

Regression analysis

Shrinath Rajeshirke

02/12/2021

#importing libraries

```
library(rlang)
library(tidymodels)

## Registered S3 method overwritten by 'tune':
##   method                from
##   required_pkgs.model_spec parsnip

## -- Attaching packages ----- tidymodels
0.1.4 --

## v broom          0.7.10      v recipes          0.1.17
## v dials          0.0.10      v rsample          0.1.1
## v dplyr          1.0.7       v tibble           3.1.6
## v ggplot2        3.3.5       v tidyr            1.1.4
## v infer          1.0.0       v tune             0.1.6
## v modeldata      0.1.1       v workflows        0.2.4
## v parsnip        0.1.7       v workflowsets     0.1.0
## v purrr          0.3.4       v yardstick        0.0.9

## -- Conflicts -----
tidymodels_conflicts() --
## x purrr::%@%()      masks rlang::%@%()
## x purrr::as_function() masks rlang::as_function()
## x purrr::discard()  masks scales::discard()
## x dplyr::filter()   masks stats::filter()
## x purrr::flatten()  masks rlang::flatten()
## x purrr::flatten_chr() masks rlang::flatten_chr()
## x purrr::flatten_dbl() masks rlang::flatten_dbl()
## x purrr::flatten_int() masks rlang::flatten_int()
## x purrr::flatten_lgl() masks rlang::flatten_lgl()
## x purrr::flatten_raw() masks rlang::flatten_raw()
## x purrr::invoke()   masks rlang::invoke()
## x dplyr::lag()       masks stats::lag()
## x purrr::list_along() masks rlang::list_along()
## x purrr::modify()    masks rlang::modify()
## x purrr::prepend()   masks rlang::prepend()
## x purrr::splice()    masks rlang::splice()
## x recipes::step()    masks stats::step()
## * Dig deeper into tidy modeling with R at https://www.tmw.org

library(tidyverse)
```

```

## -- Attaching packages ----- tidyverse
1.3.1 --

## v readr 2.1.0      v forcats 0.5.1
## v stringr 1.4.0

## -- Conflicts -----
tidyverse_conflicts() --
## x purrr::%@%()      masks rlang::%@%()
## x purrr::as_function() masks rlang::as_function()
## x readr::col_factor() masks scales::col_factor()
## x purrr::discard()   masks scales::discard()
## x dplyr::filter()    masks stats::filter()
## x stringr::fixed()   masks recipes::fixed()
## x purrr::flatten()   masks rlang::flatten()
## x purrr::flatten_chr() masks rlang::flatten_chr()
## x purrr::flatten_dbl() masks rlang::flatten_dbl()
## x purrr::flatten_int() masks rlang::flatten_int()
## x purrr::flatten_lgl() masks rlang::flatten_lgl()
## x purrr::flatten_raw() masks rlang::flatten_raw()
## x purrr::invoke()    masks rlang::invoke()
## x dplyr::lag()       masks stats::lag()
## x purrr::list_along() masks rlang::list_along()
## x purrr::modify()    masks rlang::modify()
## x purrr::prepend()   masks rlang::prepend()
## x readr::spec()      masks yardstick::spec()
## x purrr::splice()    masks rlang::splice()

library(stringr)
library(glmnet)

## Loading required package: Matrix

##
## Attaching package: 'Matrix'

## The following objects are masked from 'package:tidyr':
##
##     expand, pack, unpack

## Loaded glmnet 4.1-3

The `seoul_bike_sharing_converted_normalized.csv` will be our main dataset
which has following variables:

The response variable:

* `RENTED BIKE COUNT` - Count of bikes rented at each hour

Weather predictor variables:

```

```

* `TEMPERATURE` - Temperature in Celsius
* `HUMIDITY` - Unit is `%`
* `WIND_SPEED` - Unit is `m/s`
* `VISIBILITY` - Multiplied by 10m
* `DEW_POINT_TEMPERATURE` - The temperature to which the air would have to
cool down in order to reach saturation, unit is Celsius
* `SOLAR_RADIATION` - MJ/m2
* `RAINFALL` - mm
* `SNOWFALL` - cm

```

Date/time predictor variables:

```

* `DATE` - Year-month-day
* `HOUR` - Hour of the day
* `FUNCTIONAL DAY` - NoFunc(Non Functional Hours), Fun(Functional hours)
* `HOLIDAY` - Holiday/No holiday
* `SEASONS` - Winter, Spring, Summer, Autumn

```

#importing dataset

```

setwd("C:/Users/ASUS/Desktop/Weather Bike project")
bike_sharing_df <- read_csv("seoul_bike_sharing_converted_normalized.csv")

```

```
## Rows: 8465 Columns: 41
```

```
## -- Column specification -----
-----
```

```
## Delimiter: ","
```

```
## chr (2): DATE, FUNCTIONING_DAY
```

```
## dbl (39): RENTED_BIKE_COUNT, TEMPERATURE, HUMIDITY, WIND_SPEED,
VISIBILITY, ...
```

```
##
```

```
## i Use `spec()` to retrieve the full column specification for this data.
## i Specify the column types or set `show_col_types = FALSE` to quiet this
message.
```

```
spec(bike_sharing_df)
```

```
## cols(
##   DATE = col_character(),
##   RENTED_BIKE_COUNT = col_double(),
##   TEMPERATURE = col_double(),
##   HUMIDITY = col_double(),
##   WIND_SPEED = col_double(),
##   VISIBILITY = col_double(),
##   DEW_POINT_TEMPERATURE = col_double(),
##   SOLAR_RADIATION = col_double(),
##   RAINFALL = col_double(),
##   SNOWFALL = col_double(),
##   FUNCTIONING_DAY = col_character(),

```

```
## `0` = col_double(),
## `1` = col_double(),
## `2` = col_double(),
## `3` = col_double(),
## `4` = col_double(),
## `5` = col_double(),
## `6` = col_double(),
## `7` = col_double(),
## `8` = col_double(),
## `9` = col_double(),
## `10` = col_double(),
## `11` = col_double(),
## `12` = col_double(),
## `13` = col_double(),
## `14` = col_double(),
## `15` = col_double(),
## `16` = col_double(),
## `17` = col_double(),
## `18` = col_double(),
## `19` = col_double(),
## `20` = col_double(),
## `21` = col_double(),
## `22` = col_double(),
## `23` = col_double(),
## AUTUMN = col_double(),
## SPRING = col_double(),
## SUMMER = col_double(),
## WINTER = col_double(),
## HOLIDAY = col_double(),
## NO_HOLIDAY = col_double()
## )
```

We won't be using the DATE column, because 'as is', it basically acts like an data entry index. (However, given more time, we could use the DATE colum to create a 'day of week' or 'isWeekend' column, which we might expect has an affect on preferred bike rental times.) We also do not need the FUNCTIONAL DAY column because it only has one distinct value remaining (YES) after missing value processing.

```
bike_sharing_df <- bike_sharing_df %>%
  select(-DATE, -FUNCTIONING_DAY)
```

Split training and testing data

First, we need to split the full dataset into training and testing datasets.

The training dataset will be used for fitting regression models, and the testing dataset will be used to evaluate the trained models.

```
set.seed(1234)
split <- initial_split(bike_sharing_df, prop = 3/4)
```

```
train_data <- training(split)
test_data <- testing(split)
```

Build a linear regression model using weather variables only
weather conditions may affect people's bike renting decisions. Thus, can we predict a city's bike-sharing demand based on its local weather information? Let's try to build a regression model to do that.

Building a linear regression model called `lm_model_weather` using the following variables:

TEMPERATURE - Temperature in Celsius
HUMIDITY - Unit is %
WIND_SPEED - Unit is m/s
VISIBILITY - Multiplied by 10m
DEW_POINT_TEMPERATURE - The temperature to which the air would have to cool down in order to reach saturation, unit is Celsius
SOLAR_RADIATION - MJ/m2
RAINFALL - mm
SNOWFALL - cm

```
lm <- linear_reg()
lm_model_weather <- lm(RENTED_BIKE_COUNT ~ TEMPERATURE + HUMIDITY +
WIND_SPEED + VISIBILITY + DEW_POINT_TEMPERATURE +
SOLAR_RADIATION + RAINFALL + SNOWFALL, train_data)
summary(lm_model_weather)
```

```
##
## Call:
## lm(formula = RENTED_BIKE_COUNT ~ TEMPERATURE + HUMIDITY + WIND_SPEED +
##     VISIBILITY + DEW_POINT_TEMPERATURE + SOLAR_RADIATION + RAINFALL +
##     SNOWFALL, data = train_data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -1348.46  -294.03   -57.28    208.59   2329.78
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)      156.71      58.07   2.699  0.00698 **
## TEMPERATURE     2399.74     261.66   9.171 < 2e-16 ***
## HUMIDITY         -918.38     126.79  -7.243  4.9e-13 ***
## WIND_SPEED        404.47      48.16   8.399 < 2e-16 ***
## VISIBILITY        12.56      24.86   0.505  0.61351
## DEW_POINT_TEMPERATURE -316.92     278.83  -1.137  0.25575
## SOLAR_RADIATION   -444.85      34.69 -12.824 < 2e-16 ***
## RAINFALL         -1764.01     182.65  -9.658 < 2e-16 ***
## SNOWFALL          317.78     131.58   2.415  0.01576 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
##
## Residual standard error: 487.3 on 6339 degrees of freedom
## Multiple R-squared:  0.4303, Adjusted R-squared:  0.4296
## F-statistic: 598.5 on 8 and 6339 DF,  p-value: < 2.2e-16

Building a linear regression model using all variables

lm <- linear_reg()
lm_model_all <- lm(RENTED_BIKE_COUNT ~ ., train_data)
summary(lm_model_all)

##
## Call:
## lm(formula = RENTED_BIKE_COUNT ~ ., data = train_data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -1401.45  -218.96   -7.31   199.53  1780.67
##
## Coefficients: (3 not defined because of singularities)
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    316.008     52.341   6.037 1.65e-09 ***
## TEMPERATURE    782.658    212.129   3.690 0.000227 ***
## HUMIDITY       -886.730     99.492  -8.913 < 2e-16 ***
## WIND_SPEED      31.913     40.275   0.792 0.428169
## VISIBILITY      21.872     20.262   1.079 0.280439
## DEW_POINT_TEMPERATURE  598.387    221.369   2.703 0.006888 **
## SOLAR_RADIATION   276.882     41.466   6.677 2.64e-11 ***
## RAINFALL       -2064.638    143.276 -14.410 < 2e-16 ***
## SNOWFALL        260.973    103.498   2.522 0.011709 *
## `0`            -133.107     33.323  -3.994 6.56e-05 ***
## `1`            -220.655     32.838  -6.719 1.98e-11 ***
## `2`            -341.020     32.910 -10.362 < 2e-16 ***
## `3`            -423.680     33.498 -12.648 < 2e-16 ***
## `4`            -490.101     33.297 -14.719 < 2e-16 ***
## `5`            -466.528     32.826 -14.212 < 2e-16 ***
## `6`            -307.927     32.990  -9.334 < 2e-16 ***
## `7`              2.949     33.207   0.089 0.929246
## `8`            347.169     32.967  10.531 < 2e-16 ***
## `9`           -103.808     33.853  -3.066 0.002175 **
## `10`           -341.327     35.106  -9.723 < 2e-16 ***
## `11`           -351.192     36.879  -9.523 < 2e-16 ***
## `12`           -312.150     37.820  -8.253 < 2e-16 ***
## `13`           -295.163     38.411  -7.684 1.77e-14 ***
## `14`           -296.250     37.268  -7.949 2.21e-15 ***
## `15`           -213.542     36.764  -5.808 6.61e-09 ***
## `16`            -80.680     35.369  -2.281 0.022575 *
## `17`           201.739     34.547   5.839 5.50e-09 ***
## `18`           690.995     33.487  20.634 < 2e-16 ***
## `19`           419.180     33.099  12.664 < 2e-16 ***
```

```

## `20`          328.187      32.827    9.997 < 2e-16 ***
## `21`          342.772      32.918   10.413 < 2e-16 ***
## `22`          238.833      32.723    7.299 3.26e-13 ***
## `23`           NA         NA        NA      NA
## AUTUMN        358.999      20.290   17.694 < 2e-16 ***
## SPRING        191.365      19.362    9.884 < 2e-16 ***
## SUMMER        198.142      29.187    6.789 1.24e-11 ***
## WINTER         NA         NA        NA      NA
## HOLIDAY       -124.424      22.948   -5.422 6.11e-08 ***
## NO_HOLIDAY     NA         NA        NA      NA
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 377.9 on 6312 degrees of freedom
## Multiple R-squared:  0.6589, Adjusted R-squared:  0.657
## F-statistic: 348.4 on 35 and 6312 DF,  p-value: < 2.2e-16

predictions on the testing dataset using both lm_model_weather and
lm_model_all models

pred_weather <- predict(lm_model_weather,test_data)
pred_all <- predict(lm_model_all,test_data)

## Warning in predict.lm(lm_model_all, test_data): prediction from a rank-
deficient
## fit may be misleading

pred_df <-
data.frame(truth=test_data$RENTED_BIKE_COUNT,weather=pred_weather,all=pred_al
l)

rsq_weather <- rsq(pred_df,truth = truth,estimate=weather);rsq_weather

## # A tibble: 1 x 3
##   .metric .estimator .estimate
##   <chr>   <chr>      <dbl>
## 1 rsq     standard      0.439

rsq_all <- rsq(pred_df,truth = truth,estimate=all);rsq_all

## # A tibble: 1 x 3
##   .metric .estimator .estimate
##   <chr>   <chr>      <dbl>
## 1 rsq     standard      0.669

rmse_weather <- rmse(pred_df,truth=truth,estimate=weather);rmse_weather

## # A tibble: 1 x 3
##   .metric .estimator .estimate
##   <chr>   <chr>      <dbl>
## 1 rmse     standard      475.

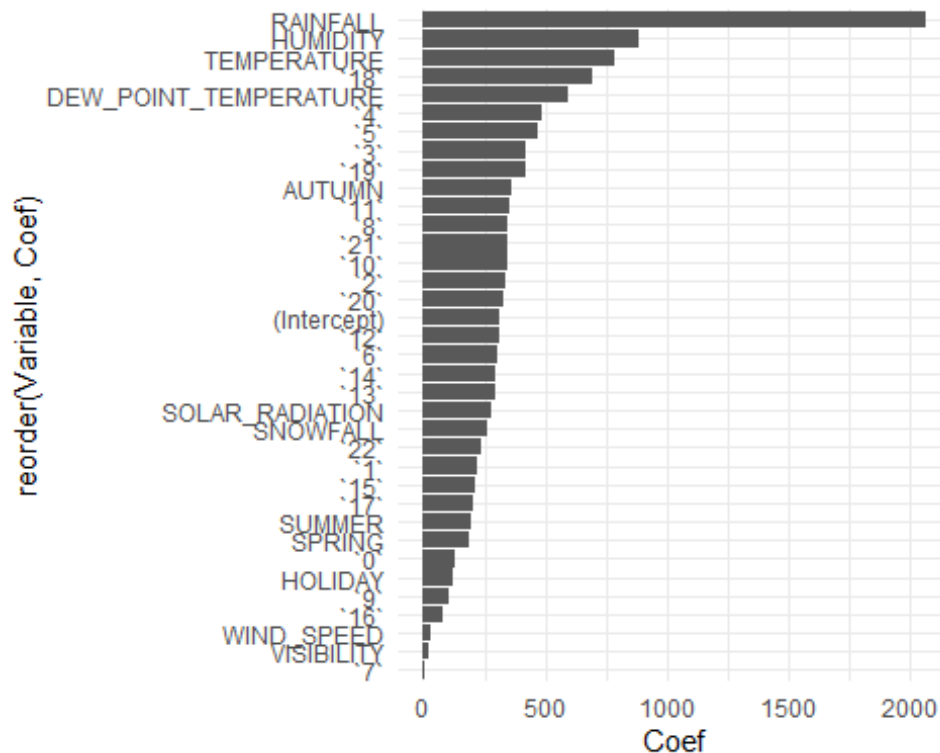
```

```
rmse_all <- rmse(pred_df,truth=truth,estimate=all);rmse_all

## # A tibble: 1 x 3
##   .metric .estimator .estimate
##   <chr>   <chr>       <dbl>
## 1 rmse    standard      364.

abs_cof_df <- stack(abs(lm_model_all$coefficients))
names(abs_cof_df) <- c("Coef", "Variable")
abs_cof_df <- abs_cof_df %>%
  select(Variable, Coef)
coefs_sorted <- arrange(abs_cof_df, -Coef)
coefs_sorted <- na.omit(coefs_sorted)

ggplot(data=coefs_sorted, aes(x= reorder(Variable,Coef),Coef)) +
  geom_bar(stat = "identity") +
  coord_flip() +
  theme_minimal()
```



Define a linear regression model specification.

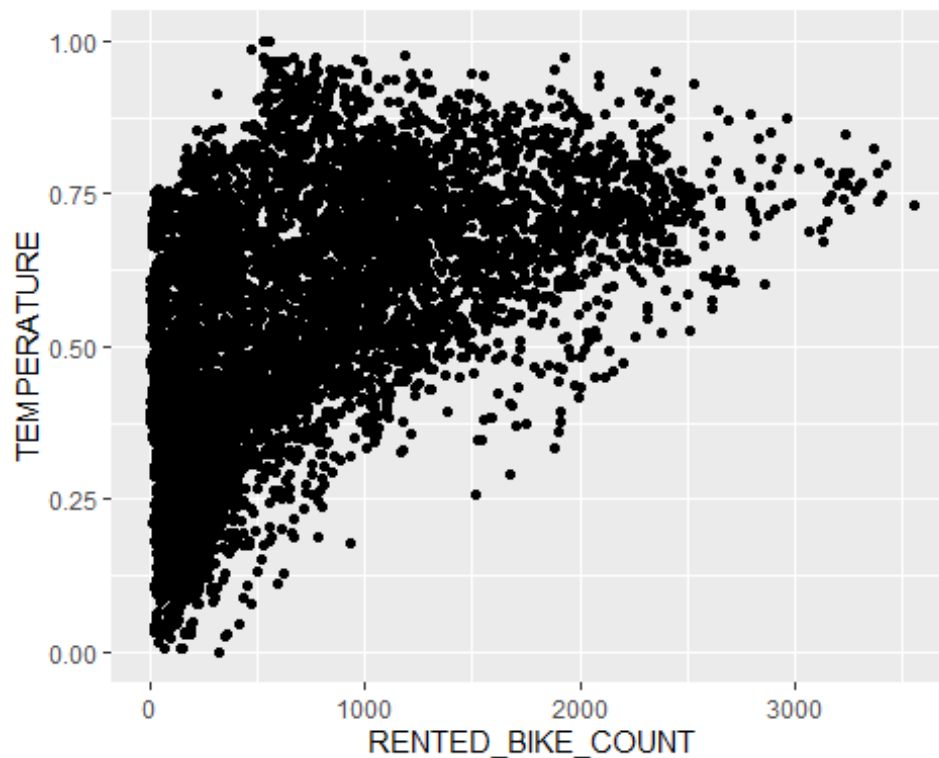
```
lm_spec <- linear_reg() %>%
  set_engine("lm") %>%
  set_mode("regression")
```

Split the data into training and testing datasets.


```
set.seed(1234)
data_split <- initial_split(bike_sharing_df, prop = 4/5)
train_data <- training(data_split)
test_data <- testing(data_split)

scatter plot of RENTED_BIKE_COUNT vs TEMPERATURE

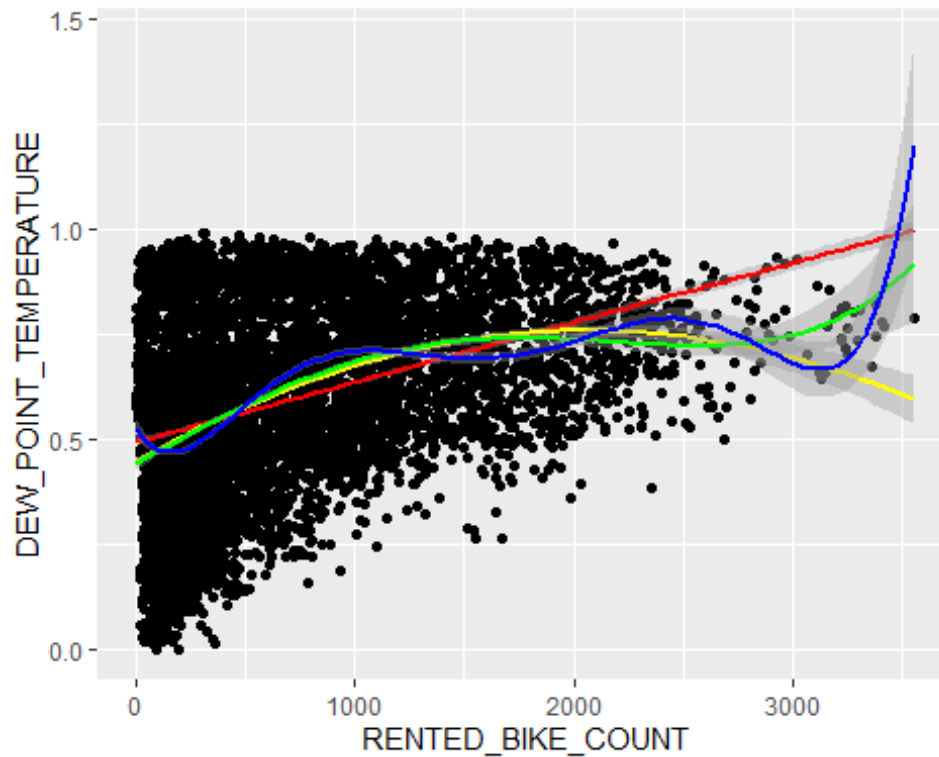
ggplot(data = train_data, aes(RENTED_BIKE_COUNT, TEMPERATURE)) +
  geom_point()
```



correlation between RENTED_BIKE_COUNT and TEMPERATURE does not look like linear

plotting higher order polynomial fits

```
ggplot(data=train_data, aes(RENTED_BIKE_COUNT, TEMPERATURE)) +
  geom_point() +
  geom_smooth(method = "lm", formula = y ~ x, color="red") +
  geom_smooth(method = "lm", formula = y ~ poly(x, 2), color="yellow") +
  geom_smooth(method = "lm", formula = y ~ poly(x, 4), color="green") +
  geom_smooth(method = "lm", formula = y ~ poly(x, 6), color="blue")
```



From above plot, we can see that curve with degree 6 fits good.

Fitting of regression model with popynomial terms

```
lm_poly <- lm(RENTED_BIKE_COUNT ~ . + poly(TEMPERATURE,6) + poly(HUMIDITY,4) +
poly(RAINFALL,4),train_data)
summary(lm_poly)
```

```
##
## Call:
## lm(formula = RENTED_BIKE_COUNT ~ . + poly(TEMPERATURE, 6) + poly(HUMIDITY,
##      4) + poly(RAINFALL, 4), data = train_data)
##
## Residuals:
```

	Min	1Q	Median	3Q	Max
	-1417.15	-207.69	-5.18	188.89	1484.60

```
##
## Coefficients: (6 not defined because of singularities)
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)      -13.91      53.22  -0.261  0.793843
## TEMPERATURE       3365.40     252.96  13.304 < 2e-16 ***
## HUMIDITY           354.62     122.09   2.904  0.003691 **
## WIND_SPEED        -31.96      35.00  -0.913  0.361232
## VISIBILITY        -73.55      18.39  -4.000  6.39e-05 ***
## DEW_POINT_TEMPERATURE -2365.93    274.72  -8.612 < 2e-16 ***
## SOLAR_RADIATION     216.19      36.95   5.851  5.10e-09 ***
## RAINFALL          -1740.24     141.59 -12.291 < 2e-16 ***
```

```

## SNOWFALL          267.65      90.83    2.947 0.003221 **
## `0`              -121.70      28.78   -4.228 2.39e-05 ***
## `1`              -233.54      28.58   -8.170 3.64e-16 ***
## `2`              -341.79      28.64  -11.935 < 2e-16 ***
## `3`              -401.77      29.05  -13.830 < 2e-16 ***
## `4`              -474.47      28.85  -16.444 < 2e-16 ***
## `5`              -448.43      28.51  -15.731 < 2e-16 ***
## `6`              -288.60      28.70  -10.057 < 2e-16 ***
## `7`               20.23      28.80    0.703 0.482320
## `8`              347.71      28.83   12.062 < 2e-16 ***
## `9`              -82.36      29.38   -2.803 0.005078 **
## `10`             -301.76      30.56   -9.874 < 2e-16 ***
## `11`             -285.55      32.27   -8.850 < 2e-16 ***
## `12`             -199.68      33.10   -6.032 1.70e-09 ***
## `13`             -190.17      33.68   -5.646 1.71e-08 ***
## `14`             -168.10      32.58   -5.160 2.54e-07 ***
## `15`             -89.10      32.10   -2.775 0.005529 **
## `16`              43.24      30.92    1.398 0.162033
## `17`             314.45      29.97   10.491 < 2e-16 ***
## `18`             762.01      29.25   26.053 < 2e-16 ***
## `19`             469.12      28.65   16.374 < 2e-16 ***
## `20`             353.67      28.50   12.411 < 2e-16 ***
## `21`             356.48      28.63   12.453 < 2e-16 ***
## `22`             243.42      28.53    8.531 < 2e-16 ***
## `23`              NA         NA      NA      NA
## AUTUMN           376.30      20.71   18.170 < 2e-16 ***
## SPRING           232.01      20.19   11.491 < 2e-16 ***
## SUMMER           262.29      26.21   10.009 < 2e-16 ***
## WINTER           NA         NA      NA      NA
## HOLIDAY          -107.01      20.02   -5.345 9.32e-08 ***
## NO_HOLIDAY       NA         NA      NA      NA
## poly(TEMPERATURE, 6)1 NA         NA      NA      NA
## poly(TEMPERATURE, 6)2 -1729.48    506.38   -3.415 0.000641 ***
## poly(TEMPERATURE, 6)3 -10071.86   356.11  -28.283 < 2e-16 ***
## poly(TEMPERATURE, 6)4 -5281.72   383.68  -13.766 < 2e-16 ***
## poly(TEMPERATURE, 6)5  353.07   347.71    1.015 0.309935
## poly(TEMPERATURE, 6)6 1822.54   354.94    5.135 2.90e-07 ***
## poly(HUMIDITY, 4)1    NA         NA      NA      NA
## poly(HUMIDITY, 4)2   -8808.27   454.83  -19.366 < 2e-16 ***
## poly(HUMIDITY, 4)3   -3115.68   399.88   -7.792 7.62e-15 ***
## poly(HUMIDITY, 4)4   1152.09   441.68    2.608 0.009116 **
## poly(RAINFALL, 4)1    NA         NA      NA      NA
## poly(RAINFALL, 4)2   3050.42   366.77    8.317 < 2e-16 ***
## poly(RAINFALL, 4)3   -1903.41   355.98   -5.347 9.24e-08 ***
## poly(RAINFALL, 4)4   2611.87   348.94    7.485 8.06e-14 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 338 on 6725 degrees of freedom

```

```
## Multiple R-squared:  0.727, Adjusted R-squared:  0.7251
## F-statistic: 389.2 on 46 and 6725 DF,  p-value: < 2.2e-16

test_results <- predict(lm_poly,test_data)

## Warning in predict.lm(lm_poly, test_data): prediction from a rank-
deficient fit
## may be misleading

#minor improvement we could do here is to convert all negative prediction
results to zero, because we can not have negative rented bike counts
test_results[test_results<0] <- 0
df <- data.frame(truth=test_data$RENTED_BIKE_COUNT,estimate=test_results)

rmse_poly <- rmse(df,truth =truth,estimate=estimate);rmse_poly

## # A tibble: 1 x 3
##   .metric .estimator .estimate
##   <chr>   <chr>       <dbl>
## 1 rmse    standard       317.

rsq_poly <- rsq(df,truth,estimate);rsq_poly

## # A tibble: 1 x 3
##   .metric .estimator .estimate
##   <chr>   <chr>       <dbl>
## 1 rsq     standard       0.753

Fitting of regression model with interaction and polynomial terms

lm_poly2 <- lm(RENTED_BIKE_COUNT ~ .+ RAINFALL*HUMIDITY +poly(TEMPERATURE,6)
+ poly(HUMIDITY,4) + poly(DEW_POINT_TEMPERATURE,4) ,train_data)
summary(lm_poly2)

##
## Call:
## lm(formula = RENTED_BIKE_COUNT ~ . + RAINFALL * HUMIDITY +
poly(TEMPERATURE,
##      6) + poly(HUMIDITY, 4)+ poly(DEW_POINT_TEMPERATURE, 4),
##      data = train_data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -1560.10  -203.91    5.57   184.69  1467.53
##
## Coefficients: (6 not defined because of singularities)
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    178.70     52.34   3.414 0.000643 ***
## TEMPERATURE    2160.10    255.57   8.452 < 2e-16 ***
## HUMIDITY       -286.80    122.47  -2.342 0.019223 *
## WIND_SPEED      13.76     34.66   0.397 0.691278
## VISIBILITY     -30.78     18.23  -1.689 0.091299 .
```

```

## DEW_POINT_TEMPERATURE      -1007.46      278.05      -3.623      0.000293 ***
## SOLAR_RADIATION             -24.74        38.49       -0.643      0.520293
## RAINFALL                    -40976.73    5378.30     -7.619      2.91e-14 ***
## SNOWFALL                    -66.83       91.86       -0.728      0.466927
## `0`                         -118.91      28.24       -4.211      2.58e-05 ***
## `1`                         -230.91      28.04       -8.236      < 2e-16 ***
## `2`                         -339.86      28.10      -12.097      < 2e-16 ***
## `3`                         -407.57      28.50      -14.301      < 2e-16 ***
## `4`                         -478.16      28.31      -16.893      < 2e-16 ***
## `5`                         -452.69      27.97      -16.187      < 2e-16 ***
## `6`                         -297.99      28.16      -10.580      < 2e-16 ***
## `7`                          19.96       28.25        0.707      0.479834
## `8`                         367.22      28.29       12.980      < 2e-16 ***
## `9`                         -37.30      28.96       -1.288      0.197720
## `10`                       -228.46     30.28       -7.544      5.16e-14 ***
## `11`                       -195.74     32.08       -6.101      1.11e-09 ***
## `12`                       -102.01     32.96       -3.095      0.001979 **
## `13`                       -94.12      33.43       -2.815      0.004886 **
## `14`                       -88.87      32.28       -2.753      0.005924 **
## `15`                       -29.04      31.68       -0.917      0.359399
## `16`                         78.23      30.40        2.573      0.010089 *
## `17`                       320.14      29.41       10.886      < 2e-16 ***
## `18`                       759.43      28.70       26.464      < 2e-16 ***
## `19`                       464.00      28.11       16.507      < 2e-16 ***
## `20`                       351.31      27.95       12.569      < 2e-16 ***
## `21`                       352.89      28.07       12.570      < 2e-16 ***
## `22`                       240.73      27.99        8.601      < 2e-16 ***
## `23`                        NA             NA           NA           NA
## AUTUMN                     348.34      20.40       17.080      < 2e-16 ***
## SPRING                     204.65      19.89       10.288      < 2e-16 ***
## SUMMER                     305.45      25.85       11.817      < 2e-16 ***
## WINTER                      NA             NA           NA           NA
## HOLIDAY                    -108.30      19.67       -5.504      3.84e-08 ***
## NO_HOLIDAY                  NA             NA           NA           NA
## poly(TEMPERATURE, 6)1       NA             NA           NA           NA
## poly(TEMPERATURE, 6)2       7461.89     734.43      10.160      < 2e-16 ***
## poly(TEMPERATURE, 6)3     -10554.08    473.81     -22.275      < 2e-16 ***
## poly(TEMPERATURE, 6)4     -7065.41    448.97     -15.737      < 2e-16 ***
## poly(TEMPERATURE, 6)5       159.15     375.47        0.424      0.671684
## poly(TEMPERATURE, 6)6     1529.21    349.04        4.381      1.20e-05 ***
## poly(HUMIDITY, 4)1         NA             NA           NA           NA
## poly(HUMIDITY, 4)2     -5337.17    506.55     -10.536      < 2e-16 ***
## poly(HUMIDITY, 4)3     -3689.63    385.42       -9.573      < 2e-16 ***
## poly(HUMIDITY, 4)4     -2141.01    454.49       -4.711      2.52e-06 ***
## poly(DEW_POINT_TEMPERATURE, 4)1 NA             NA           NA           NA
## poly(DEW_POINT_TEMPERATURE, 4)2 -13110.24    752.82     -17.415      < 2e-16 ***
## poly(DEW_POINT_TEMPERATURE, 4)3 -2380.16    475.49       -5.006      5.71e-07 ***
## poly(DEW_POINT_TEMPERATURE, 4)4   915.95     428.53        2.137      0.032601 *
## HUMIDITY:RAINFALL         40345.40    5455.12        7.396      1.58e-13 ***
## ---

```

```

## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 331.5 on 6724 degrees of freedom
## Multiple R-squared:  0.7373, Adjusted R-squared:  0.7354
## F-statistic: 401.5 on 47 and 6724 DF,  p-value: < 2.2e-16

test_results2 <- predict(lm_poly2,test_data)

## Warning in predict.lm(lm_poly2, test_data): prediction from a rank-
deficient fit
## may be misleading

#minor improvement we could do here is to convert all negative prediction
results to zero, because we can not have negative rented bike counts
test_results2[test_results2<0] <- 0
df1 <- data.frame(truth=test_data$RENTED_BIKE_COUNT,estimate=test_results2)

rmse_poly2 <- rmse(df1,truth =truth,estimate=estimate);rmse_poly2

## # A tibble: 1 x 3
##   .metric .estimator .estimate
##   <chr>   <chr>       <dbl>
## 1 rmse    standard      314.

rsq_poly2 <- rsq(df1,truth,estimate);rsq_poly2

## # A tibble: 1 x 3
##   .metric .estimator .estimate
##   <chr>   <chr>       <dbl>
## 1 rsq     standard      0.757

```