

CIRCLE ASSIGNMENT

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1 PROBLEM 1

1. ABC and ADC are two right triangles with common hypotenuse AC. Prove that $\angle CAD = \angle CBD$.

SOLUTION:

Given, AC is the common hypotenuse.

$$\angle B = \angle D = 90 \quad (1.0.1)$$

To prove,

$$\angle CAD = \angle CBD \quad (1.0.2)$$

Proof:

$\because \angle ABC$ and $\angle ADC$ are 90° .

These angles are in the semi-circle.

Thus, both the triangles are lying in the semi-circle and AC is the diameter of the circle.

\Rightarrow Points A,B,C and D are concyclic.

Thus, CD is the chord.

$$\Rightarrow \angle CAD = \angle CBD \text{ (Angles in the same segment of the circle)} \quad (1.0.3)$$