490. The Maze

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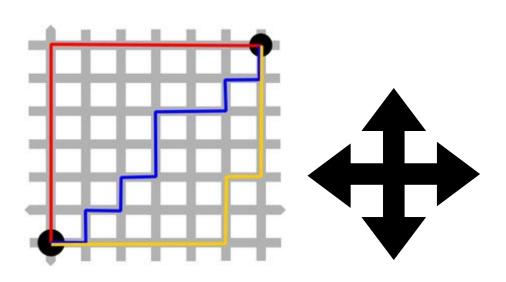
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Problem Statement

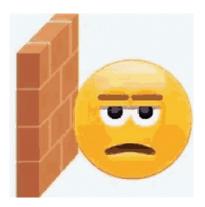
There is a ball in a maze with empty spaces (represented as 0) and walls (represented as 1). The ball can go through the empty spaces by rolling **up**, **down**, **left or right**, but it won't stop rolling until hitting a wall. When the ball stops, it could choose the next direction.

Given the m x n maze, the ball's start position and the destination, where start = [startrow, startcol] and destination = [destinationrow, destinationcol], return true if the ball can stop at the destination, otherwise return false.

Understanding the Problem Statement



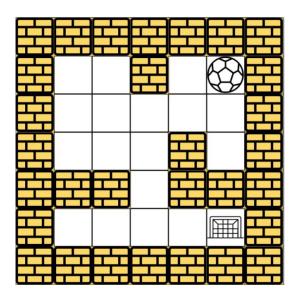
a. Traversal in manhattan/taxicab geometryb. Right, Left, Up, Down directions



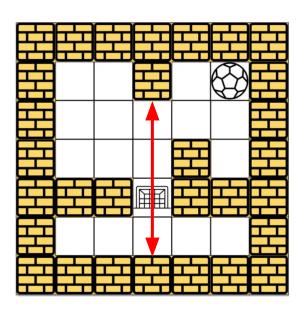
Ball stops when it hits the wall



Will the ball reach the goal?









Legged Robot

S Wheeled Robot

- Moves one cell at a time
- Directions are Right -> Left -> Up -> Down



- Moves in a direction until it hits the wall
- Directions it can move are Right ->
 Left -> Up -> Down

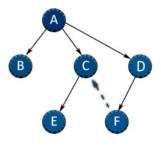


Depth First Traversal

VS Breadth First Traversal

- Uses a top down approach to reach the destination.
- Uses Stack Data Structure which follows Last In First Out (LIFO) approach

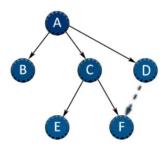
DFS



ADFCEB

- Uses left right (horizontal) approach to reach the destination.
- Uses Queue Data Structure which follows First in First Out (FIFO) approach

BFS

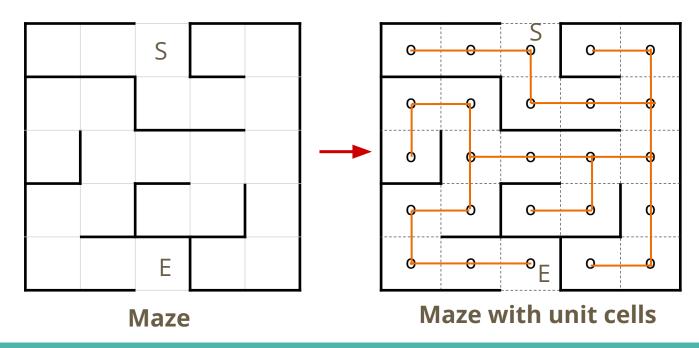


ABCDEF

Image credits: DFS vs BFS Algorithms for Graph Traversal

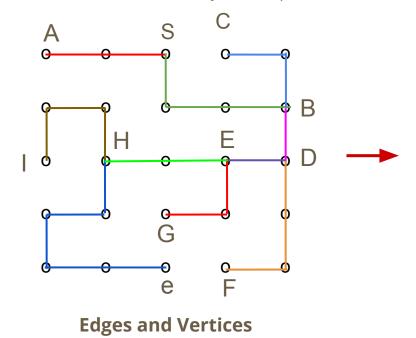
Approach 1: Depth First Traversal

- Consider the maze as a grid
- Convert the maze into unit cells and connect the nodes as shown in the figure below

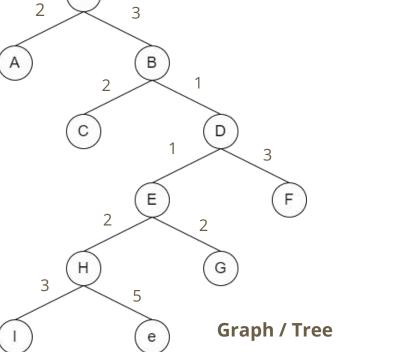


Approach 1: Depth First Traversal

- Each grid cell can be considered as the node of the graph
- Each wall in the maze represents edge of the graph
- Each vertex of the graph is connected to its neighbor
- Label the vertex at every branch point

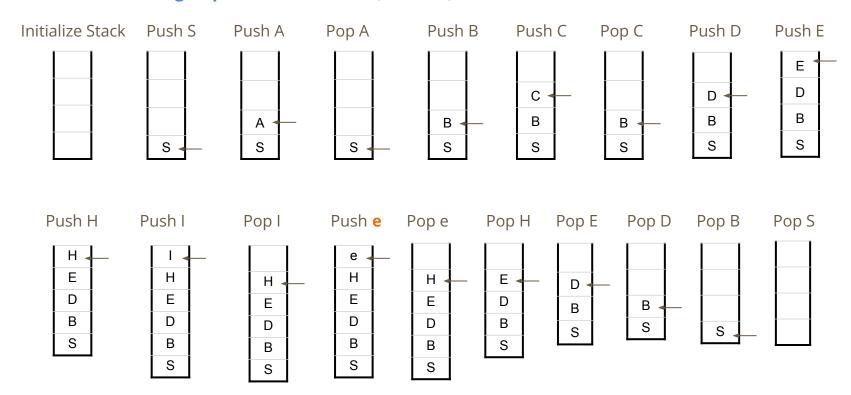


Add unit cells to calculate the weight of the edge

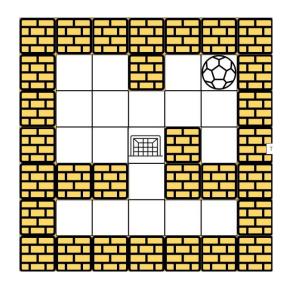


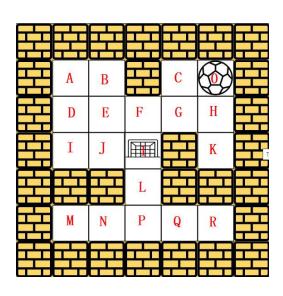
Approach 1: Depth First Traversal Using Legged Robot

Find e using Depth First Traversal (Vertical). Use Stack Data Structure



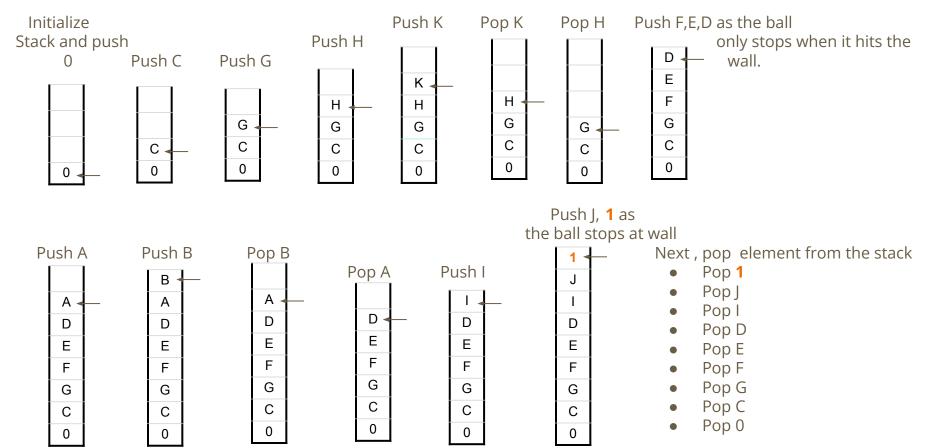
Approach 1: Depth First Traversal Using Wheeled Robot





- Will the ball reach the goal when using a Wheeled Robot approach to solve the problem?
- Source = 0 , Destination = 1

Approach 1: Depth First Traversal Using Wheeled Robot



Pseudo Code Using DFT

- Initialize an empty stack to keep track of positions to explore for DFT.
- Use a list of directions (Right: (1,0), Left: (-1,0), Up: (0,1), Down: (0,-1)) to iterate through each possible direction.
- Push the starting position onto the stack. Initialize an empty set to keep track of visited positions. Add the starting position to the set of visited positions.
- While the stack is not empty, pop the top position from the stack. Extract the row and column from the position.
- Through each direction, initialize new_row and new_col to the current position.
- If it's possible to move in the current direction without hitting a wall, update new_row and new_col accordingly. Once the loop ends, create a new position (new_pos) with the updated row and column.
- If the new position is the destination, return True.
- If the new position has not been visited, add it to the set of visited positions.
 Push it onto the stack for further exploration.
- If the loop completes without finding the destination, return False.

Python Code Using DFT

```
from collections import defaultdict
class Solution:
   def hasPath(self, maze: list[list[int]], start: list[int], destination: list[int]) -> bool:
        stack = []
        stack.append(start)
       dirs = [[1,0],[-1,0],[0,1],[0,-1]]
       visited = defaultdict()
       visited[str(start)] = True
        while stack:
           pos = stack.pop()
           row = pos[0]
           col = pos[1]
            for direction in dirs:
                new row = row
                new col = col
                while new row + direction[0] >= 0 and new col + direction[1] >= 0 and new row + direction[0] < len(maze) and
new_col + direction[1] < len(maze[0]) and maze[new_row + direction[0]][new_col + direction[1]] != 1:</pre>
                    new row = new row + direction[0]
                    new col = new col + direction[1]
                new pos = [new row,new col]
                if new pos[0] == destination[0] and new pos[1] == destination[1]:
                    return True
                if str(new pos) not in visited:
                    visited[str([new row, new col])] = True
                    stack.append(new pos)
        return False
```

Input: maze = [[0,0,1,0,0],[0,0,0,0,0],[0,0,0,1,0],[1,1,0,1,1],[0,0,0,0,0]], start = [0,4], destination = [4,4]

Output: true

Explanation: One possible way is: left -> down -> left -> down -> right -> down -> right.

```
sol = Solution()
29
     output = sol.hasPath([[0,0,1,0,0],[0,0,0,0,0],[0,0,0,1,0],[1,1,0,1,1],[0,0,0,0,0]],[0,4],[4,4])
     #output = sol.hasPath([[0,0,1,0,0],[0,0,0,0,0],[0,0,0,1,0],[1,1,0,1,1],[0,0,0,0,0]],[0,4],[3,2])
30
     #output = sol.hasPath([[0,0,0,0,0],[1,1,0,0,1],[0,0,0,0,0],[0,1,0,0,1],[0,1,0,0,0]],[4,3],[0,1])
31
     print(f"Will the ball reach the destination ?", output)
32
33
PROBLEMS
                  DFBUG CONSOLE
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  a/Local/Microsoft/WindowsApps/python3.12.exe "c:/Users/kavis/OneDrive/Documents/Trimester 2 Jan 24 - April 24/Practical Applications of
  Algorithms/Project/490 Maze DFT.py"
  Will the ball reach the destination ? True
  PS C:\Users\kavis\OneDrive\Documents\Trimester 2 Jan 24 - April 24\Practical Applications of Algorithms\Project>
```

Input: maze = [[0,0,1,0,0],[0,0,0,0,0],[0,0,0,1,0],[1,1,0,1,1],[0,0,0,0,0]], start = [0,4], destination = [3,2]

Output: false

Explanation: There is no way for the ball to stop at the destination. Notice that you can pass through the destination but you cannot stop there.

```
sol = Solution()
     #output = sol.hasPath([[0,0,1,0,0],[0,0,0,0],[0,0,0,1,0],[1,1,0,1,1],[0,0,0,0,0]],[0,4],[4,4])
     output = sol.hasPath([[0,0,1,0,0],[0,0,0,0,0],[0,0,0,1,0],[1,1,0,1,1],[0,0,0,0,0]],[0,4],[3,2])
30
     #output = sol.hasPath([[0,0,0,0,0],[1,1,0,0,1],[0,0,0,0,0],[0,1,0,0,1],[0,1,0,0,0]],[4,3],[0,1])
     print(f"Will the ball reach the destination ?", output)
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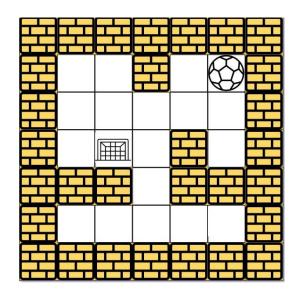
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  a/Local/Microsoft/WindowsApps/python3.12.exe "c:/Users/kavis/OneDrive/Documents/Trimester 2 Jan 24 - April 24/Practical Applications of
  Algorithms/Project/490 Maze DFT.pv"
  Will the ball reach the destination ? False
  PS C:\Users\kavis\OneDrive\Documents\Trimester 2 Jan 24 - April 24\Practical Applications of Algorithms\Project>
```

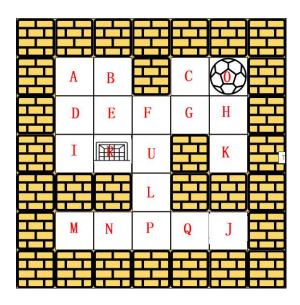
Input: maze = [[0,0,0,0,0],[1,1,0,0,1],[0,0,0,0,0],[0,1,0,0,1],[0,1,0,0,0]], start = [4,3], destination = [0,1]

Output: false

```
sol = Solution()
    \text{#output} = \text{sol.hasPath}([[0,0,1,0,0],[0,0,0,0,0],[0,0,0,1,0],[1,1,0,1,1],[0,0,0,0,0]],[0,4],[4,4])
    #output = sol.hasPath([[0,0,1,0,0],[0,0,0,0,0],[0,0,0,1,0],[1,1,0,1,1],[0,0,0,0,0]],[0,4],[3,2])
    output = sol.hasPath([[0,0,0,0,0],[1,1,0,0,1],[0,0,0,0,0],[0,1,0,0,1],[0,1,0,0,0]],[4,3],[0,1])
    print(f"Will the ball reach the destination ?", output)
ROBLEMS
        OUTPUT
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 a/Local/Microsoft/WindowsApps/python3.12.exe "c:/Users/kavis/OneDrive/Documents/Trimester 2 Jan 24 - April 24/Practical Applications of
 Algorithms/Project/490 Maze DFT.pv"
 Will the ball reach the destination ? False
 PS C:\Users\kavis\OneDrive\Documents\Trimester 2 Jan 24 - April 24\Practical Applications of Algorithms\Project>
```

Approach 2: Breadth First Traversal





- Will the ball reach the goal when using a Wheeled Robot approach to solve the problem?
- Source = 0 , Destination = R

Approach 2: Breadth First Traversal Using Legged Robot

Visited: 0

Queue: (empty) Initialize an queue

Visited: 0

Queue: 0

a. Add 0 to Queue

b. Mark 0 as visited

Visited: 0

1

Queue: Print: 0

a. Remove 0 from Queue

b. Print 0

Visited: 0 C H

Queue: C H Print: 0

a. Add C,H to Queue

b. Mark C, H visited

Visited: 0 C H

111

Queue: H Print: 0 C

a. Remove C from Queue

b. Print C

Visited: 0 C H G

1111

Queue: H G Print: 0 C

a. Add G to the Queue

b. Mark G as visited

Visited: 0 C H G

1111

Queue: G Print: 0 C H

a. Remove H from Queue

b. Print H

Visited: 0 C H G H

11111

Queue: G K Print: 0 C H

a. Add K to the Queue

b. Mark K as visited

Visited: 0 C H G H 1 1 1 1 1

Queue: K Print: 0 C H G

a. Remove G from Queue

b. Print G

Visited: 0 C H G H F 1 1 1 1 1 1

Queue: K F Print: 0 C H G

a. Add F to the Queue

b. Mark F as visited

Approach 2: Breadth First Traversal Using Legged Robot

Visited: 0 C H G H F 111 1 1 1

Queue: F Print: 0 C H G K

- a. Remove K from Queue
- b. Print K

Visited: 0 C H G H F

Queue: Print: 0 C H G K F

- a. Remove F from Queue
- b. Print F

Visited: 0 C H G H F E U

Queue: EU Print: 0 C H G K F

- a. Add E, U to the Queue
- b. Mark E, U as visited

Visited: 0 C H G H F E U

Queue: U Print: 0 C H G K F E

- a. Remove E from the Queue
- b. Print E

Visited: 0 C H G H F E U D B R

Queue: U D B R Print: 0 C H G K F E

a. Add D, B, R to the Queueb. Mark D, B, R as visited

Visited: 0 C H G H F E U D B R 1111111111111

Queue: DBR Print: 0CHGKFEU

- a. Remove U from the Queue
- b. Print U

Visited: 0 C H G H F E U D B R L

Queue: DBR Print: 0CHGKFEU

- a. Add L to the Queue
- b. Mark L as visited

Approach 2: Breadth First Traversal Using Legged Robot

Visited: 0 C H G H F E U D B R L 111 1 1 1 1 1 1 1 1 1

Queue: BRL Print: 0 CHGKFEUD

- a. Remove D from the Queue
- b. Print D

Visited: 0 C H G H F E U D B R L A I

Queue: R L A I Print: 0 C H G K F E U D B

- a. Remove B from the Queue
- b. Print B

Visited: 0 C H G H F E U D B R L A I

Queue: BRLAIPrint: 0 CHGKFEUD

- a. Add A, I to the Queue
- b. Mark A,I as visited

Visited: 0 C H G H F E U D B R L A I

Queue: R L A I Print: 0 C H G K F E U D B R

- a. Remove R from the Queue
- b. Print R

Approach 2: Breadth First Traversal Using Wheeled Robot

Visited: 0

Queue: (empty) Initialize an queue Visited: 0

1

Queue: 0

a. Add 0 to Queue

Mark 0 as visited

Visited: 0

Queue: Print: 0

a. Remove 0 from Queue

b. Print 0

Visited: 0 C K

Queue: C K Print: 0

a. Add C,K to Queue

b. Mark C, K visited

Visited: 0 C K

111

Queue: K Print: 0 C

a. Remove C from Queue

b. Print C

Visited: 0 C K G

1111

Queue: K G Print: 0 C

a. Add G to the Queue

b. Mark G as visited

Visited: 0 C K G

11111

Queue: G Print: 0 C K

a. Remove K from Queue

b. Print K

Visited: 0 C K G

1111

Queue: Print: 0 C K G

a. Remove G from Queue

b. Print G

Visited: 0 C K G D

11111

Queue: D Print: 0 C K G

a. Add D to the Queue

b. Mark D visited

Visited: 0 C K G D

11111

Queue: Print: 0 C K G D

a. Remove D from Queue

b. Print D

Approach 2: Breadth First Traversal Using Wheeled Robot

Visited: 0 C K G D A I
111111

Oueue: A I Print: 0 C K G D

- a. Add A, I to the Queue
- b. Mark A, I as visited

Visited: 0 C K G D A I 11111111

Queue: I Print: 0 C K G D A

- a. Remove A from Queue
- b. Print A

Visited: 0 C K G D A I B 111 1 1111

Queue: I B Print: 0 C K G D A

- a. Add B to the Queue
- b. Mark B as visited

Visited: 0 C K G D A I B 111 1 1111

Queue: B Print: 0 C K G D A I

- a. Remove I from the Queue
- b. Print I

Visited: 0 C K G D A I B U 111111111

Queue: B U Print: 0 C K G D A I

- a. Add U to the queue
- b. Mark U as visited

Visited: 0 C K G D A I B U 11111111

Queue: U Print: 0 C K G D A I B

- a. Remove B from the queue
- b. Print B

Visited: 0 C K G D A I B U R 111 1 1 1111 1

Queue: UR Print: 0 C K G D A I B

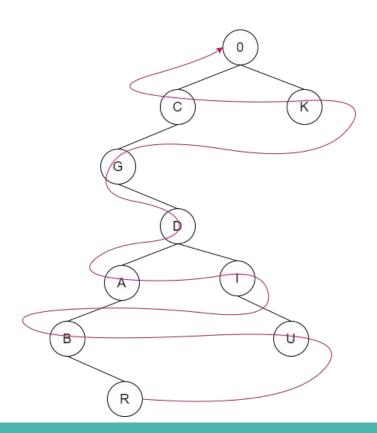
- a. Add **R** to the queue
- b. Mark R as visited

Visited: 0 C K G D A I B U R 111111111

Queue: Print: 0 C K G D A I B U R

- a. Remove U , Print U
- b. Next Remove R and Print R

Approach 2: Breadth First Traversal Using Wheeled Robot



 This is the part of the full tree which represents the path from source 0 to destination R

Pseudo Code for BFT

- Create a queue to perform BFS traversal.
- Use a list of directions (Right: (1,0), Left: (-1,0), Up: (0,1), Down: (0,-1)) to iterate through each possible direction.
- Maintain a dictionary called visited to keep track of visited positions.
- If the queue is not empty, dequeue first position and explore all possible directions from that dequeued position.
- Move in each direction until ball hits a wall.
- If the new position after movement is the destination, return True.
- Otherwise, if the new position hasn't been visited yet, mark it as visited and enqueue it.
- If no path is found after exploring all possible paths, return False.

Python Code Using BFT

```
from collections import deque, defaultdict
class Solution:
   def hasPath(self, maze: list[list[int]], start: list[int], destination: list[int]) -> bool:
        queue = deque()
        queue.append(tuple(start))
        dirs = [[1, 0], [-1, 0], [0, 1], [0, -1]]
        visited = defaultdict(bool)
        while queue:
            row, col = queue.popleft()
            for direction in dirs:
                new row, new col = row, col
                while 0 <= new row + direction[0] < len(maze) and 0 <= new col + direction[1] < len(maze[0]) and maze[new row +
direction[0]][new col + direction[1]] != 1:
                   new row += direction[0]
                   new col += direction[1]
                new pos = (new row, new col)
                if new pos == tuple(destination):
                    return True
                if not visited[new pos]:
                    visited[new pos] = True
                    queue.append(new pos)
```

Input: maze = [[0,0,1,0,0],[0,0,0,0,0],[0,0,0,1,0],[1,1,0,1,1],[0,0,0,0,0]], start = [0,4], destination = [4,4]

Output: true

Explanation: One possible way is: left -> down -> left -> down -> right -> down -> right.

```
sol = Solution()
     output = sol.hasPath([[0,0,1,0,0],[0,0,0,0],[0,0,0,1,0],[1,1,0,1,1],[0,0,0,0,0]],[0,4],[4,4])
     #output = sol.hasPath([[0,0,1,0,0],[0,0,0,0],[0,0,0,1,0],[1,1,0,1,1],[0,0,0,0,0]],[0,4],[3,2])
     #output = sol.hasPath([[0,0,0,0,0],[1,1,0,0,1],[0,0,0,0,0],[0,1,0,0,1],[0,1,0,0,0]],[4,3],[0,1])
     print(f"Will the ball reach the destination (BFS) ?", output)
                                                                                                                                   ^ X
                 DEBUG CONSOLE
         OUTPUT
                                TERMINAL

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PS C:\Users\kavis\OneDrive\Documents\Trimester 2 Jan 24 - April 24\Practical Applications of Algorithms\Project> & C:/Users/kavis/AppDat
 a/Local/Microsoft/WindowsApps/python3.12.exe "c:/Users/kavis/OneDrive/Documents/Trimester 2 Jan 24 - April 24/Practical Applications of
 Algorithms/Project/490 Maze BFT.py"
 Will the ball reach the destination (BFS) ? True
 PS C:\Users\kavis\OneDrive\Documents\Trimester 2 Jan 24 - April 24\Practical Applications of Algorithms\Project>
```

Input: maze = [[0,0,1,0,0],[0,0,0,0,0],[0,0,0,1,0],[1,1,0,1,1],[0,0,0,0,0]], start = [0,4], destination = [3,2]

Output: false

Explanation: There is no way for the ball to stop at the destination. Notice that you can pass through the destination but you cannot stop there.

```
sol = Solution()
     #output = sol.hasPath([[0,0,1,0,0],[0,0,0,0,0],[0,0,0,1,0],[1,1,0,1,1],[0,0,0,0,0]],[0,4],[4,4])
     output = sol.hasPath([[0,0,1,0,0],[0,0,0,0,0],[0,0,0,1,0],[1,1,0,1,1],[0,0,0,0,0]],[0,4],[3,2])
     #output = sol.hasPath([[0,0,0,0,0],[1,1,0,0,1],[0,0,0,0],[0,1,0,0,1],[0,1,0,0,0]],[4,3],[0,1])
     print(f"Will the ball reach the destination (BFS) ?", output)
ROBLEMS
                  DEBUG CONSOLE
                                 TERMINAL
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PS C:\Users\kavis\OneDrive\Documents\Trimester 2 Jan 24 - April 24\Practical Applications of Algorithms\Project> cd "c:/Users/kavis/OneD
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PS C:\Users\kavis\OneDrive\Documents\Trimester 2 Jan 24 - April 24\Practical Applications of Algorithms\Project> & C:/Users/kavis/AppDat
 a/Local/Microsoft/WindowsApps/python3.12.exe "c:/Users/kavis/OneDrive/Documents/Trimester 2 Jan 24 - April 24/Practical Applications of
 Algorithms/Project/490 Maze BFT.py"
 Will the ball reach the destination (BFS) ? False
 PS C:\Users\kavis\OneDrive\Documents\Trimester 2 Jan 24 - April 24\Practical Applications of Algorithms\Project>
```

Input: maze = [[0,0,0,0,0],[1,1,0,0,1],[0,0,0,0,0],[0,1,0,0,1],[0,1,0,0,0]], start = [4,3], destination = [0,1]

Output: false

```
sol = Solution()
     #output = sol.hasPath([[0,0,1,0,0],[0,0,0,0,0],[0,0,0,1,0],[1,1,0,1,1],[0,0,0,0,0]],[0,4],[4,4])
     #output = sol.hasPath([[0,0,1,0,0],[0,0,0,0,0],[0,0,0,1,0],[1,1,0,1,1],[0,0,0,0,0]],[0,4],[3,2])
     output = sol.hasPath([[0,0,0,0,0],[1,1,0,0,1],[0,0,0,0,0],[0,1,0,0,1],[0,1,0,0,0]],[4,3],[0,1])
     print(f"Will the ball reach the destination (BFS) ?", output)
ROBLEMS
                  DEBUG CONSOLE
                                TERMINAL
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PS C:\Users\kavis\OneDrive\Documents\Trimester 2 Jan 24 - April 24\Practical Applications of Algorithms\Project> cd "c:/Users/kavis/OneD
 rive/Documents/Trimester 2 Jan 24 - April 24/Practical Applications of Algorithms/Project"
PS C:\Users\kavis\OneDrive\Documents\Trimester 2 Jan 24 - April 24\Practical Applications of Algorithms\Project> & C:/Users/kavis/AppDat
 a/Local/Microsoft/WindowsApps/python3.12.exe "c:/Users/kavis/OneDrive/Documents/Trimester 2 Jan 24 - April 24/Practical Applications of
 Algorithms/Project/490 Maze BFT.py"
 Will the ball reach the destination (BFS) ? False
 PS C:\Users\kavis\OneDrive\Documents\Trimester 2 Jan 24 - April 24\Practical Applications of Algorithms\Project>
```

Next steps...

- If the maze is very large, **DFS** is indeed preferred over BFS. Based on the size of the maze, either of the algorithms will be preferred.
- If the problem is modified to find the shortest path, only BFS gives the right answer.
- Other algorithms like A* and Dijkstra can be explored.

Summary

- Both BFS and <u>DFS</u> have same big O time complexity (<u>O(N*M)</u>) (N, M are rows and columns in the maze)
- **BFS** will generally use **more memory** since it keeps track of all the paths from the visited nodes, while <u>DFS</u> keeps track of <u>only one path</u> at a time.
- BFS will give the shortest path while <u>DFS</u> gives <u>a path</u> (not necessarily shortest one).

References

- Difference between BFS and DFS GeeksforGeeks
- Wheels Are Better Than Feet for Legged Robots IEEE Spectrum
- Leet Code 490. The Maze Explained Python3 Solution | by Edward Zhou | Tech Life & Fun |
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