

(Q.1) Algorithm \rightarrow step-by-step procedure or a set of well-defined instructions designed to perform a specific task or solve a particular problem.

\Rightarrow Importance of efficiency in algorithm design.
 It ensures that the algorithm runs fast saving time
 uses fewer resources like memory & processor power.
 It can handle large inputs effectively, making them practical for real-world applications.

(Q.2) Row Major and Column major representation of arrays

In memory, 2D array is stored as 1D sequence of elements. The way elements are arranged depends on whether the system uses row or column major order.

* Row-Major representation

elements of each row are stored contiguously in memory. (used in C, C++, Java)

Ex

$$\begin{bmatrix} 2 & 3 \\ 3 & 4 \end{bmatrix}$$

RMO $\Rightarrow [2, 3, 4]$

2 \rightarrow 3 \rightarrow 4

*

Column-Major representation

elements of each column are stored contiguously in memory (used in MATLAB and Fortran)

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix}$$

1 \rightarrow 4 \rightarrow 2 \rightarrow 5 \rightarrow 3 \rightarrow 6

3) General index formula for multi-Dimensional Arrays

Let's consider an n -dimensional array:

$$A [L_1 \dots U_1] [L_2 \dots U_2] \dots [L_n \dots U_n]$$

Base address = Address of the first element $A[L_1][L_2][L_3]$

Element size (w) = Number of bytes per element

L_i = Lower bound of the i^{th} dimension

U_i = Upper bound of i^{th} dimension

General Formula

$$\text{LOC}(A[i_1, i_2, \dots, i_n]) = BA + w \times [(i_1 - L_1) \times (U_2 - L_2 + 1) \times \dots \times (U_n - L_n + 1) + (i_2 - L_2) \times (U_3 - L_3 + 1) \times \dots + \dots + (i_n - L_n)]$$

0.7) Insertion Sort

- * Builds the sorted array by inserting elements into the correct position.

Best case Time Complexity

$$O(n)$$

Avg case $\Rightarrow O(n^2)$

Worst case $\Rightarrow O(n^2)$

Stable

in-place

Insertion Sort is faster for nearly sorted data

Selection Sort

- * Repeatedly selects the smallest (or largest) element and places it in order.

Best case Time Complexity

$$O(n^2)$$

Avg case $\Rightarrow O(n^2)$

Worst case $\Rightarrow O(n^2)$

Not Stable

in-place

Selection sort performs the same number of comparisons regardless of data order.

(Q.5) Merge Sort Algorithm

Divide - split the array into two halves until each subarray has only one element.

Conquer - Recursively sort the two halves

Combine - Merge the two sorted halves into one sorted array.

For Example

$\begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 \\ [38, 27, 43, 3, 9, 82, 10] \end{matrix}$

Divide $\begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 \\ [38, 27, 43, 3] & [9, 82, 10] \end{matrix}$

$\begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 \\ [38, 27] & [43, 3] & [9, 82] & [10] \end{matrix}$

$\begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 \\ [38] & [27] & [43] & [3] & [9] & [82] & [10] \end{matrix}$

Merge (sort each pair)

$[27, 38] [3, 43] [9, 82] [10]$

Merge again

$[3, 27, 38, 43] [9, 10, 82]$

Final Merge

$[3, 9, 10, 27, 38, 43, 82]$

⇒ Time Complexity

Best, Average, Worst case $\Rightarrow O(n \log n)$

Space complexity $\approx O(n)$

Merge sort is efficient & stable, ideal for large datasets but uses extra memory for merging.

6) Removal of Recursion

We convert the recursive process into an iterative one using loops, which saves memory & improves efficiency.

Recursive Factorial function

```
int fact(n){  
    if (n == 0 || n == 1) {  
        return 1;  
    } else {  
        return n * fact(n-1);  
    }  
}
```

Equivalent iterative Algorithm

```
int num = 5  
for (int i=1; i <= num; i++) {  
    factorial *= i;  
}  
cout << "Factorial = " << factorial;
```

Advantages of Removing Recursion

Saves stack memory

Reduces function call overhead

Improves speed for large inputs.

7) Types of insertions in SLL

(A) At the beginning (head)

(a) Create a new node.

(b) Set `newNode->next = head`

(c) Update `head = newNode`

Program

$10 \rightarrow 20 \rightarrow 30$

insert 5 at the head = $5 \rightarrow 10 \rightarrow 20 \rightarrow 30$

`newNode -> [5 | *] -> [10 | *] -> [20 | *] -> [30 | NULL]`

(B) Insertion at the End

(a) Create a new Node & set $\text{newNode} \rightarrow \text{next} = \text{NULL}$

(b) Traverse the list until last node.

(c) Set $\text{last} \rightarrow \text{next} = \text{new Node}$.

Diagram

$10 \rightarrow 20 \rightarrow 30$
insert 5 at the end

$[10] * \rightarrow [20] * \rightarrow [30] * \rightarrow [5] \text{NULL}$

(C) Insertion at a Specific Position

(a) Create a new Node

(b) Traverse to the node after which insertion is to be done

(c) Set $\text{newNode} \rightarrow \text{next} = \text{temp} \rightarrow \text{next}$.

Set $\text{temp} \rightarrow \text{next} = \text{newNode}$.

Diagram

Insert 5 at the 2nd position

$10 \rightarrow 20 \rightarrow 30$

$10 \rightarrow 5 \rightarrow 20 \rightarrow 30$

$[10] * \rightarrow [5] * \rightarrow [20] * \rightarrow [30] *$

Advantages of LL insertion -

- * Efficient insertion (no shifting like arrays)
- * Dynamic memory allocation

Disadvantages -

- * Requires traversal to find insertion point ($O(n)$ time).
- * Extra memory for pointers.

Q. 8) (a) Recursive Solution to Tower of Hanoi

$\text{TOH}(n, A, B, C)$

if $n = 1$;

print "Move disk 1 from", A, "to", C

return

$\text{TOH}(n-1, A, C, B)$ // Move n-1 disks from A to B

print "Move disk", n, "from", A, "to", C

$\text{TOH}(n-1, B, A, C)$ // Move n-1 disks from B to C

where A = source ; B = auxiliary ; C = destination

Logic \Rightarrow

i. Move n-1 disks from A \rightarrow B (C as aux)

Move nth (largest disk from A \rightarrow C

Move n-1 disks from B \rightarrow C (A as aux)

Time Complexity $\Rightarrow T(n) = 2T(n-1) + 1$
 $\Rightarrow T(n) = 2^n - 1$

(b)

Advantages recursion

(i) Simplifies complex problems like TOH, Fibonacci

Tree Traversal etc

(ii) Code is shorter & easier to understand

(iii) Useful for divide & conquer algorithms

(iv) Natural fits for hierarchical data structures like trees & graphs.

Disadvantages recursion

(i) Uses more memory due to function call stack

(ii) May cause stack overflow for large input values

(iii) Slower execution due to repeated function calls

(iv) Can be harder to debug and trace.

(Q.9) Sparse Matrix Representation Using a 2D array
 A sparse matrix contains more zeros than non-zero elements.
 Normal (2D Array) Representation

$$A[4][4] = \{ \{0, 0, 3, 0\}, \\ \{0, 0, 5, 7\}, \\ \{0, 0, 0, 0\}, \\ \{0, 2, 6, 0\} \}$$

→ To store efficiently, we use a 3-column representation (also called Triplet form):

Row	Column	Value
0	2	3
1	2	5
1	3	7
3	1	2
3	2	6

→ We can store this data in a 2D array

$$\text{Sparse}[6][3] = \{$$

$$\{4, 4, 5\} \\ \{0, 2, 3\} \\ \{1, 2, 5\} \\ \{1, 3, 7\} \\ \{3, 1, 2\} \\ \{3, 2, 6\}$$

7;

→ First row stores matrix dimensions of
 number of non-zero values
 → 4 rows, 4 columns, 5 non-zero elements

→ Remaining rows store (rows, columns, value) of each non-zero element.

Advantages of Sparse Matrix Representation:

- (1) Memory Efficiency - saves space by storing only ^{non-0} elements
- (2) Faster computation - operations like add, or multiplication skip zero elements, making computation faster.
- (3) Easier for data transmission
- (4) Useful for Real-world applications
Ex ML, graph, algo of scientific computing

Limitations

- (1) Complex implementation → requires additional logic to handle insertion, deletion, or search of elements.
- (2) Extra Overhead → Must store row & column indices along with each value.
- (3) Not suitable for Dense matrices → If many elements are non-zero, triplet form may use more space than a normal array.
- (4) Difficult Random Access → direct access to an element is slower compared to normal 2D arrays.

OR

(P.T.O)

Doubly Linked Lists in Complex Data Management

Applications

- (1) Browser History Management :
Forward & backward navigation using next and prev pointers
- (2) Undo / Redo Functionality in Editors :
Each action is stored as a node; backward traversal undoes actions, forward traversal redos them.
- (3) Music / Video Playlist Management :
Allows skipping forward / backward in a playlist efficiently.
- (4) Database Transaction Logs :
Easier insertion/deletion of records with previous/next links.

I. Traversal in DLL

⇒ Forward Traversal ($10 \rightarrow 20 \rightarrow 30 \rightarrow \text{NULL}$)

Node temp = head;

while (temp != null) {

SOP ($\leftarrow \text{temp.data} + " \rightarrow "$);

temp = temp.next;

}
SOP ("NULL");

II. Backward Traversal

Backward Traversal ($30 \rightarrow 20 \rightarrow 10 \rightarrow \text{NULL}$)

Node temp = tail;

while (temp != null) {

SOP (temp.data + " \rightarrow ");

}
temp = temp.prev;

SOP ("NULL");

2. Deletion in DLL

- (i) Identify the node to delete (delNode)
- (ii) Update the next pointers of delNode.prev to delNode.next.
- (iii) Update the prev pointer of delNode.next to delNode.prev.
- (iv) Delete delNode.

Code →

```
if ( delNode.prev != null )
    delNode.prev.next = delNode.next;
if ( delNode.next != null )
    delNode.next.prev = delNode.prev ;
delNode = null ;
```