

$$\frac{\partial x}{\partial \theta} \cdot e^{-\frac{x^2}{\theta}}$$

$$\rightarrow \ln\left(\frac{\partial x}{\partial \theta}\right) + \ln\left(e^{-\frac{x^2}{\theta}}\right)$$

$$\ln\left(\frac{\partial x}{\partial \theta}\right) - \frac{x^2}{\theta}$$

$$\rightarrow \ln[2x \cdot \theta]^{-1} = -\ln(2x \cdot \theta)$$

$$-\ln(2x \cdot \theta) - \frac{x^2}{\theta} \rightarrow -\ln(2x) - \ln(\theta) - \frac{x^2}{\theta}$$

$$-(n) \ln(2x) - (n) \ln(\theta) - \frac{x^2}{\theta} - \dots$$

$$\frac{x_n^2}{\theta} - \dots$$

$$\rightarrow \frac{1}{n} + \frac{1}{\theta} [x^2 + \dots + x_n^2] = 0$$

$$\frac{\partial}{\partial \theta} = -\frac{1}{\theta} + \frac{x^2}{\theta^2} + \dots + \frac{x_n^2}{\theta^2}$$

$$-n + \frac{1}{\theta} [x^2 + \dots + x_n^2] \rightarrow n = \frac{1}{\theta} [x^2 + \dots + x_n^2] \rightarrow \theta = \frac{x^2 + \dots + x_n^2}{n}$$

$$\theta = \frac{0.9^2 + 0.5^2 + 1^2}{3} = 0.5$$