

VISVESVARAYA TECHNOLOGICAL UNIVERSITY

“JnanaSangama”, Belgaum -590014, Karnataka.



LAB RECORD

Bio Inspired Systems (23CS5BSBIS)

Submitted by

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in partial fulfillment for the award of the degree of

BACHELOR OF ENGINEERING
in
COMPUTER SCIENCE AND ENGINEERING



B.M.S. COLLEGE OF ENGINEERING

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**B.M.S. College of Engineering,
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Department of Computer Science and Engineering



CERTIFICATE

This is to certify that the Lab work entitled “ Bio Inspired Systems (23CS5BSBIS)” carried out by **Shreyas T S (1BM23CS322)**, who is bonafide student of **B.M.S. College of Engineering**. It is in partial fulfillment for the award of **Bachelor of Engineering in Computer Science and Engineering** of the Visvesvaraya Technological University, Belgaum. The Lab report has been approved as it satisfies the academic requirements of the above mentioned subject and the work prescribed for the said degree.

| | |
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Github Link:

<https://github.com/Shreyes45/BIS-lab>

Program 1

Genetic Algorithm for Optimization Problems

The image is a collage of handwritten notes and diagrams, likely from a lecture or study session, focused on Genetic Algorithms (GA) and their applications. The notes are organized into several sections:

- Genetic Algorithm:** A flowchart showing the process: Selection → Encoding techniques (0 to 31) → Selecting the initial population → Selection -> Mating Pool (Individuals with fitness values) → Selection -> crossover (parents) → crossover (parents, crossover point = Random Number In Range(0,1)) → Child1 = crossover_point * Parent1 + (1 - crossover_point) * Parent2 → Child2 = crossover_point * Parent2 + (1 - crossover_point) * Parent1 → return Child1, Child2.
- Selection:** A table showing the initial population and their fitness values. The population consists of binary strings of length 5. The first column is the index (No), the second is the binary string, the third is the value, and the fourth is the fitness (f(x)).

| No | Initial population | Value | Fitness |
|----|--------------------|-------|---------|
| 1 | 10110 | 19 | 0.64 |
| 2 | 11001 | 85 | 0.65 |
| 3 | 00101 | 5 | 0.016 |
| 4 | 10011 | 19 | 0.3125 |
- Crossover:** A diagram showing the crossover operation. It shows two parents (Child1 and Child2) and their respective crossover points. Child1 is created by taking the first part of Parent1 up to the crossover point and the rest from Parent2. Child2 is created by taking the first part of Parent2 up to the crossover point and the rest from Parent1.
- Mutation:** A table showing mutation rates for each bit position. The columns are bit position (0 to 4), probability (0.001 to 0.0001), and mutation value (0 to 1).

| bit no | probability | mutation value |
|--------|-------------|----------------|
| 0 | 0.001 | 0.000 |
| 1 | 0.001 | 0.000 |
| 2 | 0.001 | 0.000 |
| 3 | 0.001 | 0.000 |
| 4 | 0.001 | 0.000 |
- Pseudo code:**

```
function Parent(x)
    Return x[0]
```

```
function generate_population(pop_size, lower_bound, upper_bound)
    population = []
    for i from 1 to pop_size:
        individual = Random Number in Range(lower_bound, upper_bound)
        Add individual to population
    return population
```

```
function Select_population(population):
    fitneess_value = 0
    for each individual in population:
        fitneess_value += individual.fitness
    total_fitness = sum(fitneess_value)
    selection_prob = []
    for each fitneess_value in fitness_values:
        selection_prob.append(fitneess_value / total_fitness)
    return selection_prob
```

```
selection_prob = []
for each fitneess_value in fitness_values:
    selection_prob.append(fitneess_value / total_fitness)
```

```
selection_prob.append(Ptneess_value / total_fitness)
```
- Assistant Professor:** Department of CSE, BMSCE
- Professor & HOD:** Department of CSE
- Applications:** Traveling Salesman problem, Knapsack problem, Function optimization.

Code:

```
import random

def fitness_function(x):
    return x ** 2

def decode(chromosome):
    return int(chromosome, 2)

def evaluate_population(population):
    return [fitness_function(decode(individual)) for individual in population]

def select(population, fitnesses):
    total_fitness = sum(fitnesses)
    if total_fitness == 0:
        return random.choice(population)
    pick = random.uniform(0, total_fitness)
    current = 0
    for individual, fitness in zip(population, fitnesses):
        current += fitness
        if current > pick:
            return individual

def crossover(parent1, parent2):
    if random.random() < CROSSOVER_RATE:
        point = random.randint(1, CHROMOSOME_LENGTH - 1)
        return (parent1[:point] + parent2[point:], parent2[:point] + parent1[point:])
    return parent1, parent2

def mutate(chromosome):
    new_chromosome = ""
    for bit in chromosome:
        if random.random() < MUTATION_RATE:
            new_chromosome += '0' if bit == '1' else '1'
        else:
            new_chromosome += bit
    return new_chromosome

def get_initial_population(size, length):
    population = []
    print(f'Enter {size} chromosomes (each of {length} bits, e.g., "10101")')
    while len(population) < size:
        chrom = input(f'Chromosome {len(population)+1}: ').strip()
        if len(chrom) == length and all(bit in '01' for bit in chrom):
            population.append(chrom)
        else:
            print(f'Invalid input. Please enter a {length}-bit binary string.')
    return population
```

```

def genetic_algorithm():
    population = get_initial_population(POPULATION_SIZE, CHROMOSOME_LENGTH)
    best_solution = None
    best_fitness = float('-inf')

    for generation in range(GENERATIONS):
        fitnesses = evaluate_population(population)

        for i, individual in enumerate(population):
            if fitnesses[i] > best_fitness:
                best_fitness = fitnesses[i]
                best_solution = individual

        print(f"Generation {generation + 1}: Best Fitness = {best_fitness}, Best x = {decode(best_solution)}")

        new_population = []
        while len(new_population) < POPULATION_SIZE:
            parent1 = select(population, fitnesses)
            parent2 = select(population, fitnesses)
            offspring1, offspring2 = crossover(parent1, parent2)
            offspring1 = mutate(offspring1)
            offspring2 = mutate(offspring2)
            new_population.extend([offspring1, offspring2])

        population = new_population[:POPULATION_SIZE]

    print("\nBest solution found:")
    print(f"Chromosome: {best_solution}")
    print(f"x = {decode(best_solution)}")
    print(f"f(x) = {fitness_function(decode(best_solution))}")

POPULATION_SIZE = 4
CHROMOSOME_LENGTH = 5
MUTATION_RATE = 0.01
CROSSOVER_RATE = 0.8
GENERATIONS = 20

if __name__ == "__main__":
    genetic_algorithm()

```

Program 2

Particle Swarm Optimization for Function Optimization

Lab-9
Particle Swarm Optimization

PseudoCode

- 1) P: Particle initialization
- 2) for p=1 to max
- 3) for each particle p in P do
 - a) $p_p = f(p)$
 - b) if p_p is better than $f(pbest)$
 $pbest = p^*$
- 4) end
- 5) cnt
- 6) if $pbest = best$ p in P
- 7) for each particle p in P do
 - a) $U_i^{t+1} = U_i^t + C_1 U_i^t (Pbest - p_i^t) + C_2 U_i^t (p_j^t - p_i^t)$

inertia
Personal influence
Global influence
- 8) $p_i^{t+1} = p_i^t + U_i^{t+1}$
- 9) print $pbest$, $pbest$, $f(pbest)$
- 10) end

Output:

Iteration 1/20 - Best Fitness = 0.081045
 Iteration 2/20 - Best Fitness = 0.081044
 Iteration 3/20 - Best Fitness = 0.081044
 :
 Iteration 10/20 - Best Fitness = 0.002956
 :
 Iteration 20/20 - Best Fitness = 0.000018

Best Solution found:
 Position: [0.0032145, -0.00208]
 Since: 1.75302 - 0.05

Date _____
 Page _____

Iteration-1

| Iteration-1 | | Position | | Velocity | | Best | |
|-------------|---------|----------|-----|----------|---|------|-----|
| Particle No | Initial | x | y | x | y | x | y |
| P1 | 1 | 1 | 1 | 0 | 0 | 1000 | 2 |
| P2 | -1 | -1 | -1 | 0 | 0 | 1000 | 2 |
| P3 | 0.5 | 0.5 | 0.5 | 0 | 0 | 100 | 0.5 |
| P4 | 1 | 1 | 1 | 0.01 | 0 | 100 | 2 |
| P5 | 0.5 | 0.5 | 0.5 | 0.01 | 0 | 100 | 0 |

Iteration-2

| Iteration-2 | | Position | | Velocity | | Best | | | | |
|-------------|---------|----------|-----|----------|-------|-------|------|------|------|---|
| Particle No | Initial | x | y | x | y | x | y | | | |
| P1 | 1 | 1 | 1 | -0.35 | 0.35 | 2 | 1 | 2 | | |
| P2 | -1 | -1 | -1 | 0.35 | -0.35 | 2 | -1 | 2 | | |
| P3 | 0.5 | 0.5 | 0.5 | -0.35 | 0.35 | 0.5 | 0.5 | 0.5 | | |
| P4 | 1 | 1 | 1 | -0.01 | 0.01 | 1.95 | 2 | 1 | -1 | 3 |
| P5 | 0.5 | 0.5 | 0.5 | 0 | 0 | 0.195 | 0.05 | 0.05 | 0.05 | |

Best position: 2.5 Best = 0.0029502

Code:

```
import numpy as np

def objective_function(x):
    return np.sum(x**2)

num_particles = 30
num_dimensions = 5
max_iter = 15
w = 0.7
c1 = 1.5
c2 = 1.5
x_min = -10
x_max = 10

positions = np.random.uniform(x_min, x_max, (num_particles, num_dimensions))
velocities = np.random.uniform(-1, 1, (num_particles, num_dimensions))
personal_best_positions = positions.copy()
personal_best_scores = np.array([objective_function(x) for x in positions])

global_best_index = np.argmin(personal_best_scores)
global_best_position = personal_best_positions[global_best_index].copy()
global_best_score = personal_best_scores[global_best_index]

for iteration in range(max_iter):
    for i in range(num_particles):
        r1 = np.random.rand(num_dimensions)
        r2 = np.random.rand(num_dimensions)
        velocities[i] = (
            w * velocities[i]
            + c1 * r1 * (personal_best_positions[i] - positions[i])
            + c2 * r2 * (global_best_position - positions[i])
        )
        positions[i] = positions[i] + velocities[i]
        positions[i] = np.clip(positions[i], x_min, x_max)
        fitness = objective_function(positions[i])
        if fitness < personal_best_scores[i]:
            personal_best_scores[i] = fitness
            personal_best_positions[i] = positions[i].copy()
    best_particle_index = np.argmin(personal_best_scores)
    if personal_best_scores[best_particle_index] < global_best_score:
        global_best_score = personal_best_scores[best_particle_index]
        global_best_position = personal_best_positions[best_particle_index].copy()

print("Best Solution Found:", global_best_position)
print("Best Fitness Value:", global_best_score)
```

Program 3

Ant Colony Optimization for the Traveling Salesman Problem

lab-3
Ant colony optimization for Traveling Salesman Problem

Input :-

- Number of ants (num_ants)
- Pheromone importance (alpha)
- pheromone evaporation rate (rho)
- Number of iteration (iterations)
- initial pheromone on all edges

For each iteration from 1 to iterations

- initialize an empty list to store the tour & visited cities
- while there are cities to visit:
- select the next city based on pheromone & heuristic using the probabilities
- calculate probability for each destination
- $P(\text{city}) = (\text{pheromone}^{\alpha}) \cdot (\text{heuristic}^{\beta})$
- normalize probabilities
- choose next city probability
- Add the starting city to start the tour
- Show tour

- update pheromone:

- evaporate pheromone on all edges
- pheromone $(i,j) := (\text{pheromone}(i,j))^{\gamma} \cdot (1 - \rho)$

For each tour in all_tours:

- calculate the tour length
- deposit pheromone along the edges of tour
- $\text{pheromone}(i,j) += 1/tour.length$

Output the best tour & its length after all iterations.

M9
10/10/25

Code:

```
import numpy as np

def ant_colony_optimization(dist_matrix, n_ants, n_iterations, alpha=1, beta=2, rho=0.5, q=100):
    n = len(dist_matrix)
    pheromone = np.ones((n, n))
    visibility = 1 / (dist_matrix + np.eye(n) * 1e10)
    best_length = np.inf
    best_path = None

    for _ in range(n_iterations):
        all_paths = []
        all_lengths = []
        for _ in range(n_ants):
            path = [np.random.randint(n)]
            while len(path) < n:
                i = path[-1]
                prob = (pheromone[i] ** alpha) * (visibility[i] ** beta)
                prob[path] = 0
                prob /= prob.sum()
                next_city = np.random.choice(range(n), p=prob)
                path.append(next_city)
            length = sum(dist_matrix[path[i], path[i+1]] for i in range(n-1)) + dist_matrix[path[-1], path[0]]
            all_paths.append(path)
            all_lengths.append(length)
            if length < best_length:
                best_length = length
                best_path = path
        pheromone *= (1 - rho)
        for path, length in zip(all_paths, all_lengths):
            for i in range(n-1):
                pheromone[path[i], path[i+1]] += q / length
            pheromone[path[-1], path[0]] += q / length
    return best_path, best_length

dist = np.array([
    [0, 2, 9, 10],
    [1, 0, 6, 4],
    [15, 7, 0, 8],
    [6, 3, 12, 0]
])

path, length = ant_colony_optimization(dist, n_ants=10, n_iterations=100)
print("Best path:", path)
print("Best length:", length)
```

Program 4

Cuckoo Search

Date: 19/10/2018
Page: 1

Cuckoo Search (CS):

Cuckoo Search - Job Scheduling:

- Initialize n nests with random job orders.
- Define diversity rate α and $MaxIterations$.
- For $i = 1$ to $MaxIterations$:
 - For each nest j :
 - Generate new schedule using Levy flight.
 - Evaluate Best nest: $\leftarrow \text{TotalCompletionTime}(\text{Schedule}_j)$
 - If fitness new Best.nest.old:
 - Replace nest j with new one.
 - Abandon a fraction p_a of worst nests.
 - Generate new random job orders.
 - Keep the best schedules.
- End for.
- Output the job order with the minimum total completion time.

Output:

Iteration 1, BestFitness (negative total completion time): -162

Iteration 4, BestFitness (negative total completion time): -155

Iteration 5, BestFitness (negative total completion time): -154

Iteration 10, BestFitness (negative total completion time): -156

Best job sequence found: 50 6 3 5 4 1 3
minimum total Completion time: 154

Code:

```
import numpy as np
from scipy.special import gamma # import gamma from scipy.special
```

```
def levy_flight(dim, beta=1.5):
    sigma_u = (gamma(1 + beta) * np.sin(np.pi * beta / 2) /
               gamma((1 + beta) / 2) * beta * np.power(2, (beta - 1) / 2)) ** (1 / beta)
    u = np.random.normal(0, sigma_u, dim)
    v = np.random.normal(0, 1, dim)
```

```

step = u / np.power(np.abs(v), 1 / beta)
return step

def cuckoo_search(objective_function, n, dim, Pa=0.25, MaxGen=100, bounds=(-5, 5)):
    nests = np.random.uniform(bounds[0], bounds[1], (n, dim))
    fitness = np.apply_along_axis(objective_function, 1, nests)
    best_solution = nests[np.argmin(fitness)]
    best_fitness = np.min(fitness)

    for gen in range(MaxGen):
        new_nests = np.copy(nests)
        for i in range(n):
            step = levy_flight(dim)
            new_nests[i] = nests[i] + step
            new_nests[i] = np.clip(new_nests[i], bounds[0], bounds[1])
        new_fitness = np.apply_along_axis(objective_function, 1, new_nests)
        better_nests = new_fitness < fitness
        nests[better_nests] = new_nests[better_nests]
        fitness[better_nests] = new_fitness[better_nests]
        forget_idx = np.random.rand(n) < Pa
        nests[forget_idx] = np.random.uniform(bounds[0], bounds[1], (np.sum(forget_idx), dim))
        fitness = np.apply_along_axis(objective_function, 1, nests)
        current_best_fitness = np.min(fitness)
        if current_best_fitness < best_fitness:
            best_fitness = current_best_fitness
            best_solution = nests[np.argmin(fitness)]
        print(f"Generation {gen + 1}/{MaxGen}, Best Fitness: {best_fitness}")
    return best_solution, best_fitness

def sphere_function(x):
    return np.sum(x**2)

n = 30
dim = 5
MaxGen = 100
Pa = 0.25

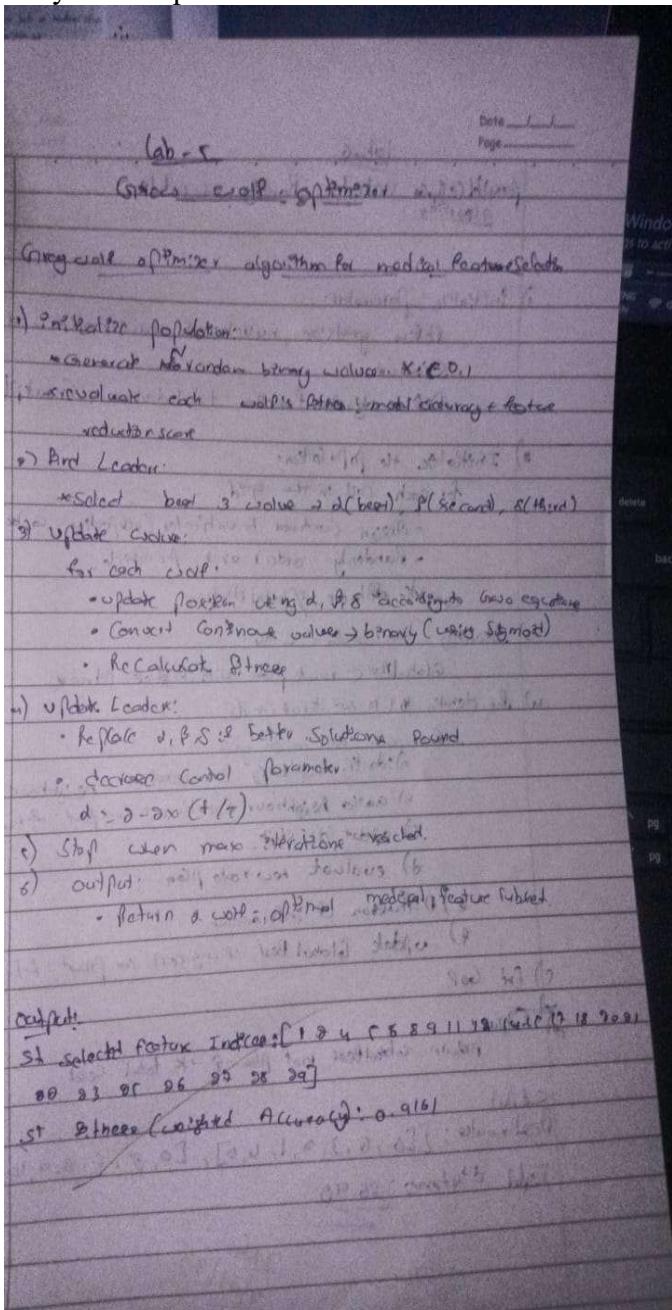
best_solution, best_fitness = cuckoo_search(sphere_function, n, dim, Pa, MaxGen)

print("\nBest Solution Found: ", best_solution)
print("Best Fitness Value: ", best_fitness)

```

Program 5

Grey Wolf Optimizer



Code:

```
import numpy as np

def gwo(objective_function, n, dim, max_gen, lb, ub):
    wolves = np.random.uniform(lb, ub, (n, dim))
    fitness = np.apply_along_axis(objective_function, 1, wolves)
    alpha, beta, delta = np.copy(wolves), np.copy(wolves), np.copy(wolves)
    alpha_f, beta_f, delta_f = np.copy(fitness), np.copy(fitness), np.copy(fitness)

    for gen in range(max_gen):
        sorted_idx = np.argsort(fitness)
        alpha, beta, delta = wolves[sorted_idx[0]], wolves[sorted_idx[1]], wolves[sorted_idx[2]]
        alpha_f, beta_f, delta_f = fitness[sorted_idx[0]], fitness[sorted_idx[1]], fitness[sorted_idx[2]]

        A = 2 * np.random.rand(n, dim) - 1
        C = 2 * np.random.rand(n, dim)
        for i in range(n):
            D_alpha = np.abs(C[i] * alpha - wolves[i])
            D_beta = np.abs(C[i] * beta - wolves[i])
            D_delta = np.abs(C[i] * delta - wolves[i])

            wolves[i] = wolves[i] + A[i] * (D_alpha + D_beta + D_delta) / 3
            wolves[i] = np.clip(wolves[i], lb, ub)

        fitness = np.apply_along_axis(objective_function, 1, wolves)
        print(f"Gen {gen+1}/{max_gen}, Best Fitness: {min(fitness)}")

    return alpha, alpha_f

def sphere_function(x):
    return np.sum(x**2)

n = 30
dim = 5
max_gen = 50
lb, ub = -5, 5

best_solution, best_fitness = gwo(sphere_function, n, dim, max_gen, lb, ub)
print("\nBest Solution Found: ", best_solution)
print("Best Fitness: ", best_fitness)
```

Program 6

Parallel Cellular Algorithm

Job-6
Parallel Cellular Vehicle Routing Problem Solving
Algorithm

1) Initialize parameters:
Define grids' size, number of vehicles, number of customers, and neighborhood structure.
Define objective function - total distance (route plan).

2) Initialize the population:
For each cell in the grid:
- Assign customer to vehicle (nearest, global)
- Randomly assign work for vehicle.
Compute distance > total Distance.

3) Identifying best solution & etc:
Global Best ← route plan with highest fitness

4) For iteration No 1 to no iterations do:
a) Each cell in the grid
 a) Identify neighbouring cell based on neighbourhood structure
 b) Gather neighbour solution & compare fitness
 c) update cell state
 d) evaluate new route plan

e) Diffusion of information:

f) Update Global Best if new cell is found better

5) End loop

Output:
return global best tour (No. of total cost)

Output
Best route: [[0, 6, 3, 9, 1, 4, 0], [0, 8, 5, 3, 9, 10, 0]]
Total distance: 86.90

Code: import numpy as np

```
def total_distance(routes, dist_matrix):
    dist = 0
    for route in routes:
        for i in range(len(route)-1):
            dist += dist_matrix[route[i], route[i+1]]
    return dist

def generate_random_routes(num_customers, num_vehicles):
    customers = np.arange(1, num_customers + 1)
    np.random.shuffle(customers)
    splits = np.array_split(customers, num_vehicles)
    return [[0] + list(s) + [0] for s in splits if len(s) > 0]

def crossover(r1, r2):
    flat1 = np.concatenate([x[1:-1] for x in r1 if len(x)>2]) if r1 else []
    flat2 = np.concatenate([x[1:-1] for x in r2 if len(x)>2]) if r2 else []
    if len(flat1)==0 or len(flat2)==0:
        return r1 if len(flat1)>0 else r2
    point = np.random.randint(1, len(flat1))
    child_seq = list(flat1[:point]) + [x for x in flat2 if x not in flat1[:point]]
    splits = np.array_split(child_seq, 2)
    return [[0]+list(s)+[0] for s in splits if len(s)>0]

def mutate(routes, rate=0.2):
    for route in routes:
        if np.random.rand() < rate and len(route) > 3:
            i, j = np.random.choice(range(1, len(route)-1), 2, replace=False)
            route[i], route[j] = route[j], route[i]
    return routes

def local_optimize(routes, dist_matrix):
    for route in routes:
        improved = True
        while improved:
            improved = False
            for i in range(1, len(route)-2):
                for j in range(i+1, len(route)-1):
                    a, b, c, d = route[i-1], route[i], route[j], route[j+1]
                    before = dist_matrix[a,b]+dist_matrix[c,d]
                    after = dist_matrix[a,c]+dist_matrix[b,d]
                    if after < before:
                        route[i:j+1] = route[i:j+1][::-1]
                        improved = True
    return routes

def create_distance_matrix(num_customers):
    coords = np.random.rand(num_customers + 1, 2) * 20
```

```

return np.sqrt(((coords[:, None, :] - coords[None, :, :]) ** 2).sum(-1))

def parallel_cellular_vrp(num_customers=10, num_vehicles=2, grid_size=(3,3), iterations=50):
    dist_matrix = create_distance_matrix(num_customers)
    grid = np.empty(grid_size, dtype=object)
    fit = np.zeros(grid_size)

    for i in range(grid_size[0]):
        for j in range(grid_size[1]):
            routes = generate_random_routes(num_customers, num_vehicles)
            grid[i,j] = routes
            fit[i,j] = 1 / (1 + total_distance(routes, dist_matrix))

    best = grid[np.unravel_index(np.argmax(fit), fit.shape)]

    for _ in range(iterations):
        new_grid = np.empty_like(grid)
        for i in range(grid_size[0]):
            for j in range(grid_size[1]):
                neighbors = []
                for di in [-1,0,1]:
                    for dj in [-1,0,1]:
                        if di==0 and dj==0: continue
                        ni, nj = (i+di)%grid_size[0], (j+dj)%grid_size[1]
                        neighbors.append(grid[ni,nj])
                best_neighbor = max(neighbors, key=lambda r: 1/(1+total_distance(r, dist_matrix)))
                child = crossover(grid[i,j], best_neighbor)
                child = mutate(child)
                child = local_optimize(child, dist_matrix)
                new_fit = 1 / (1 + total_distance(child, dist_matrix))
                if new_fit > fit[i,j]:
                    new_grid[i,j] = child
                    fit[i,j] = new_fit
                else:
                    new_grid[i,j] = grid[i,j]
        grid = new_grid
        current_best = grid[np.unravel_index(np.argmax(fit), fit.shape)]
        if (1/(1+total_distance(current_best, dist_matrix))) > (1/(1+total_distance(best, dist_matrix))):
            best = current_best

    return best, total_distance(best, dist_matrix)

best_routes, best_cost = parallel_cellular_vrp()
print("Best Routes:", best_routes)
print("Total Distance:", round(best_cost, 2))

```

Program 7

Optimization via Gene Expression Algorithm

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Gene Expression algo

Step 1:
 1) Initialization
 2) Fitness function
 3) Selection
 4) Crossover
 5) Mutation
 6) Gene expression
 7) Termination

Step 2: Fitness (x) = $\sum_{i=1}^n x_i$

1) Select ordering technique 0 to 31 on chromosome
 e.g. fixed length with (0, 1, 2, 3, ..., 30)
 2) Initial Population:

| Chromosome | Phenotype | Volume | fitness | Probability |
|------------|-----------|--------|---------|-------------|
| 0 | 110 | 10 | 10.00 | 0.1940 |
| 1 | 111 | 15 | 15.00 | 0.1940 |
| 2 | 112 | 20 | 20.00 | 0.1940 |
| 3 | 113 | 25 | 25.00 | 0.1940 |
| 4 | 114 | 30 | 30.00 | 0.1940 |
| 5 | 115 | 35 | 35.00 | 0.1940 |
| 6 | 116 | 40 | 40.00 | 0.1940 |
| 7 | 117 | 45 | 45.00 | 0.1940 |
| 8 | 118 | 50 | 50.00 | 0.1940 |
| 9 | 119 | 55 | 55.00 | 0.1940 |
| 10 | 120 | 60 | 60.00 | 0.1940 |
| 11 | 121 | 65 | 65.00 | 0.1940 |
| 12 | 122 | 70 | 70.00 | 0.1940 |
| 13 | 123 | 75 | 75.00 | 0.1940 |
| 14 | 124 | 80 | 80.00 | 0.1940 |
| 15 | 125 | 85 | 85.00 | 0.1940 |
| 16 | 126 | 90 | 90.00 | 0.1940 |
| 17 | 127 | 95 | 95.00 | 0.1940 |
| 18 | 128 | 100 | 100.00 | 0.1940 |
| 19 | 129 | 105 | 105.00 | 0.1940 |
| 20 | 130 | 110 | 110.00 | 0.1940 |
| 21 | 131 | 115 | 115.00 | 0.1940 |
| 22 | 132 | 120 | 120.00 | 0.1940 |
| 23 | 133 | 125 | 125.00 | 0.1940 |
| 24 | 134 | 130 | 130.00 | 0.1940 |
| 25 | 135 | 135 | 135.00 | 0.1940 |
| 26 | 136 | 140 | 140.00 | 0.1940 |
| 27 | 137 | 145 | 145.00 | 0.1940 |
| 28 | 138 | 150 | 150.00 | 0.1940 |
| 29 | 139 | 155 | 155.00 | 0.1940 |
| 30 | 140 | 160 | 160.00 | 0.1940 |
| 31 | 141 | 165 | 165.00 | 0.1940 |

$E(x) = 115.5$

Avg = 88.67

max = 165

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1) Selection -> mating pool

| Selected Chromosome | Crossover point | Offspring phenotype | Offspring value |
|---------------------|-----------------|---------------------|-----------------|
| 1 110 | 2 | 111 | 11.94 |
| 2 111 | 1 | 110 | 11.94 |
| 3 112 | 3 | 113 | 12.94 |
| 4 113 | 1 | 112 | 12.94 |

2) Crossover:

| Offspring | Applied mutation | Offspring phenotype | Offspring value |
|-----------|------------------|---------------------|-----------------|
| 1 111 | 112 | 110 | 11.94 |
| 2 110 | 111 | 111 | 11.94 |
| 3 113 | 114 | 112 | 12.94 |
| 4 114 | 113 | 113 | 12.94 |

3) Mutation:

| Offspring | Applied mutation | Offspring phenotype | Offspring value |
|-----------|------------------|---------------------|-----------------|
| 1 111 | 112 | 110 | 11.94 |
| 2 110 | 111 | 111 | 11.94 |
| 3 113 | 114 | 112 | 12.94 |
| 4 114 | 113 | 113 | 12.94 |

4) Selection:

| Offspring | Applied mutation | Offspring phenotype | Offspring value |
|-----------|------------------|---------------------|-----------------|
| 1 111 | 112 | 110 | 11.94 |
| 2 110 | 111 | 111 | 11.94 |
| 3 113 | 114 | 112 | 12.94 |
| 4 114 | 113 | 113 | 12.94 |

5) Gene expression & evolution:

Decide each genotype \rightarrow phenotype
 Calculate fitness

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$E(x) = 88.67$
 Avg = 88.67
 max = 165

1) Iterate until convergence happens (step 24)
 until fitness improvement is negligible/generation limit has reached

Required code (Python):

- Define fitness calculation func.
- Create population
- Define parameters
- Select mating pool (size = 10)
- mutation after mating (size = 2)
- Gene expression and evolution
- print best value

Output:

Genes = [09.53, 29.80, 29.34, 28.54, 16.61, 21.08, 83.13, 30.81, 22.51, 26.38]

$x = 36.37$
 $p(x) = 69.45$

Final output:

Final output: 36.37

Code:

```
import random
import math

def fitness_function(x):
    return x * math.sin(10 * math.pi * x) + 2

POPULATION_SIZE = 6
GENE_LENGTH = 10
MUTATION_RATE = 0.05
CROSSOVER_RATE = 0.8
GENERATIONS = 20
DOMAIN = (-1, 2)

def random_gene():
    return random.uniform(DOMAIN[0], DOMAIN[1])

def create_chromosome():
    return [random_gene() for _ in range(GENE_LENGTH)]

def initialize_population(size):
    return [create_chromosome() for _ in range(size)]

def evaluate_population(population):
    return [fitness_function(express_gene(chrom)) for chrom in population]

def express_gene(chromosome):
    return sum(chromosome) / len(chromosome)

def select(population, fitnesses):
    total_fitness = sum(fitnesses)
    pick = random.uniform(0, total_fitness)
    current = 0
    for individual, fitness in zip(population, fitnesses):
        current += fitness
        if current > pick:
            return individual
    return random.choice(population)

def crossover(parent1, parent2):
    if random.random() < CROSSOVER_RATE:
        point = random.randint(1, GENE_LENGTH - 1)
        child1 = parent1[:point] + parent2[point:]
        child2 = parent2[:point] + parent1[point:]
        return child1, child2
    return parent1[:,], parent2[:]

def mutate(chromosome):
    new_chromosome = []
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for gene in chromosome:
    if random.random() < MUTATION_RATE:
        new_chromosome.append(random_gene())
    else:
        new_chromosome.append(gene)
return new_chromosome

def gene_expression_algorithm():
    population = initialize_population(POPULATION_SIZE)
    best_solution = None
    best_fitness = float("-inf")

    for generation in range(GENERATIONS):
        fitnesses = evaluate_population(population)

        for i, chrom in enumerate(population):
            if fitnesses[i] > best_fitness:
                best_fitness = fitnesses[i]
                best_solution = chrom[:]

        print(f"Generation {generation+1}: Best Fitness = {best_fitness:.4f}, Best x = {express_gene(best_solution):.4f}")

        new_population = []
        while len(new_population) < POPULATION_SIZE:
            parent1 = select(population, fitnesses)
            parent2 = select(population, fitnesses)
            offspring1, offspring2 = crossover(parent1, parent2)
            offspring1 = mutate(offspring1)
            offspring2 = mutate(offspring2)
            new_population.extend([offspring1, offspring2])

        population = new_population[:POPULATION_SIZE]

    print("\nBest solution found:")
    print(f"Genes: {best_solution}")
    x_value = express_gene(best_solution)
    print(f"x = {x_value:.4f}")
    print(f"f(x) = {fitness_function(x_value):.4f}")

if __name__ == "__main__":
    gene_expression_algorithm()

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