

## 数学公式简单示例

## 1. 基本公式:

$$f(x) = 2\sigma + 3$$

## 2. 积分公式:

$$\int_a^b f(x) dx.$$

## 3. 上下标:

$$\sum_{i=1}^n a_i = 0$$
$$f(x) = x^{x^x}$$

## 4. 添加公式标号:

$$\sigma_z = \sqrt{\Sigma(\Delta_z - \langle \Delta_z \rangle)^2 / (N - 1)} \quad (1)$$

## 5. 取消公式标号:

$$\sigma_z = \sqrt{\Sigma(\Delta_z - \langle \Delta_z \rangle)^2 / (N - 1)}$$

## 6. 在公式中插入文本:

对任意的  $x > 0$ , 有  $f(x) > 0$ .

## 7. 分式及开方:

$$y = \frac{m}{n}$$
$$y = \sqrt{\sigma}$$
$$y = \sqrt[n]{\lambda}$$

## 8. 省略号:

$$f(x_1, x_2, \dots, x_n) = x_1^2 + x_2^2 + \dots + x_n^2$$

## 9. 括号和分隔符:

$$f(x, y, z) = 3y^2z \left( 3 + \frac{7x+5}{1+y^2} \right).$$
$$\left. \frac{du}{dx} \right|_{x=0} = 2x$$

## 10. 多行对齐公式:

$$\begin{aligned} \cos 2\theta &= \cos^2 \theta - \sin^2 \theta \\ &= 2 \cos^2 \theta - 1. \end{aligned}$$

$$\cos 2\theta = \cos^2 \theta - \sin^2 \theta \quad (2)$$

$$= 2 \cos^2 \theta - 1. \quad (3)$$

11. 矩阵:

The *characteristic polynomial*  $\chi(\lambda)$  of the  $3 \times 3$  matrix

$$\begin{pmatrix} a & b & c \\ d & e & f \\ g & h & i \end{pmatrix}$$

is given by the formula

$$\chi(\lambda) = \begin{vmatrix} \lambda - a & -b & -c \\ -d & \lambda - e & -f \\ -g & -h & \lambda - i \end{vmatrix}.$$

12、导数、极限、求和、积分 (Derivatives, Limits, Sums and Integrals):

$$\frac{du}{dt} \text{ and } \frac{d^2u}{dx^2}$$

$$\frac{\partial u}{\partial t} = h^2 \left( \frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} + \frac{\partial^2 u}{\partial z^2} \right)$$

$$\lim_{x \rightarrow +\infty}, \inf_{x > s} \text{ and } \sup_K$$

$$\lim_{x \rightarrow 0} \frac{3x^2 + 7x^3}{x^2 + 5x^4} = 3.$$

$$\sum_{k=1}^n k^2 = \frac{1}{2}n(n+1).$$

$$\int_a^b f(x) dx.$$

$$\int_0^{+\infty} x^n e^{-x} dx = n!.$$

$$\int \cos \theta d\theta = \sin \theta.$$

$$\int_{x^2+y^2 \leq R^2} f(x,y) dx dy = \int_{\theta=0}^{2\pi} \int_{r=0}^R f(r \cos \theta, r \sin \theta) r dr d\theta.$$

$$\int_0^R \frac{2x dx}{1+x^2} = \log(1+R^2).$$

One would typeset this in LaTeX by typing In non-relativistic wave mechanics, the wave function  $\psi(\mathbf{r}, t)$  of a particle satisfies the *Schrödinger Wave Equation*

$$i\hbar \frac{\partial \psi}{\partial t} = \frac{-\hbar^2}{2m} \left( \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2} \right) \psi + V\psi.$$

It is customary to normalize the wave equation by demanding that

$$\iiint_{\mathbf{R}^3} |\psi(\mathbf{r}, 0)|^2 dx dy dz = 1.$$

A simple calculation using the Schrödinger wave equation shows that

$$\frac{d}{dt} \iiint_{\mathbf{R}^3} |\psi(\mathbf{r}, t)|^2 dx dy dz = 0,$$

and hence

$$\iiint_{\mathbf{R}^3} |\psi(\mathbf{r}, t)|^2 dx dy dz = 1$$

for all times  $t$ . If we normalize the wave function in this way then, for any (measurable) subset  $V$  of  $\mathbf{R}^3$  and time  $t$ ,

$$\iiint_V |\psi(\mathbf{r}, t)|^2 dx dy dz$$

represents the probability that the particle is to be found within the region  $V$  at time  $t$ .