Subject/Odd Sem 2023-23/Experiment 1

Name : Shreya Singh	Class/Roll No. : D16AD/55	Grade:
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Title of Experiment: Multilayer Perceptron Algorithm.

Objective of Experiment: Implementation of basic neural network models

Outcome of Experiment : Enabling the model to learn the non-linear relationship between inputs and outputs, providing correct XOR gate behavior

Problem Statement : Multilayer Perceptron algorithm to Simulate XOR Gate.

Theory: The XOR gate is a logical gate that takes two binary inputs (0 or 1) and outputs 1 if exactly one of the inputs is 1, and 0 otherwise. Here is the truth table for the XOR gate:

x1	x2	у
0	0	0
0	1	1
1	0	1
1	1	0

$$XOR(\boldsymbol{x_1}, \boldsymbol{x_2}) = AND(NOT(AND(\boldsymbol{x_1}, \boldsymbol{x_2})), OR(\boldsymbol{x_1}, \boldsymbol{x_2}))$$

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The XOR gate is interesting because it is not linearly separable, meaning we cannot draw a straight line to separate the inputs that yield output 0 from those that yield output 1. This nonlinearity makes it a good example to demonstrate the capabilities of a Multilayer Perceptron.

A Multilayer Perceptron is a type of artificial neural network that consists of multiple layers of interconnected nodes (neurons). The first layer is the input layer, the last layer is the output layer, and any layers in between are called hidden layers. Each connection between nodes has an associated weight, and each node has an activation function that determines its output based on the weighted sum of its inputs.

Designing the Perceptron Network:

Step1: Now for the corresponding weight vector w:(w1,w2) of the input vector x:(x1,x2) to the AND and OR node,the associated Perceptron Function can be defined as:

For the AND node:
$$\hat{m{y}}_1=\Theta\left(w_1x_1+w_2x_2+b_{
m AND}
ight)$$
 For the OR node: $\hat{m{y}}_{m{2}}=\Theta\left(w_1x_1+w_2x_2+b_{
m OR}
ight)$

Step2:

$$oldsymbol{\hat{y}_3} = \Theta\left(w_{ ext{NOT}}oldsymbol{\hat{y}_1} + b_{ ext{NOT}}
ight)$$

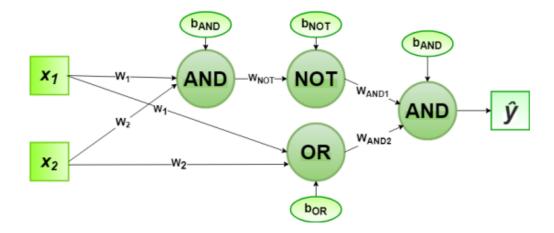


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Step3: The output (\hat{y}_2) from the OR node and the output (\hat{y}_3) from the NOT node as mentioned in Step2 will be inputted to the AND node with weight (w_{AND1}, w_{AND2}) . Then the corresponding output (\hat{y}) is the final output of the XOR logic function. The associated Perceptron Function can be defined as:

$$oldsymbol{\hat{y}} = \Theta\left(w_{ ext{AND1}} oldsymbol{\hat{y}_3} + w_{ ext{AND2}} oldsymbol{\hat{y}_2} + b_{ ext{AND}}
ight)$$

Flowchart



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Program:

```
[1] # importing Python library
import numpy as np

[2] # define Unit Step Function
def Activation(v):
    if v >= 0:
        return 1
    else:
        return 0

[3] # design Perceptron Model
def perceptronModel(x, w, b):
    v = np.dot(w, x) + b
    y = Activation(v)
    return y
```

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```
# NOT Logic Function
 \# wNOT = -1, bNOT = 0.5
 def NOT logicFunction(x):
  WNOT = -1
   bNOT = 0.5
   return perceptronModel(x, wNOT, bNOT)
 # AND Logic Function
 # here w1 = wAND1 = 1,
 \# w2 = wAND2 = 1, bAND = -1.5
 def AND logicFunction(x):
  W = np.array([1, 1])
   bAND = -1.5
   return perceptronModel(x, w, bAND)
 # OR Logic Function
 # w1 = 1, w2 = 1, b0R = -0.5
 def OR logicFunction(x):
  W = np.array([1, 1])
   b0R = -0.5
   return perceptronModel(x, w, bOR)
```

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```
√ [5] # XOR Logic Function
        # with AND, OR and NOT
        # function calls in sequence
        def XOR logicFunction(x):
          y1 = AND_logicFunction(x)
          y2 = 0R logicFunction(x)
          y3 = NOT_logicFunction(y1)
          final_x = np.array([y2, y3])
          finalOutput = AND logicFunction(final x)
          return finalOutput
_{0\mathrm{s}}^{\checkmark} [6] # testing the Perceptron Model
        test1 = np.array([0, 1])
        test2 = np.array([1, 1])
        test3 = np.array([0, 0])
        test4 = np.array([1, 0])
        print("XOR({}, {}) = {}".format(0, 1, XOR_logicFunction(test1)))
        print("XOR({}, {}) = {}".format(1, 1, XOR logicFunction(test2)))
        print("XOR({}, {}) = {}".format(0, 0, XOR_logicFunction(test3)))
        print("XOR({}, {}) = {}".format(1, 0, XOR logicFunction(test4)))
        XOR(0, 1) = 1
        XOR(1, 1) = 0
        XOR(\emptyset, \emptyset) = \emptyset
        XOR(1, 0) = 1
```

Results and Discussions:

We have implemented a basic neural network model, Multilayer Perceptron and have understood the working of the Multilayer Perceptron Algorithm by stimulating XOR Gate.