np.random.uniform(gene_bounds[0], gene_bounds[1], (population_size, num_genes))

def evaluate_fitness(population):
    return np.array([objective_function(ind[0], ind[1]) for ind in population])

def select_parents(population, fitness):
    probabilities = 1 / (fitness + 1e-6) # Convert fitness to probabilities
    probabilities /= probabilities.sum()
    indices = np.random.choice(np.arange(population_size), size=population_size, p=probabilities)
    return population[indices]

def crossover(parent1, parent2):
    if np.random.rand() < crossover_rate:
        point = np.random.randint(1, num_genes)
        child1 = np.concatenate((parent1[:point], parent2[point:]))
        child2 = np.concatenate((parent2[:point], parent1[point:]))
    return child1, child2
    return parent1, parent2

def mutate(individual):
    for i in range(num_genes):
        if np.random.rand() < mutation_rate:
            individual[i] += np.random.uniform(-1, 1)
            individual[i] = np.clip(individual[i], gene_bounds[0], gene_bounds[1])
    return individual

# Main GEA process
def gene_expression_algorithm():
    population = initialize_population()
    best_solution = None
    best_fitness = float('inf')

    for generation in range(num_generations):
        fitness = evaluate_fitness(population)
        if fitness.min() < best_fitness:
            best_fitness = fitness.min()
            best_solution = population[fitness.argmin()]

```

```

parents = select_parents(population, fitness)
offspring = []

for i in range(0, population_size, 2):
    parent1, parent2 = parents[i], parents[i + 1]
    child1, child2 = crossover(parent1, parent2)
    offspring.append(mutate(child1))
    offspring.append(mutate(child2))

population = np.array(offspring)

print(f"Generation {generation + 1}: Best Fitness = {best_fitness:.5f}, Best Solution = {best_solution}")

return best_solution, best_fitness

# Run the algorithm
best_solution, best_fitness = gene_expression_algorithm()
print("\nBest Solution Found:")
print(f"Solution: {best_solution}, Fitness: {best_fitness:.5f}")

Generation 9: Best Fitness = 0.00282, Best Solution = [-0.05287625 -0.00484865]
Generation 10: Best Fitness = 0.00282, Best Solution = [-0.05287625 -0.00484865]
Generation 11: Best Fitness = 0.00282, Best Solution = [-0.05287625 -0.00484865]
Generation 12: Best Fitness = 0.00282, Best Solution = [-0.05287625 -0.00484865]
Generation 13: Best Fitness = 0.00043, Best Solution = [-0.02010828 -0.00484865]
Generation 14: Best Fitness = 0.00043, Best Solution = [-0.02010828 -0.00484865]
Generation 15: Best Fitness = 0.00043, Best Solution = [-0.02010828 -0.00484865]
Generation 16: Best Fitness = 0.00008, Best Solution = [ 0.00727875 -0.00484865]
Generation 17: Best Fitness = 0.00008, Best Solution = [ 0.00727875 -0.00484865]
Generation 18: Best Fitness = 0.00008, Best Solution = [ 0.00727875 -0.00484865]
Generation 19: Best Fitness = 0.00008, Best Solution = [ 0.00727875 -0.00484865]
Generation 20: Best Fitness = 0.00008, Best Solution = [ 0.00727875 -0.00484865]
Generation 21: Best Fitness = 0.00008, Best Solution = [ 0.00727875 -0.00484865]
Generation 22: Best Fitness = 0.00008, Best Solution = [ 0.00727875 -0.00484865]
Generation 23: Best Fitness = 0.00008, Best Solution = [ 0.00727875 -0.00484865]
Generation 24: Best Fitness = 0.00008, Best Solution = [ 0.00727875 -0.00484865]
Generation 25: Best Fitness = 0.00008, Best Solution = [ 0.00727875 -0.00484865]
Generation 26: Best Fitness = 0.00008, Best Solution = [ 0.00727875 -0.00484865]
Generation 27: Best Fitness = 0.00007, Best Solution = [ 0.00727875 0.0046719 ]
Generation 28: Best Fitness = 0.00007, Best Solution = [ 0.00727875 0.0046719 ]
Generation 29: Best Fitness = 0.00007, Best Solution = [ 0.00727875 0.0046719 ]
Generation 30: Best Fitness = 0.00007, Best Solution = [ 0.00727875 0.0046719 ]
Generation 31: Best Fitness = 0.00007, Best Solution = [ 0.00727875 0.0046719 ]
Generation 32: Best Fitness = 0.00007, Best Solution = [ 0.00727875 0.0046719 ]
Generation 33: Best Fitness = 0.00007, Best Solution = [ 0.00727875 0.0046719 ]
Generation 34: Best Fitness = 0.00007, Best Solution = [ 0.00727875 0.0046719 ]
Generation 35: Best Fitness = 0.00007, Best Solution = [ 0.00727875 0.0046719 ]
Generation 36: Best Fitness = 0.00007, Best Solution = [ 0.00727875 0.0046719 ]
Generation 37: Best Fitness = 0.00007, Best Solution = [ 0.00727875 0.0046719 ]
Generation 38: Best Fitness = 0.00006, Best Solution = [ 0.00727875 -0.00304049]
Generation 39: Best Fitness = 0.00006, Best Solution = [ 0.00727875 -0.00304049]
Generation 40: Best Fitness = 0.00006, Best Solution = [ 0.00727875 -0.00304049]
Generation 41: Best Fitness = 0.00006, Best Solution = [ 0.00727875 -0.00304049]
Generation 42: Best Fitness = 0.00006, Best Solution = [ 0.00727875 -0.00304049]
Generation 43: Best Fitness = 0.00006, Best Solution = [ 0.00727875 -0.00304049]
Generation 44: Best Fitness = 0.00006, Best Solution = [ 0.00727875 -0.00304049]
Generation 45: Best Fitness = 0.00006, Best Solution = [-0.0056377 -0.00484865]
Generation 46: Best Fitness = 0.00006, Best Solution = [-0.0056377 -0.00484865]
Generation 47: Best Fitness = 0.00006, Best Solution = [-0.0056377 -0.00484865]
Generation 48: Best Fitness = 0.00006, Best Solution = [-0.0056377 -0.00484865]
Generation 49: Best Fitness = 0.00006, Best Solution = [-0.0056377 -0.00484865]
Generation 50: Best Fitness = 0.00004, Best Solution = [-0.0056377 -0.00304049]

Best Solution Found:
Solution: [-0.0056377 -0.00304049], Fitness: 0.00004

```

