# Problem set 3

### Buan 6340

## Linear algebra

#### 1. General Least Squares:

Suppose we are estimating a linear model:

$$y = \mathbf{X}\beta + e$$

However instead of the  $Var(e) = \sigma^2 \mathbf{I}_n$ , we know that  $Var(e) = \Sigma$ . Derive the optimal OLS estimator given this condition. That is, minimize  $e'\Sigma^{-1}e$  and obtain the optimal estimator. It may be helpful to take the square root  $\Sigma$ , i.e.,  $\Sigma = \Sigma^{1/2}\Sigma^{1/2}$ .

## **Programming**

#### 2. OLS estimation of AR(1):

Consider the following AR(1) model:

$$x_t = \alpha + \rho x_{t-1} + e_t$$

Generate data from this model. Then estimate the model using ordinary least squares. The estimated  $\hat{\rho}$  that you will find will be biased. Write a simulation to study this bias. See if you can find the functional form of the bias via simulation.