

# Multi-view Laplacian Least Squares For Human Emotion Recognition

Shuai Guo<sup>a</sup>, Lin Feng<sup>a,\*</sup>, Zhan-Bo Feng<sup>b</sup>, Yi-Hao Li<sup>b</sup>, Yang Wang<sup>a</sup>, Sheng-Lan Liu<sup>a</sup>, Hong Qiao<sup>c</sup>

<sup>a</sup>*School of Innovation and Entrepreneurship, Dalian University of Technology, Dalian 116024, China*

<sup>b</sup>*School of Electronic Information and Electrical Engineering, Dalian University of Technology, Dalian 116024, China*

<sup>c</sup>*State Key Laboratory of Management and Control for Complex Systems, Institute of Automation, Chinese Academy of Sciences, Beijing 100190, China*

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## Abstract

Human emotion recognition is an emerging and important area in the field of human-computer interaction and artificial intelligence, which has been more and more related with multi-view learning methods. Subspace learning is an important direction of multi-view learning. However, most existing subspace learning methods could not make full use of both category discriminant information and local neighborhood information. As a typical subspace learning method, PLS performs better and more robustly than many other subspace learning methods, because PLS is optimized with iteration method. However, PLS suffers from linear relationship assumption and two-view limitation. In this paper, a new nonlinear multi-view laplacian least squares (MvLLS) is proposed. MvLLS constructs a global laplacian weighted graph (GLWP) to introduce category discriminant information as well as protect the local neighborhood information. Optimized with iteration method, MvLLS is a multi-view extension of PLS. The proposed method has great extendibility and robustness. To meet the requirements of large-scale applications, weighted local preserving embedding (WLPE) is proposed as the out-of-sample extension of MvLLS, based on the idea of maintaining the manifold structures of original space. Finally, the proposed method

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\*Corresponding author  
Email address: [fenglin@dlut.edu.cn](mailto:fenglin@dlut.edu.cn) (Lin Feng)

is verified on three multi-view emotion recognition tasks, the experiment results validate the effectiveness and robustness of MvLLS.

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## 1. Introduction

Human emotion recognition is a long-standing and emerging problem in computer vision and human-computer interaction, where there have been many significant researches. Most early human emotion recognition researches focused on single view learning methods, such as image-based face emotion recognition [1], video-based body emotion recognition [2, 3], speech emotion recognition [4], and physiological signal emotion recognition [5, 6, 7]. However, human emotion can be observed at various viewpoints, even by different sensors. Recently, many multi-view human emotion recognition methods [8, 9, 10] are proposed to learn feature from each view effectively and improve the recognition accuracy. One effective approach of multi-view learning is subspace learning [11, 12], which aims at getting a common subspace shared by various views. Generally speaking, subspace learning based multiview learning methods can be divided into three categories according to their key ideas:

*Maximize the cross correlations.* This line of methods mainly come from canonical correlation analysis (CCA) [13], which attempts to learn two linear transforms for each view to maximize their cross correlation in the subspace. Kernel CCA (KCCA) [14], multiview CCA (MCCA) [15] are the kernel and multiview extensions of CCA respectively. Partial least squares (PLS) [16] uses iterative method and least square regression to approximate a optimization problem that is similar to CCA, but with different constraints. The kernel version of PLS is introduced in [17]. And a single optimization termed method SVM-2K that combines SVM and KCCA is proposed in [18]. Multi-view SVM-2K [19] presents a multi-view modification for SVM-2K. In addition, a nonparametric

25 sparse matrix and automatic model is proposed for multi-feature fusion in [20],  
by imposing label information across all views to exploit the correlations. Recently, a hierarchical multi-view multi-feature fusion method (HMMF) [21] is  
proposed by using a sparse covariance matrix to represent the correlations over  
all views. However, HMMF has a great spatiotemporal complexity.

30 *Balance the scatter discriminant information.* Inspired by linear discriminant analysis (LDA) [22], the scatter discriminant information of multi-view learning refers chiefly to within-class, between-class, intra-view or inter-view discriminants. Protecting the discriminant structure contributes to get samples of the same class together and separate samples of different classes. Correlation  
35 discriminant analysis (CDA) [23] is a supervised improvement of CCA based on the definitions of within-class correlation and between-class correlation. A generalized multi-view analysis framework (GMA) which considers the intra-view discriminant information in the common subspace is proposed in [24]. Multi-view discriminant analysis (MvDA) [25] gets a linear transform for each view by  
40 maximizing the between-class variations and minimizing the within-class variations across all views. And MvDA-VC [25] is proposed based on MvDA by adding view-consistency. Besides, multi-view uncorrelated discriminant analysis (MULDA) [26] combines uncorrelated LDA [27] with CCA to preserve both category discriminant information and correlation information. A generalized  
45 multi-view embedding method (GME) [28] is proposed for CCA, PLS and LDA, using intrinsic and penalty graphs to characterize the intra-view and inter-view discriminant information. And laplacian multi-set canonical correlations (LaM-CCs) [29] constructs the nearest neighbor graphs to take intra-view and inter-view correlations into consideration. Multi-view local discrimination and canonical correlation analysis (MLDC<sup>2</sup>A) [30] aims at optimizing a combination of  
50 between-class scatter, within-class scatter and correlation.

*Protect the local neighborhood information.* Protecting the local characteristics would help in maintaining the manifold structures. Multi-view spectral embedding (MSE) is developed to obtain a smooth low-dimensional embedding  
55 across multiple views in [31]. And locality-preserving CCA (LPCCA) [32] inte-

grates the local neighborhood information together with CCA to discover the low-dimensional manifold structures for different views. To solve the problem of large pose variations and facial expression recognition, locality-constrained linear coding is utilized to construct the model in [33]. A graph regularized multi-set canonical correlations (GrMCC) [34] is proposed to utilize discriminative and intrinsic geometrical information under the framework of correlation analysis. Recently, noticing that Hessian can exploit the intrinsic local geometry of data, Hessian multiset CCA [35] shows superior extrapolating capability with nonlinear multi-view features.

Note that some of these methods may have more than two of the three ideas mentioned above, they are still classified with the most important idea.

### 1.1. Motivations

Although many significant subspace learning methods have been proposed, there is still much room for improvement. The main motivations of this paper are elaborated as follows:

- (1) There are few methods could balance the scatter discriminant information as well as protect the local neighborhood information. For example, GMA and MULDA just consider the cross correlations and the scatter discriminant information. MvDA maximizes the between-class variation and minimizes the within-class variation, but breaks the unity of each view. LPCCA and GrMCC integrate the cross correlations and local neighborhood information. In this paper, MvLLS constructs a global weighted graph GLWP to protect the local neighborhood information, and introduces the category discriminant information.
- (2) PLS get much better performance in practical applications compared with CCA, even they have similar optimization targets. This may boils down to the iteration method and regression method used in PLS. However, traditional PLS suffers from the basic assumption that latent linear relationships exist between different views, and the basic framework of PLS is difficult

85 to extend to more views. In this paper, MvLLS abandons the linear relationship assumption of PLS, maintains the advantages of iteration method, and extends PLS to multi-view learning. MvLLS can work on the cases that category information or features of some samples in particular views are missed, even on semi-supervised or unsupervised mood.

## 90 1.2. Contributions

In this paper, we present a nonlinear multi-view laplacian least squares (MvLLS) method for the human emotion recognition. The main contributions and characteristics of our work are summarized as below:

- 95 (1) Inspired by LE, a global laplacian weighted graph (GLWP) is constructed across all views, where the local neighbor information is maintained and category discriminant information is introduced. Moreover, the global weighted graph is not only insensitive to the missing of part samples or labels, but also easy to extend to more views. GLWP makes MvLLS easily to perform the semi-supervised or unsupervised tasks.
- 100 (2) Traditional PLS is upgraded to a supervised, nonlinear and multi-view modification MvLLS. Having abandoned the basic assumption that latent linear relationships exist between views, MvLLS gets a score vector of subspace in each iteration with GLWP. Specially, as GLWP upgrades after each iteration, we could predict the intrinsic dimension of the subspace as GLWP tends to be stable.
- 105 (3) To accommodate the large-scale applications, an out-of-sample method weighted local preserving embedding (WLPE) is presented to process the new samples. WLPE represents each new sample with weighted sum of its neighbors. The neighbors that connected with more samples are expected to have higher weights. Afterwards, the embeddings of new samples are regarded  
110 as weighted sum of embeddings of their neighbors.

### 1.3. Organization

The remainder of this paper is organized as below: Section 2 defines the common notations and review some related works. Then Section 3 introduces the formulations and optimizations of MvLLS in detail, as well as some extensions. After that, Section 4 presents the experimental results as well as quantitative evaluations, followed with a conclusion.

## 2. Related works

In this section, common notations used throughout this paper are defined firstly. Then some researches that are related to our work are introduced, including PCA, CCA, LE, PLS and MvDA.

### 2.1. Notations

Given samples of various different views and their labels. For each view, subspace learning methods expect to learn a low-dimensional embedding in the common subspace. Important notations in this paper are listed in Table 1:

When we refer to single-view learning methods, the view  $X \in \mathbb{R}^{d \times n}$  is used. And when we refer to methods that require the equality of number of samples,  $n$  is used instead of  $n_i$ . In some other specific situations, we would remove upper and lower corner markers as needed.

### 2.2. PCA and CCA

PCA [36] is a classical dimensional reduction (DR) and single view learning method. With normalization as the first step, PCA finds a group of standard orthogonal basis to maximum the variance of view  $X$  after projection, which can be transformed as the trace of covariance matrix of projection of  $X$ :

$$\begin{aligned} & \max_w w^T X X^T w \\ & s.t. \ w^T X X^T w = 1 \end{aligned} \tag{1}$$

Table 1: Definitions of important notations

Notation	Description
$X_i \in \mathbb{R}^{d_i \times n_i}$	All $n_i$ samples of $i^{th}$ view
$Label_i \in \mathbb{R}^{n_i}$	Labels that correspond to samples in $X^i$
$x_{ia}, x_{jb} \in \mathbb{R}^d$	The $a^{th}$ and $b^{th}$ of view $X_i$ and $X_j$
$label_{ia}, label_{jb}$	The labels of $x_{ia}$ and $x_{jb}$
$v$	The number of views
$c$	The number of class across all views
$dim$	The number of dimension of the subspace
$w_i \in \mathbb{R}^{d_i}$	A basic vector of the linear transform of $X_i$
$Y_i \in \mathbb{R}^{dim \times n_i}$	The embedding of $X_i$ in the subspace
$y_{ia}, y_{jb} \in \mathbb{R}^{dim}$	The embeddings of $x_{ia}$ and $x_{jb}$
$y^i \in \mathbb{R}^{n_i} \ y^j \in \mathbb{R}^{n_j}$	A basic vector of $Y_i$ and $Y_j$
$W_{ab}^{ij}$	The weight of connection between $x_{ia}$ and $x_{jb}$
$I$	The identity matrix
$tr(X)$	Trace of matrix $X$

135 CCA [13] is a two-view learning method that attempts to find two linear transforms  $w_1$  and  $w_2$  for the normalized feature matrices  $X_1$  and  $X_2$ , such that their embeddings in the common subspace are most correlated:

$$\begin{aligned}
& \max_{w_1, w_2} w_1^T X_1 X_2^T w_2 \\
& s.t. \ w_1^T X_1 X_1^T w_1 = 1, w_2^T X_2 X_2^T w_2 = 1
\end{aligned} \tag{2}$$

Eq. (1) and Eq. (2) can be solved by using Lagrange multiplier method. CCA can be regarded as the two-view version of PCA. And one of the main  
140 drawbacks of CCA is that the number of samples of the two views must be equal.

### 2.3. Laplacian eigenmaps

Laplacian Eigenmaps (LE) [37] is an effective single-view nonlinear manifold learning method. Given the  $n$  samples of  $X$ , LE has great locality preserving  
145 properties by constructing a weighted graph  $W$ :

$$W_{ab} = \begin{cases} \exp(-\frac{\|x_a - x_b\|_2^2}{t}), & \text{if } \|x_a - x_b\|_2^2 < \epsilon \\ 0, & \text{else} \end{cases} \quad (3)$$

In  $W$ , the neighboring samples are connected with weighted edges to record the locality information. Let  $y_a$  and  $y_b$  denote the low-dimensional representation of  $a^{th}$  and  $b^{th}$  sample, LE maps the weighted graph  $W$  to a low-dimensional space with connected samples stay as close together as possible:

$$\begin{aligned} \min_Y \frac{1}{2} \sum_{a,b} \|y_a - y_b\|_2^2 W_{ab} &= \min_Y \text{tr}(Y^T L Y) \\ \text{s.t. } Y^T D Y &= I \\ D_{kk} &= \sum_{j=1}^n W_{jk}, \quad L = D - W \end{aligned} \quad (4)$$

150 In Eq. (4),  $D$  is a diagonal matrix and  $L$  is the laplacian matrix. This equation can be solved by computing eigenvalues and eigenvectors of a generalized eigenvector problem.

### 2.4. Partial least squares

Partial least squares regression (PLS) [16] has similar optimization target  
155 to CCA, it can be regarded as a linear unsupervised two-view learning method. Traditional PLS maximizes the correlation of the two views after projection. PLS supposes that the two views can be driven by a few latent variables, which are not directly observed or measured. PLS uses iterative method to predict  $X_2$  with  $X_1$  by finding the component of  $X_1$  and using it as the regressor of  
160 both views. After each iteration step,  $X_1$  and  $X_2$  are covered by the residual matrices  $E$  and  $F$ :



$$\begin{aligned}
\max_{w_1, w_2} y_1 y_2^T &= \max_{w_1, w_2} w_1^T X_1 X_2^T w_2 \\
s.t. \quad w_1^T w_1 &= 1, w_2^T w_2 = 1 \\
X_1 &= P^T Y_1 + E \\
X_2 &= Q^T Y_2 + F \\
Y_2 &= D Y_1 + H
\end{aligned} \tag{5}$$

PLS supposes  $X_1$  and  $X_2$  have the same number of samples like CCA, that is  $n_1 = n_2 = n$ . In Eq. (5),  $P \in \mathbb{R}^{dim \times d_1}$ ,  $Q \in \mathbb{R}^{dim \times d_2}$  are the loading matrices.  $E \in \mathbb{R}^{d_1 \times n}$ ,  $F \in \mathbb{R}^{d_2 \times n}$  and  $H \in \mathbb{R}^{dim \times n}$  are the residual matrices. And  $D \in \mathbb{R}^{dim \times dim}$  shows the latent scores of two views. But in the cross-view classification problems, the latent linear relationship between different views do not always exist.

### 2.5. Multi-view discriminant analysis

Inspired by LDA [22], the main idea of MvDA [25] is to find  $v$  linear transforms to project samples of all views to a common subspace, where the between-class variation  $S_B^y$  is maximized and the within-class variation  $S_W^y$  is minimized.

$$\begin{aligned}
&\max_{w_1, \dots, w_v} \frac{tr(S_B^y)}{tr(S_W^y)} \\
S_W^y &= \sum_{i=1}^v \sum_{j=1}^c \sum_{k=1}^{n_{ij}} (y_{ijk} - \mu_j)(y_{ijk} - \mu_j)^T \\
S_B^y &= \sum_{i=1}^c n_i (\mu_i - \mu)(\mu_i - \mu)^T
\end{aligned} \tag{6}$$

where  $n_{ij}$  is the number of samples that are labeled as  $j$  in  $X_i$ ,  $y_{ijk}$  is the label of  $k^{th}$  sample in  $X_i$  that is labeled as  $j$ ,  $\mu_j$  is the mean of low-dimensional embeddings of all samples in the  $v$  views that are labeled as  $j$ , and  $\mu$  is the mean of low-dimensional embeddings of all samples in the  $v$  views. Supposing that each view can be a flipping of any other one, MvDA-VC is proposed by adding a view-consistency term to the denominator of Eq. (6).

MvDA and MvDA-VC take both between-class and within-class discriminant information into consideration. They can deal with the cases where there are different number of samples or classes for the  $v$  views. However, the integrity and local structure of a single view is broke up, as  $S_W^y$  and  $S_B^y$  are calculated across all views.

### 3. Multi-view laplacian least squares

#### 3.1. Overview

In this section we present the detailed ideas and optimizations of multi-view laplacian least squares (MvLLS), followed with some extensions. Based on the frameworks of LE and PLS, MvLLS is proposed to get the nonlinear subspace embedding of each view directly. MvLLS aims to find a subspace for all views where the connected samples stay as close together as possible. In Section 3.2, the global laplacian weighted graph (GLWP)  $\mathcal{W}$  is constructed over all views. GLWP can not only protect the local geometry structure, but also introduce the category discriminant information. As features of the  $v$  views lie on different dimensions, a DR framework should be applied to make samples of different views measurable. The basic idea and usage of DR framework are shown in Fig. 1. In Section 3.3, inspired by PLS, iteration method and regression method are used to solve the optimization problem. We remove the estimated variations and update  $\mathcal{W}$  in each iteration, the variations are predicted by low-dimensional embeddings of views. In Section 3.4, to accommodate the large-scale applications, an out-of-sample extension method weighted local preserving embedding (WLPE) is introduced to get the embeddings of new samples. WLPE attempts to maintain the high-dimensional local neighborhood information in the subspace. In Section 3.5, some extensions of MvLLS are presented.

The proposed method takes both advantages of scatter discriminant balance and locality protection. With a robust weighted graph, MvLLS can deal with the lack of partial samples or category information. One of the great advantages over other methods is that, MvLLS can also work on unsupervised or semi-supervised

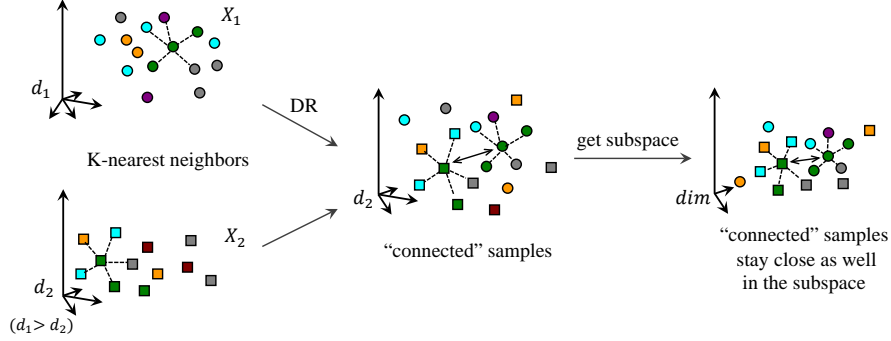


Fig. 1: The basic idea of MvLLS, with  $X_1$  and  $X_2$  as an example. Squares and circulars denote samples from  $X_1$  and  $X_2$  respectively, labels of samples are represented by different colors. PCA is used to get a common space for  $X_1$  and  $X_2$ . Whether samples are connected or not depends on labels of themselves and their neighbors. And the connected samples would stay close as well in the subspace got by MvLLS.

models, even the cases that the number of samples are different for the given views. Moreover, as the weighted graph varies by iteration, the change rate can be used to predict the intrinsic dimension of the subspace got by MvLLS.

### 210 3.2. Global laplacian weighted graph

In this section we construct the global laplacian weighted graph that weights the connections of samples across all views, and get the embeddings of all samples on the first dimension of the subspace, which are  $y^1, \dots, y^v$ . MvLLS tries to find a subspace in which the connected samples of each pair views stay as close together as possible.

We talk about connections between two views firstly, with  $X_i$  and  $X_j$  as an example:

$$\begin{aligned}
 \min_{y^i, y^j} \xi(i, j) &= \frac{1}{2} \sum_{\substack{1 \leq a \leq n_i \\ 1 \leq b \leq n_j}} \|y_{ia} - y_{jb}\|_2^2 W_{ab}^{ij} \\
 &= \frac{1}{2} \sum_{a, b} (y_a^2 + y_b^2 - 2y_a y_b) W_{ab}^{ij}
 \end{aligned} \tag{7}$$

$$\begin{aligned}
&= \text{tr}(Y_i^T L^{ij} Y_j) \\
&= y^i L^{ij} y^{jT} \\
D_{kk} &= \sum_{j=1}^{n_i} W_{jk}, \quad L^{ij} = D - W^{ij}
\end{aligned}$$

In Eq. (7),  $W^{ij} \in \mathbb{R}^{n_i \times n_j}$  is a weighted matrix which measures the weights of connections between samples of  $X_i$  and  $X_j$ ,  $D$  is a diagonal matrix, and  $L^{ij}$  is the laplacian matrix corresponds to  $W^{ij}$ . As the dimensions of the two views are different, DR frameworks are used to project  $X_i$  and  $X_j$  to a common dimension which is the minimum of  $d_i$  and  $d_j$ . And in  $W^{ij}$ , the weighted edge  $W_{ab}^{ij}$  that connects  $X_{ia}$  and  $X_{jb}$  is defined as below:

$$W_{ab}^{ij} = \begin{cases} \exp(-\frac{\|X_{ia} - X_{jb}\|_1}{t}), & \text{if } X_{ia} \text{ and } X_{jb} \text{ are "connected"} \\ 0, & \text{else} \end{cases} \quad (8)$$

Let  $Leighby_{ia}$  and  $Leighby_{jb}$  denote the labels of the  $K$ -nearest neighbors of  $X_{ia}$  and  $X_{jb}$ , which are measured by 1-norm distance. If  $label_{ia} \in Leighby_{jb}$  and  $label_{jb} \in Leighby_{ia}$ ,  $X_{ia}$  would be thought "connected" with  $X_{jb}$ . Taking this approach, the category discriminant information is introduced. Then we would put an edge between  $X_{ia}$  and  $X_{jb}$  based on 1-norm distance as Eq. (8) shows.

Furthermore, for the  $v$  views, MvLLS protects all connections between each pair views:

$$\min_{y^1, \dots, y^v} \sum_{1 \leq i, j \leq v} \xi(i, j) = \sum_{1 \leq i, j \leq v} y^i L^{ij} y^{jT} \quad (9)$$

$$\begin{aligned}
&= [y^1, y^2, \dots, y^v] \begin{bmatrix} L^{11} & L^{12} & \dots & L^{1v} \\ L^{21} & L^{22} & \dots & L^{2v} \\ \vdots & \vdots & \vdots & \vdots \\ L^{v1} & L^{v2} & \dots & L^{vv} \end{bmatrix} \begin{bmatrix} y^{1T} \\ y^{2T} \\ \vdots \\ y^{vT} \end{bmatrix} \\
&= \mathcal{Y} \mathcal{L} \mathcal{Y}^T \quad (10)
\end{aligned}$$

$$s.t. \mathcal{Y}\mathcal{D}\mathcal{Y}^T = 1 \quad (11)$$

where  $\mathcal{Y} = [y^1, y^2, \dots, y^v]$ ,  $\mathcal{L}$  is composed of  $[L^{11}, \dots, L^{vv}]$  as shown above, and  $\mathcal{W}$  is composed of  $[W^{11}, \dots, W^{vv}]$ :

$$\mathcal{W} = \begin{bmatrix} W^{11} & W^{12} & \dots & W^{1v} \\ W^{21} & W^{22} & \dots & W^{2v} \\ \vdots & \vdots & \vdots & \vdots \\ W^{v1} & W^{v2} & \dots & W^{vv} \end{bmatrix} \quad (12)$$

$\mathcal{W}$  is the global laplacian weighted graph (GLWP).  $L^{ij}$  is not a square matrix  
 235 always, as  $n_i$  may differ from  $n_j$ . But when we come to all  $v$  views in Eq. (10),  $\mathcal{L}$ ,  
 $\mathcal{W}$  and  $\mathcal{D}$  are exactly square matrices. Lagrange multiplier method is then em-  
 ployed to obtain the optimum solution of this problem, and the constraint that  
 $\mathcal{Y}\mathcal{D}\mathcal{Y}^T = 1$  ensures this problem has a unique solution. Finally, this problem  
 boils down to a problem of getting the smallest nonzero generalized eigenvalue  
 240 and feature vector:

$$\mathcal{L}\mathcal{Y}^T = \lambda\mathcal{D}\mathcal{Y}^T \quad (13)$$

How does GLWP introduce category discriminant information and protect  
 the local structure at the same time? On the one hand, category information  
 determines whether samples are connected or not, such that category discrim-  
 inant is introduced. And samples of the same class are always connected with  
 245 each other, as their  $K$ -nearest neighbors include themselves. Samples of dif-  
 ferent classes are still connected, if they are within the  $K$ -nearest neighbors of  
 each other. On the other hand, MvLLS expects to find a subspace where the  
 connected samples stay close as well. Therefore, all of the within-class or ad-  
 jacent samples tend to stay close in the subspace, while between-class samples  
 250 that are nonadjacent would have no effect to the subspace.

### 3.3. Laplacian partial least squares

Inspired by PLS, after getting  $\mathcal{Y}$  which is the embeddings of all views on the first dimension of the subspace,  $\mathcal{Y}$  is used as the regressor of  $\mathcal{W}$  to predict it. In another word, MvLLS removes the variation estimated by  $\mathcal{Y}$  from  $\mathcal{W}$  [38].

$$\mathcal{W} = P^T \mathcal{Y} + E \quad (14)$$

255 where  $P \in \mathbb{R}^{1 \times (n_1 + \dots + n_v)}$  is a loading vector that describes how closely  $\mathcal{W}$  is related to  $\mathcal{Y}$ .  $E$  is the residual matrix.

$$\begin{aligned} U &= \mathcal{Y} \mathcal{W} \\ P &= \frac{U \mathcal{W}}{U U^T} \\ E &= \mathcal{W} - P^T \mathcal{Y} \end{aligned} \quad (15)$$

As shown in Eq. (15),  $\mathcal{Y}$  is then used as a weight vector to produce the score of  $\mathcal{W}$  that is  $U$ , and therefore finding the loading vector  $P$ . Residual matrix  $E$  is got by removing the found variation of  $\mathcal{W}$ . Then  $(E + E^T)/2$  is assigned to  $\mathcal{W}$  260 to keep the symmetrical characteristic of  $\mathcal{W}$ , and the negative values of  $\mathcal{W}$  is set to zero. With the new GLWP  $\mathcal{W}$ , we can get a new embedding  $\mathcal{Y}$  as introduced in Eq. (9). This procedure is repeated for *dim* times to get the embeddings on each dimension of the target subspace.

### 3.4. Weighted local preserving embedding

265 As MvLLS is a nonlinear method, it could not get the embeddings of new samples directly. In order to meet the requirements of large-scale applications, an out-of-sample method weighted local preserving embedding (WLPE) is introduced for MvLLS. Inspired by the work of [39], WLPE finds an embedding in the subspace that maintains the local neighborhood structures of the high-dimensional space. WLPE keeps the global nonlinearity of MvLLS from the 270 local linear fits. Firstly, we get the 1-norm measured  $K$ -nearest neighbors for every sample in the original space, which includes samples from all views. Then

we characterize the local neighborhood structure by linear confidence, in other words, each sample is represented by a linearly weighted sum of its neighbors across all views. Reconstruction error is minimized in Eq. (16) to get the weights:

$$\begin{aligned} \min_M \epsilon(M) \quad & \sum_{1 \leq a \leq n} \|x_a - \sum_{1 \leq b \leq K} M_{ab} x_b\|_F^2 \\ \text{s.t.} \quad & \sum_b M_{ab} = 1 \end{aligned} \quad (16)$$

In Eq. (16),  $x_b$  is one of the  $K$  neighbors of  $x_a$ ,  $M_{ab}$  shows the contribution of  $x_b$  to the reconstruction of  $x_a$ . Lagrangian multiplier method is then employed to get the optimum solution:

$$\begin{aligned} 2M_a = \frac{1}{2} \lambda (G_a G_a^T)^{-1} e \\ G_a = [M_{a1}, M_{a2}, \dots, M_{ak}] \quad \begin{bmatrix} x_a - x_1 \\ x_a - x_2 \\ \vdots \\ x_a - x_k \end{bmatrix} \end{aligned} \quad (17)$$

In Eq. (17),  $e$  is a zero column vector except that the  $a^{th}$  element of  $e$  is 1. The neighbors that weighted greater in  $\mathcal{W}$  are expected to be more confident:

$$M'_{ab} = M_{ab} + \sum_{1 \leq i \leq n_1 + \dots + n_v} \mathcal{W}_{bi} \quad (18)$$

Then  $M'$  is normalized. Afterwords,  $M'$  is used to predict the low-dimensional embeddings of new samples. Embedding of the sample  $a$  would be represented as Eq. (19) shows:

$$y_a = \sum_{1 \leq b \leq K} y_b M'_{ab} \quad (19)$$

Finally, the precess of MvLLS is summarized in Algorithm 1.

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285	<b>Algorithm 1</b> MvLLS
	<b>Input:</b> $X_1, \dots, X_v, Label_1, \dots, Label_v, dim, K$ , a new sample $x_a$ .
	<b>Output:</b> $Y_1, Y_2, \dots, Y_v$ , embedding of the new sample $y_a$ .

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- 1: Project  $X_1, X_2, \dots, X_v$  and  $x_a$  to a common space with a DR framework.
- 2: Obtain  $W^{11}, \dots, W^{vv}$ , piece them into  $\mathcal{W}$  and obtain  $\mathcal{L}$ ,  $i = 1$ .
- 290 3: **Repeat**
- 4: Obtain the embedding of samples on the  $i^{th}$  dimension of the subspace  $\mathcal{Y}_i$  with Eq. (13);
- 5: Project  $\mathcal{W}$  on  $\mathcal{Y}_i$ , remove the predicted variation from  $\mathcal{W}$  to obtain a new graph with Eq. (15);
- 295 6: Make the new graph a symmetric and nonzero matrix;
- 7: Replace  $\mathcal{W}$  with the new graph, construct the new  $\mathcal{L}$  and  $\mathcal{D}$ ;
- 8: **Until**  $i$  is equal to  $dim$
- 9: Obtain embeddings on all dimensions  $\mathcal{Y} = [\mathcal{Y}_1; \mathcal{Y}_2; \dots; \mathcal{Y}_{dim}]$ ;
- 10: Obtain the  $K$  neighbors  $y_b$  and reconstruction contribution matrix  $M'$  of  $x_a$  with Eq. (17) and Eq. (18);
- 300 11:  $Y_1$  is set as the first  $n_1$  columns of  $\mathcal{Y}$ ,  $Y_2$  is set as the second  $n_2$  columns of  $\mathcal{Y}$ ,  $\dots$ ,  $Y_v$  is the last  $n_v$  columns of  $\mathcal{Y}$ ;
- 12:  $y_a = \sum_{1 \leq b \leq K} y_b M'_{ab}$ .
- 13: Output  $Y_1, Y_2, \dots, Y_v$  and  $y_a$ .

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### 305 3.5. Extensions

In this section, we further present some extensions of MvLLS in detail.

- (1) The unsupervised and semi-supervised versions of MvLLS. As the construction of  $\mathcal{W}$  is very flexible, MvLLS has its unsupervised and semi-supervised versions. We reconstruct  $W^{ij}$  with  $x_{ia}$  and  $x_{jb}$  here, then the new  $\mathcal{W}$  can be pieced up. For unsupervised learning, if neither  $label_a^i$  nor  $label_b^j$  are given,  $x_{ia}$  and  $x_{jb}$  would be “connected” when  $\|x_{ia} - x_{jb}\|_2^2 < \epsilon$ , where  $\epsilon$  is an adjustable parameter. For semi-supervised learning, if  $label_a^i$  is given while  $label_b^j$  is not, they would be “connected” when both of the two samples are



within the  $K$ -nearest neighbors of each other, or  $label_{ia} \in Leighby_{jb}$ . Of  
 315 course, there could be many other construction method based on different  
 starting points or optimization targets.

(2) Estimation of intrinsic dimension of the subspace. As the global laplacian  
 weighted graph  $\mathcal{W}$  upgrades gradually with each iteration, the intrinsic  
 dimension could be estimated when  $\mathcal{W}$  tends to be stable. Suppose that the  
 320 weighted graph after a single iteration is  $\mathcal{W}'$ , we would think the subspace  
 is stable when  $\|\mathcal{W}' - \mathcal{W}\|_F^2 < \epsilon$ , where  $\epsilon$  is an adjustable parameter.

#### 4. Experiments

In this section, we compare the performance of MvLLS with some state-of-  
 art methods on two human emotion datasets: RGB-D human video-emotion  
 325 dataset and KDEF human face-emotion dataset. We evaluate the proposed  
 method on human emotion recognition of multi-sensor, multi-pose, and multi-  
 feature. Many experiments are designed to show the effeteness and robustness  
 of MvLLS, detailed discussions and comparisons are presented as well.

##### 4.1. Dataset descriptions and feature representations

330 RGB-D human video-emotion dataset [40] includes 4224 clips of RGB video  
 and 4224 clips of Depth video belonging to 7 emotion categories: angry, dis-  
 gusted, fearful, happy, neutral, sad, and surprised. To get these clips, profes-  
 sional actors were employed to perform human emotion scripts that are designed  
 under psychological principles. In Fig. 2, some discontinuous frames show a per-  
 335 formance of sad emotion, from right, middle and left.

For the RGB-D human video-emotion dataset, we extracted the 3-Dimensional  
 Convolutional Neural Networks (3D-CNN) feature, which is a popular and effec-  
 tive method for video learning and feature extraction. As a modified version of  
 BVLC\_caffe to support 3D-CNN, C3D-1.0 [41, 42, 43] trained on UCF-101 [44]  
 340 is used to extract the features. And features of RGB view and Depth view both  
 have a dimension of 4096.

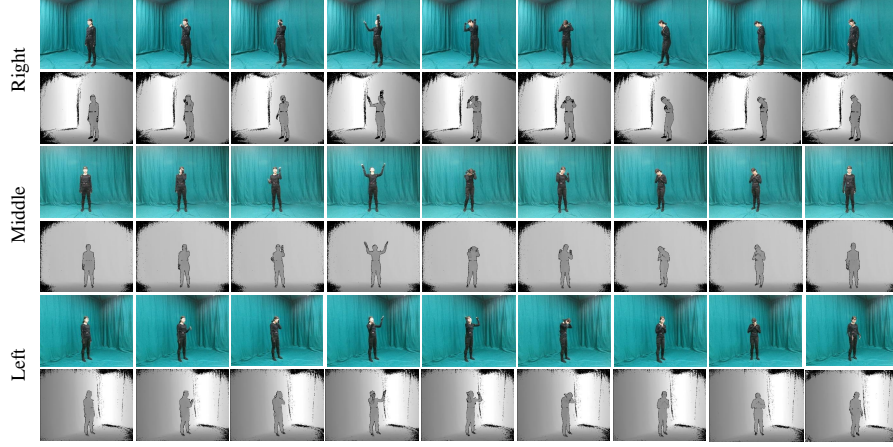


Fig. 2: An example of sad emotion from RGB-D human video-emotion dataset.

Karolinska Directed Emotional Faces (KDEF) dataset [45, 46] consists of 4900 pictures of 7 human facial emotions: afraid, angry, disgusted, happy, neutral, sad, surprised. A total number of 70 participants were employed to perform these emotions from 5 angles: full left, half left, straight, half right and full right. In this paper we select angles of half left, half right and straight, which include 2940 images totally. Fig. 3 shows examples of surprised, angry and happy emotions from half left, straight and half right angles in KDEF dataset.



Fig. 3: Examples of surprised, angry and happy from three different angles in KDEF dataset.

For the KDEF dataset, three features are extracted for each selected image with the 2nd last layer of Xception network [47], the 2nd last layer of Inception network [48], and the 6th last layer of MobileNet [49]. All networks are pre-trained on ImageNet [50]. Dimensions of the features are 2048, 1024 and 2048 respectively.

#### 4.2. Comparison methods and experimental setting

355 We evaluate the proposed method with as many as two-view and multi-view learning methods that we can compare with, including CCA, PLS, MCCA, MULDA, GMA, MvDA and MvDA-VC. All experiments about the comparison methods are conducted with available codes.

360 After extracting the features of both datasets, C3D feature of RGB view and Depth view from the RGB-D human video-emotion dataset are used in human emotion recognition across sensors (multi-sensor task); MobileNet feature of half left, half right and straight angles of KDEF dataset are used in human emotion recognition across poses (multi-pose task); and Xception feature, Inception feature, and MobileNet feature of straight view in KDEF dataset are  
365 used in human emotion recognition across features (multi-feature task).

Averaged classification accuracy is used to evaluate the performance of different methods. Each experiment is randomly repeated for 10 times and the results are averaged. If there is no special explanation, the dimension of subspace  $dim$  of each experiment is set to the minimum of its all views, to preserve  
370 as much as energy. DR framework used in the experiments is PCA [36], as PCA may be the most classical, effective and widely used DR framework. In multi-sensor experiments, the parameter  $t$  of Eq. (8) is set to 1000, the number of neighbors  $K$  is set to 50; in multi-pose and multi-feature experiments,  $t$  is set to 200 and  $K$  is set to 300. And extreme learning machine (ELM) [51] is  
375 used as the classifier for all experiments. ELM is a classical feedforward network with a single hidden layer, the number of hidden layer node is set to 8000, with *sigmoid* function as the activation function.

#### 4.3. Comparisons and evaluations

##### 4.3.1. Evaluation as a whole

380 In this section, we compare MvLLS with some two-view or multi-view learning method on the three tasks, 2/3 data of each view is randomly selected for training with the others for testing. Table 2 and Table 3 show the average accuracy of each view for both datasets before the subspace learning. Table 4 shows

the comparisons between MvLLS and many other methods on human emotion  
 385 recognition of the multi-sensor, multi-pose and multi-feature task. CCA and  
 PLS could not be used in multi-pose task and multi-feature task as they are  
 two-view learning methods, such that the corresponding spaces in Table 4 are  
 marked as “-”. Experimental results indicate that MvLLS performs better than  
 other methods. In the multi-sensor emotion recognition task, average classifi-  
 390 cation accuracy is improved by 2.42% (=48.41%-45.59%) from MvDA-VC, the  
 best performing comparison method. And in the multi-pose emotion recogni-  
 tion task, the average accuracy is improved by 4.38% (=74.02%-69.64%) from  
 MvDA-VC; in the multi-feature emotion recognition task, the average accuracy  
 is improved by 3.57% (75.71%-72.14%) from MvDA-VC. Specially, it can be  
 395 observed that MvLLS performs better than any single view before multi-view  
 learning.

Table 2: The average accuracy of each view for RGB-D video-emotion dataset (%)

Feature	RGB view	Depth view
C3D feature	37.97	31.72

Table 3: The average recognize accuracy of each view for KDEP dataset (%)

Feature	Half Left	Half Right	Straight
Xception feature	64.11	65.09	72.18
Inception feature	56.50	57.79	68.07
MobileNet feature	66.27	66.07	73.74

The improvements of MvLLS in average accuracy could be boiled down to  
 its great nonlinear learning, scatter discriminant balance and locality protection  
 characters. CCA and GMA perform poorly as the inter-view and intra-view  
 400 information is not considered. By using iterative approximation, PLS performs  
 much better than CCA. MvDA jointly learns between-class variation and within-  
 class variation across all views, while the entirety of each view and locality is

Table 4: Comparisons on three tasks in terms of average accuracy (%)

Task	CCA	PLS	MCCA	MULDA	GMA	MvDA	MvDA-VC	MvLLS
Multi-sensor	13.08	40.63	15.15	32.63	35.20	43.65	45.99	48.41
Multi-pose	-	-	35.02	43.21	47.50	61.07	69.64	74.02
Multi-feature	-	-	38.57	46.63	56.79	60.02	72.14	75.71

not taken into consideration. And MvDA-VC has a significant improvement than MvDA by adding view-consistency. The proposed method MvLLS takes  
405 advantages of PLS, category discriminant information and locality information, then get better performance in average accuracy.

#### 4.3.2. Evaluation with different training sizes

To analyze the robustness of the proposed method, we evaluate the average classification accuracy with different training sizes. Multi-pose and multi-feature task are taken as examples. Fig. 4 and Fig. 5 show the accuracies with different  
410 training sizes for multi-pose and multi-feature task respectively. The training size is set in change interval of [10, 90] (%) with the step size of 10. And from these tables, we can observe that MvLLS outperforms than all related methods with different training size.

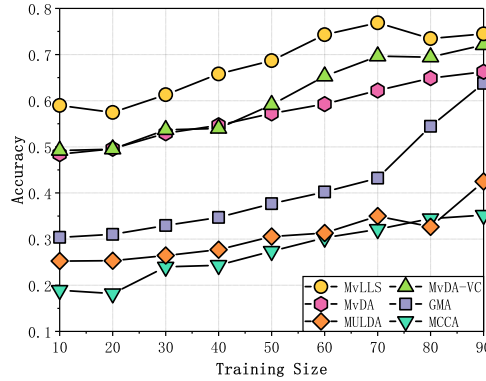


Fig. 4: Comparisons of average accuracy for multi-pose task with different training Sizes.

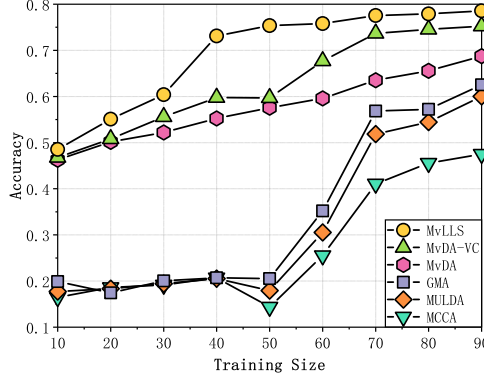


Fig. 5: Comparisons of average accuracy for multi-feature task with different training sizes.

When training size is extremely low, all methods could not learn enough information. When training size is high enough, MvDA, MvDA-VC and MvLLS learn surplus information. When the training size is close to 50%, MvLLS performs much better than other methods. That is because MvLLS could make full use of category discriminant information and local neighborhood information, and WLPE gets new samples involved in known samples very well. MvDA and MvDA-VC focus more on scatter discriminant information, GMA just consider the cross correlations, MULDA ignores the local structure as well.

#### 4.3.3. Evaluation with different dimensions of the subspace

In this section we compare the performance of each method on different dimensions of the subspace. Multi-pose task and multi-feature task are taken as examples as well. For the both tasks,  $dim$  varies in change interval of [100, 1000] with the step size of 100. Fig. 6 and Fig. 7 indicate that MvLLS could get the best classification accuracy as  $dim$  varies.

MvLLS performs well when  $dim$  is extremely low, which means the subspace got by MvLLS is more representative and typical. Furthermore, MvLLS performs better and better as  $dim$  improves, because MvLLS is a nonlinear method optimized with iteration method. MvLLS removes the estimated variations of the embeddings gradually to get a proper solution, while other methods get

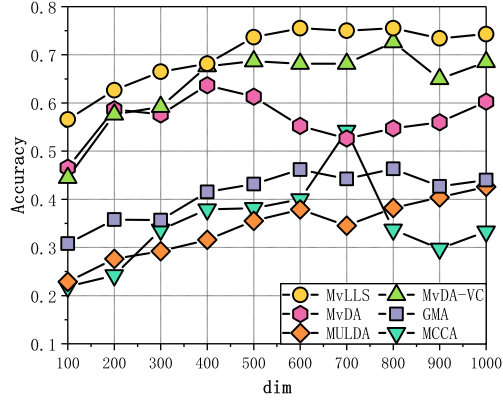


Fig. 6: Comparisons of average accuracy for multi-pose task on different target dimensions.

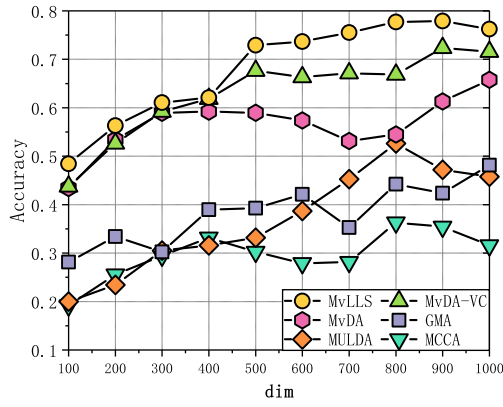


Fig. 7: Comparisons of average accuracy for multi-feature task on different target dimensions.

linear transformers directly.

#### 4.3.4. Evaluation of the effectiveness of interactive method

To analyse the effectiveness of interactive method used in MvLLS, we conduct experiments on the three tasks to compare the average accuracy between MvLLS and its non-iterative version (called MvLLS<sub>noITE</sub>). Similarly, 2/3 data of each view is used as the training set with the others as the test set. From Table 8 it can be observed that the average classify accuracy is improved by nearly 1% for each task when iterative method is used.

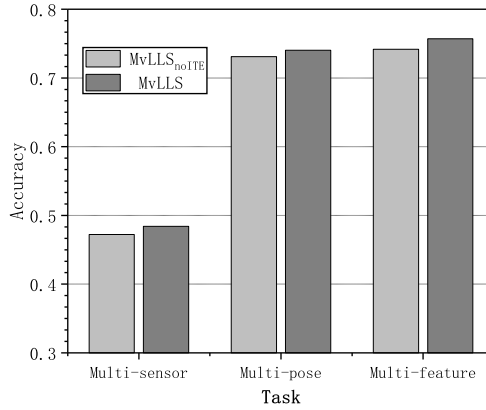


Fig. 8: Comparisons of average accuracy between MvLLS and MvLLS<sub>noITE</sub>

#### 4.3.5. Evaluation of influence of the parameters

The coefficient  $t$  and the number of neighbor  $K$  in the neighborhood are two important parameters in MvLLS. Taking the multi-sensor task as an example, we conduct experiments to evaluate the influence of the two parameters. In Table 5,  $K$  is set as 50 and  $t$  varies in the interval of [600, 1400] with the step size of 100. And in Table 6,  $t$  is set as 1000 and  $K$  varies in the interval of [10, 90] with the step size of 10. We can draw the conclusion that  $t$  has little influence on MvLLS, but MvLLS performs worse when the value of  $K$  is extremely low. That is due to each sample would not be represented well and not many samples would be connected. In general, MvLLS has fine robustness as parameter varies.



Table 5: Influence of  $t$  in the multi-sensor recognition task (%)

t	600	700	800	900	1000	1100	1200	1300	1400
Accuracy	48.33	48.41	48.72	48.25	48.88	48.64	48.52	48.71	48.53

Table 6: Influence of  $K$  in the multi-sensor recognition task (%)

K	10	20	30	40	50	60	70	80	90
Accuracy	43.86	46.53	47.17	48.28	48.41	48.33	48.41	48.64	48.32

## 5. Conclusion

In this paper, a flexible and extensible nonlinear method multi-view laplacian least square (MvLLS) is proposed for multi-view human-emotion recognition. MvLLS finds a common subspace across all views where the connected samples stay close to each other as well. With the global laplacian weighted graph (GLWP), MvLLS introduces the category discriminant information and protects the local neighborhood information. MvLLS is optimized with interactive method, and the weighted local preserving embedding (WLPE) is the out-of-sample extension of MvLLS. Experimental results verified the effectiveness and robustness of the proposed method.

In the future, we will work to reduce the time complexity of MvLLS, and evaluate MvLLS with more datasets.

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**Lin Feng** received the B.S. degree in electronic technology from Dalian University of Technology, China, in 1992, the M.S. degree in power engineering from Dalian University of Technology, China, in 1995, and the PhD degree in mechanical design and theory from Dalian University of Technology, China, in 2004. He is currently a professor and doctoral supervisor in the School of Innovation and Entrepreneurship, Dalian University of Technology, China. His research interests include intelligent image processing, robotics, data mining, and embedded systems.



**Shuai Guo** received the B.S. degree in the School of Computer Science and Technology from Dalian University of Technology, in 2017. Currently, he is working toward the M.S. degree in the School of Innovation and Entrepreneurship, Dalian University of Technology. His research interests include multi-view learning, dimensionality reduction, image and video learning.

630



**Zhan-Bo Feng** is working toward the B.S. degree in the School of Electronic Information and Electrical Engineering, Dalian University of Technology. His research interests include reinforcement learning, robot control and collaboration.



**Yi-Hao Li** is working toward the B.S. degree in the School of Electronic Information and Electrical Engineering, Dalian University of Technology. His research interests include computer vision and deep learning.



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**Yang Wang** is a M.S. degree candidate in the School of Innovation and Entrepreneurship, Dalian University of Technology. His research interests include information retrieval, computer vision and machine learning.





**Sheng-Lan Liu** received the Ph.D. degree in the School of Computer Science and Technology, Dalian University of Technology, China, in 2015. Currently, he is an associate professor with the School of Innovation and Entrepreneurship, Dalian University of Technology, China. His research interests include manifold learning, human perception computing. Dr. Liu is currently the editorial board member of Neurocomputing.



**Hong Qiao** (SM'06) received the B.Eng. degree in hydraulics and control and the M.Eng. degree in robotics and automation from Xi'an Jiaotong University, Xi'an, China, and the Ph.D. degree in robotics control from De Montfort University, Leicester, U.K., in 1995. She was an Assistant Professor with the City University of Hong Kong, Hong Kong, and a Lecturer with the University of Manchester, Manchester, U.K., from 1997 to 2004. She is currently a Professor with the State Key Laboratory of Management and Control for Complex Systems, Institute of Automation, Chinese Academy of Sciences, Beijing, China. Her current research interests include robotics, machine learning, and pattern recognition.