

Question Paper

**MANIPAL ACADEMY OF HIGHER EDUCATION****COMPUTATIONAL MATHEMATICS - II [MAT 1272]****Marks: 30****Duration: 90 mins.****MCQ****Answer all the questions.**

Section Duration: 20 mins

- 1) The degree of homogeneous function

$$f(x, y) = \sqrt{\frac{\frac{1}{x^2} + \frac{1}{y^2}}{\frac{1}{x^3} + \frac{1}{y^3}}}$$

is \_\_\_\_

(0.5)

$$\frac{1}{12} \quad \frac{1}{3} \quad \frac{1}{6} \quad \frac{1}{2}$$

- 2) The percentage error in the area of a rectangle when an error of 1% is made in measuring its length and breadth is \_\_\_\_

(0.5)

$$\underline{2\%} \quad \underline{1\%} \quad \underline{0\%} \quad \underline{3\%}$$

- 3) The coefficient of
- $y^3$
- in the Maclaurin's series expansion of
- $xy + \cos y$
- is \_\_\_\_

(0.5)

$$\underline{2} \quad \underline{0} \quad \underline{4} \quad \underline{6}$$

- 4) If
- $u = f(r, s)$
- and
- $r = x + at$
- ,
- $s = y + bt$
- , where
- $a$
- and
- $b$
- are constants, then
- $\frac{\partial u}{\partial t} =$
- \_\_\_\_

(0.5)

$$a \frac{\partial r}{\partial x} + a \frac{\partial r}{\partial x} + b \frac{\partial s}{\partial y} + a \frac{\partial u}{\partial x} + b \frac{\partial u}{\partial y} + \frac{\partial u}{\partial x} + \frac{\partial u}{\partial y}$$

- 5) The value of
- $\frac{\Gamma(7/2)}{\Gamma(5/2)}$
- is

(0.5)

$$\underline{3.5} \quad \underline{4.5} \quad \underline{2.5} \quad \underline{1.4}$$

- 6) The value of
- $\int_0^1 x^4 (1 - \sqrt{x})^3 dx$
- is

(0.5)

$$2\beta(10, 4) \quad \beta(10, 4) \quad \beta(9, 3) \quad 2\beta(6, 4)$$

- 7) (0.5)

On changing to spherical polar coordinates, the integral

$$\int_0^1 \int_0^{\sqrt{1-x^2}} \int_0^{\sqrt{1-x^2-y^2}} \frac{dz dy dx}{\sqrt{1-x^2-y^2-z^2}}$$

is \_\_\_\_

$$\int_0^{2\pi} \int_0^{\frac{\pi}{2}} \int_0^1 \frac{r^2 \sin \theta}{\sqrt{1-r^2}} dr d\theta d\phi \int_0^{2\pi} \int_0^{\pi} \int_0^1 \frac{r^2 \sin \theta}{\sqrt{1-r^2}} dr d\theta d\phi \int_0^{\pi} \int_0^{\frac{\pi}{2}} \int_0^1 \frac{r^2 \sin \theta}{\sqrt{1-r^2}} dr d\theta d\phi \int_0^{\frac{\pi}{2}} \int_0^{\frac{\pi}{2}} \int_0^1 \frac{r^2 \sin \theta}{\sqrt{1-r^2}} dr d\theta d\phi$$

- 8) The value of the double integral

$$\iint_R \frac{1}{\sqrt{x^2+y^2}} dx dy$$

, where

$R$

is the region bounded by the circle

$$x^2 + y^2 = 1$$

is

(0.5)

$$\pi \quad 2\pi \quad \frac{\pi}{2} \quad 0$$

- 9) The value of

$$\int_{x=1}^2 \int_{y=2}^3 \int_{z=1}^3 (x^2 + 1) dz dy dx$$

is

(0.5)

$$\frac{10}{3} \quad \frac{20}{3} \quad \frac{22}{3} \quad \frac{20}{7}$$

- 10) If

$$u = x + y, \quad v = 3x - 2y,$$

then  $\frac{\partial(x, y)}{\partial(u, v)}$  is \_\_\_\_

(0.5)

$$-\frac{1}{5} \quad -5 \quad -1 \quad \underline{1}$$

### DESCRIPTIVE

Answer all the questions.

- 11) Using triple integral, find the volume of the portion of sphere  $x^2 + y^2 + z^2 = 9$  lying inside the cylinder  $x^2 + y^2 = 3y$  above the  $xy$ -plane. (4)

- 12) Expand  $f(x, y) = \tan^{-1}(xy)$  about the point  $(1, 1)$  up to second degree terms. (3)

- 13) Find the extreme values of the function  $f(x, y) = x^3 + y^3 - 63(x + y) + 12xy$ . (3)

- 14) If  $u = \sin^{-1}\left(\frac{x^2 y^2}{x+y}\right)$ , then prove that  $x^2 u_{xx} + 2xy u_{xy} + y^2 u_{yy} = 3 \tan u (3 \tan^2 u + 2)$ . (3)

- 15) Calculate the line of regression for the following data:

x	0	25	50	75	100
y	14	38	54	76	95

(3)

- 16) Evaluate  $\int_0^1 \int_y^{2-y} xy dx dy$  by changing the order of integration. (3)

- 17) Evaluate  $\int_0^1 \int_0^{1-x} (y-x)^2 \sqrt{x+y} dy dx$ , using the transformations  $x + y = u$ ,  $y - x = v$ . (3)

- 18) Use double integration to find the area of the region inside the circle  $r = 4\cos\theta$  and outside the circle  $r = 2$ . (3)