

# 8-Puzzle Solver

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# INTRODUCTION:

## PROBLEM STATEMENT:

The task is to develop an intelligent solver for the 8-puzzle problem, a sliding tile puzzle that consists of a 3×3 grid containing eight numbered tiles (1-8) and a blank space (0). The goal of the AI rearrange the tiles into the correct order. The problem is solved using A\* search, where the input of the tiles are given by human.

Step 1: Initial	Step 2	Step 3	Step 4: Final																																				
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**User Input Handling:** The program prompts the user to enter the puzzle's initial state while ensuring valid input.

*A Search Algorithm:*\* It finds the optimal path to the solution by prioritizing states with the lowest cost (depth + heuristic).

**Manhattan Distance Heuristic:** This heuristic estimates how far tiles are from their correct positions, guiding the search efficiently.

**Priority Queue (Min-Heap):** Ensures that the most promising states are explored first.

**Solution Path Display:** The program prints each move taken and the depth at which the solution is reached

# METHODOLOGY:

The 8-puzzle problem is a classic state-space search problem that involves arranging tiles in a 3×3 grid to match a predefined goal configuration. The solution must determine a sequence of moves required to reach the goal from a user-defined initial state. To achieve this, **Depth-First Search (DFS)** is implemented to explore possible moves systematically.

## Problem Formulation

The puzzle consists of eight numbered tiles (1-8) and a blank space (0), which can move **left, right, up, or down** within the grid. The objective is to transform a given initial state into the goal state:

### *Algorithm Selection: Depth-First Search (DFS)*

*DFS is a blind search algorithm that explores a path as deep as possible before backtracking. It does not guarantee the shortest path but is simple and effective for small problem spaces. The algorithm is implemented using a stack (LIFO) and follows these steps:*

*User Input Handling – The program verifies that the input configuration is valid and ensures that numbers 0-8 are entered correctly.*

*State Representation – A PuzzleState class is used to store the board configuration, depth, blank tile position, and solution path.*

### *DFS Execution*

*The initial state is pushed onto the stack.*

*The algorithm explores possible moves (up, down, left, right) and generates new board states.*

*If a state has not been visited, it is added to the stack for further exploration.*

*The search continues until the goal state is reached or all possibilities are exhausted.*

- 1. Solution Path Display – The sequence of moves taken to reach the goal is printed*

# CODE:

```
1  # Import necessary libraries
2  from collections import deque
3
4  # Define the dimensions of the puzzle
5  N = 3
6
7  # Structure to store a state of the puzzle
8  class PuzzleState:
9      def __init__(self, board, x, y, depth, path):
10         self.board = board
11         self.x = x
12         self.y = y
13         self.depth = depth
14         self.path = path
15
16 # Possible moves: Left, Right, Up, Down
17 row_moves = [0, 0, -1, 1]
18 col_moves = [-1, 1, 0, 0]
19
20 # Function to check if a given state is the goal state
21 def is_goal_state(board):
22     goal = [[1, 2, 3], [4, 5, 6], [7, 8, 0]]
23     return board == goal
24
25 # Function to check if a move is valid
26 def is_valid(x, y):
27     return 0 <= x < N and 0 <= y < N
28
29 # Function to print the board
30 def print_board(board):
31     for row in board:
```

```

32     print(' '.join(map(str, row)))
33     print("-----")
34
35     # Function to take user input for the board with validation
36     def get_user_input():
37         print("Enter the 8-puzzle numbers row by row (use 0 for the blank space):")
38         board = []
39         numbers = set()
40
41         for i in range(N):
42             while True:
43                 try:
44                     row = list(map(int, input(f"Row {i+1}: ").split()))
45                     if len(row) != N:
46                         raise ValueError("Each row must contain exactly 3 numbers.")
47                     if any(num < 0 or num > 8 for num in row):
48                         raise ValueError("Numbers must be between 0 and 8.")
49                     if any(num in numbers for num in row):
50                         raise ValueError("Duplicate numbers are not allowed.")
51                     numbers.update(row)
52                     break
53                 except ValueError as e:
54                     print(f"Invalid input: {e}. Please try again.")
55             board.append(row)
56
57     # Ensure there's exactly one 0 (blank space)

```

```

57     # Ensure there's exactly one 0 (blank space)
58     if 0 not in numbers:
59         print("Error: The input must contain exactly one 0 for the blank space.")
60         return get_user_input()
61
62     # Find the position of the blank space (0)
63     x, y = next((i, j) for i in range(N) for j in range(N) if board[i][j] == 0)
64     return board, x, y
65
66     # Depth-First Search (DFS) to solve the 8-puzzle problem
67     def solve_puzzle_dfs(start, x, y):
68         stack = [] # Stack for DFS
69         visited = set()
70         stack.append(PuzzleState(start, x, y, 0, []))
71         visited.add(tuple(map(tuple, start)))
72
73         while stack:
74             curr = stack.pop()
75
76             # Print the current board
77             print(f'Depth: {curr.depth}')
78             print_board(curr.board)
79
80             # Check if goal state is reached
81             if is_goal_state(curr.board):
82                 print(f'Goal state reached at depth {curr.depth}')
83                 print("Solution Path:")
84                 for step in curr.path:
85                     print_board(step)
86                 return

```

```

86         return
87
88     # Explore possible moves
89     for i in range(4):
90         new_x = curr.x + row_moves[i]
91         new_y = curr.y + col_moves[i]
92
93         if is_valid(new_x, new_y):
94             new_board = [row[:] for row in curr.board]
95             # Swap the tiles
96             new_board[curr.x][curr.y], new_board[new_x][new_y] = new_board[new_x][new_y], new_board[curr.x][curr.y]
97
98             # If this state has not been visited before, push to stack
99             board_tuple = tuple(map(tuple, new_board))
100             if board_tuple not in visited:
101                 visited.add(board_tuple)
102                 stack.append(PuzzleState(new_board, new_x, new_y, curr.depth + 1, curr.path + [new_board]))
103
104     print('No solution found (DFS reached depth limit)')
105
106 # Driver Code
107 if __name__ == '__main__':
108     start, x, y = get_user_input()
109
110     print('Initial State:')
111     print_board(start)
112
113     solve_puzzle_dfs(start, x, y)
114

```

# OUTPUT/RESULT:

INITAIL INPUT:

```
Streaming c
4 8 2
3 7 0
1 5 6
-----
```

OUTPUTS and proccess:

```
9s 2 0 3
    1 8 5
    4 7 6
    -----
    0 2 3
    1 8 5
    4 7 6
    -----
    1 2 3
    0 8 5
    4 7 6
    -----
    1 2 3
    4 8 5
    0 7 6
    -----
    1 2 3
    4 8 5
    7 0 6
    -----
    1 2 3
    4 0 5
    7 8 6
    -----
    1 2 3
    4 5 0
    7 8 6
    -----
    1 2 3
    4 5 6
    7 8 0
    -----
```



THIS IS THE FINAL OUTPUT, THE  
NUMBER TILES ARE ARRANGED IN  
INCREASING ORDER PER ROW



# REFERENCE AND CREDITS ;):

Depth-First Search (DFS)- For understanding the Depth-First Search (DFS) and 8 tile puzzle solving, I referred to various online resources and tutorials:

**GEEKSFORGEEKS:**

[8 puzzle Problem - GeeksforGeeks](#)

**WIKIPEDIA:**

[Depth-first search - Wikipedia](#)