

28/10/2022

Example 1:

$V_N = \{S\}, T = \{a, b\}, S = \{S\}, P = \{S \rightarrow aSb \mid \epsilon\}$   
 $S \rightarrow \epsilon, S \rightarrow aSb \rightarrow ab \quad L(G) = \{\epsilon, ab\}$

$$L(G) = \{a^n \cdot b^n \mid n \geq 0\}$$

Example 2:

$P: \{S \rightarrow aCa, C \rightarrow aCa \mid b\}$

$S \Rightarrow aCa \Rightarrow aCaa \dots \Rightarrow a^n b^n$

$$L(G) = a^n \cdot b^n \quad n \geq 0$$

$$\epsilon \notin L(G)$$

Example 3:

$S \rightarrow AbB, A \rightarrow aA \mid \epsilon, B \rightarrow aB \mid a$

Example 4:

$S \rightarrow aS \mid bS \mid \epsilon$

$$L(G) = \{a, b\}^*$$

Example 5:

$S \rightarrow aSa \mid bSb \mid c$  ( $c$  is also terminal symbol)

$L(G) = W \in W^R$ ,  $W$  is any string from  $\{a, b\}^*$   
 $W^R$  is reverse of  $W$ .

## Language to Grammar:

Example 1:

$$L(G) = a^n, n > 0$$

$$S \rightarrow aS \text{ or } S \rightarrow a. \quad S \rightarrow aS/a \quad S \rightarrow aS/\epsilon \quad a^0 = \epsilon$$

Grammar:

$$S \rightarrow \epsilon$$

$$G = \{V_N = \{S\}, T = \{a\}, S, P = \{S \rightarrow aS/a\}\}$$

Example 2:

$$L(G) = (ab)^n, n > 0 \quad ab, abab, ababab, \dots$$

$$G = \{V_N = S, T = \{ab\}, S, P = \{S \rightarrow abS/ab\}\}$$

Example 3:

$$L(G) = a^n b^n, n > 0$$

$$S \rightarrow aSb/ab$$

$$G = \{V_N = \{S\}, T = \{a, b\}, S, P = \{S \rightarrow aSb/ab\}\}$$

Example 4:

$$L(G) = a^n c^i b^n, n, i \geq 0$$

$$S \rightarrow aWb, W \rightarrow cW/\epsilon$$

$$P \rightarrow \{S \rightarrow aSb/A, A \rightarrow AC/\epsilon\}$$

## Context - Sensitive Grammar :

$$L(G) = a^n b^n c^n, n \geq 1$$

$$G = \{V_N = \{S, A, B\}, T = \{a, b, c\}, S, P = \{S \rightarrow Abc \mid ABS, BA \rightarrow AB, Bb \rightarrow bb, A \rightarrow a\}\}$$

### Example 2:

$$L(G) = \alpha\alpha, \alpha \in \{a, b\}^*$$

## Regular Grammar

→ Uses three operations, Union, Concatenation and Kleene Star.

→ Description:

Obtained by:

replacing " $\{ \}$ " by " $( )$ " or leaving it out

replacing " $\cup$ " by " $+$ "

replacing concatenation by " $.$ "

Language Regular Expression

$$\{\epsilon\}$$

$$\epsilon$$

$$\{0\}$$

$$0$$

$$\{0\} \{0\} \{1\}$$

$$0.0.1$$

$$\{1, \epsilon\} \{001\}$$

$$(1 + \epsilon).001$$

$$\{110\}^* \{0, 1\}$$

$$(110)^* (0 + 1)$$



R- Set of Regular over  $\Sigma$

(i)  $\phi \notin R \Rightarrow R.E$  is  $\phi$  -  
(~~if~~)

(ii)  $\{\epsilon\} \in R \Rightarrow R.E$  is  $\epsilon$

(iii) For any  $a \in \Sigma$ ,  $\{a\} \in R \Rightarrow R.E$  is  $a$ .

(iv) If  $L_1, L_2 \in R$ ,  $r_1$  and  $r_2$  are the R-E for  $L_1, L_2$

$$L_1 \cup L_2 \Rightarrow r_1 + r_2$$

$$L_1 \cdot L_2 \Rightarrow r_1 \cdot r_2$$

$$L_1^* \Rightarrow r_1^*$$

$\rightarrow$  Only those languages obtained from (i) - (iv) are [REGEX] over  $\Sigma$ .

$$L^2 = L \cdot L \Rightarrow r^2 = r \cdot r$$

Order of Precedence:

Kleene Star - Highest

Concatenation -

Union - least



$$\text{Example: } (a + (b)^*)c = a + b^*c$$

$$(a+b)^* \neq a+b^*$$

$$1^*, 1^* = 1^*$$

$$(0^* 1^*)^* \neq (0^* 1)^*$$

$$L \subseteq \{0,1\}^*$$

(i) string of even length :

~~is~~ it regular

$$\{00, 01, 10, 11\}^* \Rightarrow (0 \cdot 0 + 0 \cdot 1 + 1 \cdot 0 + 1 \cdot 1)^*$$

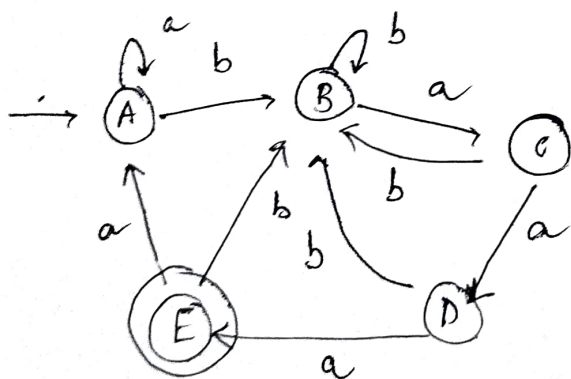
$$[(0+1)(0+1)]^*$$

(ii) string having odd no. of 1's -

$$L = \{ x \in \{0,1\}^* : n_1(x) \text{ is odd} \}$$

DFA to language expressions.

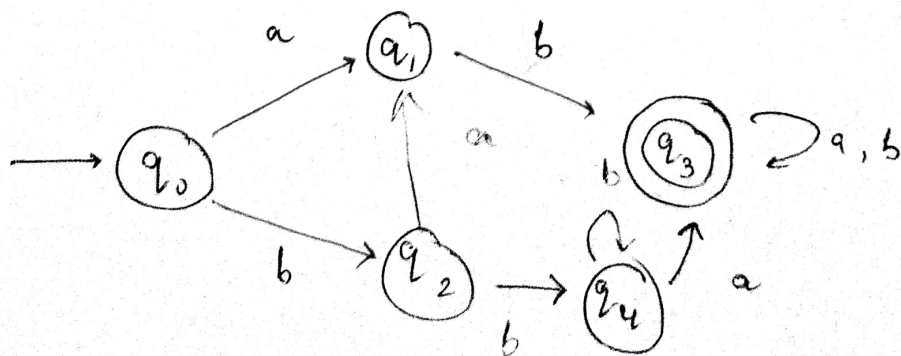
①



$$\{a, b\}^* \cdot baaa$$

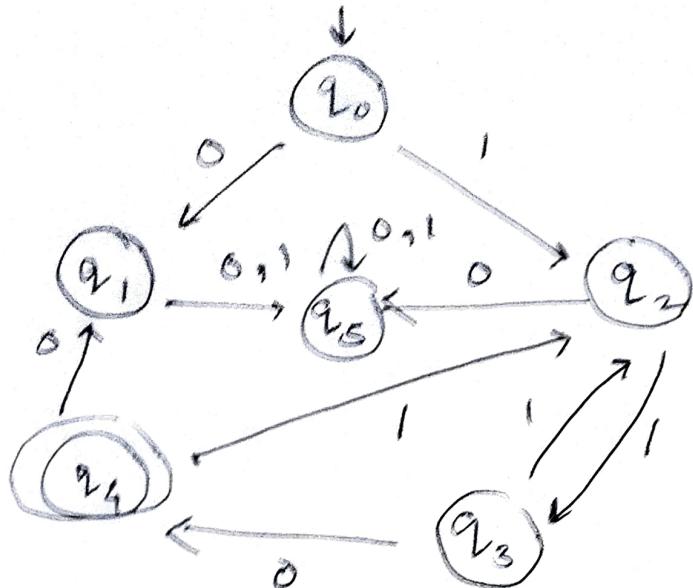
$$= (a+b)^* baaa$$

②



$$a \cdot a + b \cdot b a$$

3



$$\frac{(11+110)^* 0}{}$$